

Status of γ/ϕ_3 measurement @ Belle + Belle II

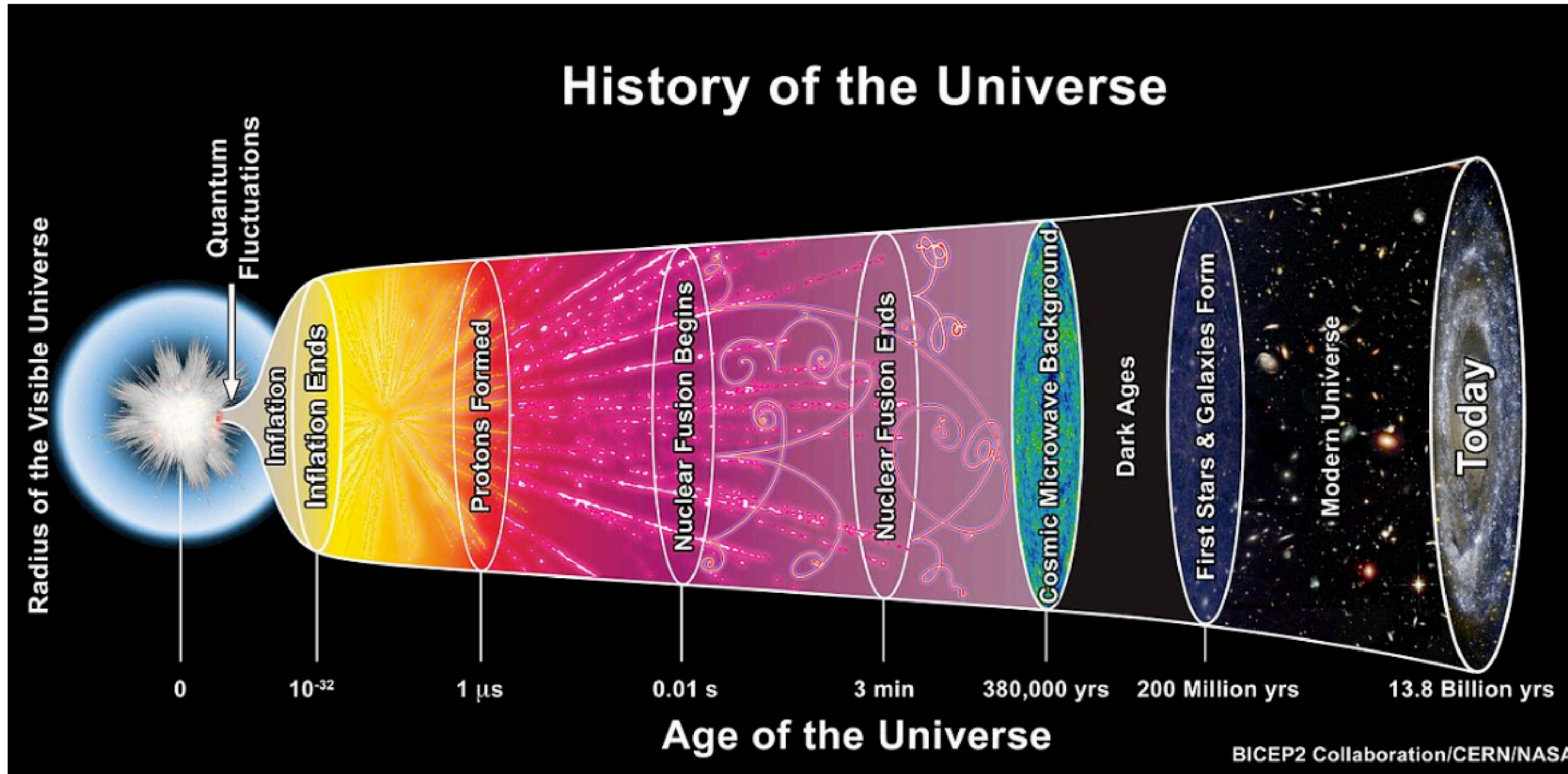
Xiaodong Shi
KEK, IPNS
2023.08.31 @ USTC



Outline

- **Why CPV is interesting and what is CKM matrix**
- About γ/ϕ_3
- SuperKEKB and Belle II
- All γ/ϕ_3 results from Belle and Belle II
- Discussion and outlook

Matter-antimatter asymmetry



- Same anti-matter and matter in the initial period.

- But now we observe much more matter than anti-matter!

$$\frac{N_B - N_{\bar{B}}}{N_B + N_{\bar{B}}} \sim 10^{-10}$$

Matter-antimatter asymmetry, CP violation

- In 1967, Andrei Sakharov proposed three conditions for the matter-antimatter asymmetry:
 - Baryon number violation
 - **C and CP violation**
 - Interactions out of thermal equilibrium
- So we shall understand **CP violation (CPV)**!

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- In 1964, first CPV observation in Kaon system
- In 2001, CPV observed in B system
- In 2019, direct CPV observed in D system by LHCb
- Standard Model (SM) can describe these CPV by a phase in Cabibbo-Kobayashi-Maskawa (CKM) matrix.

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- SM only gives $\sim 10^{-17}$,

$$\frac{N_B - N_{\bar{B}}}{N_B + N_{\bar{B}}} \sim \mathbf{10^{-10}}$$

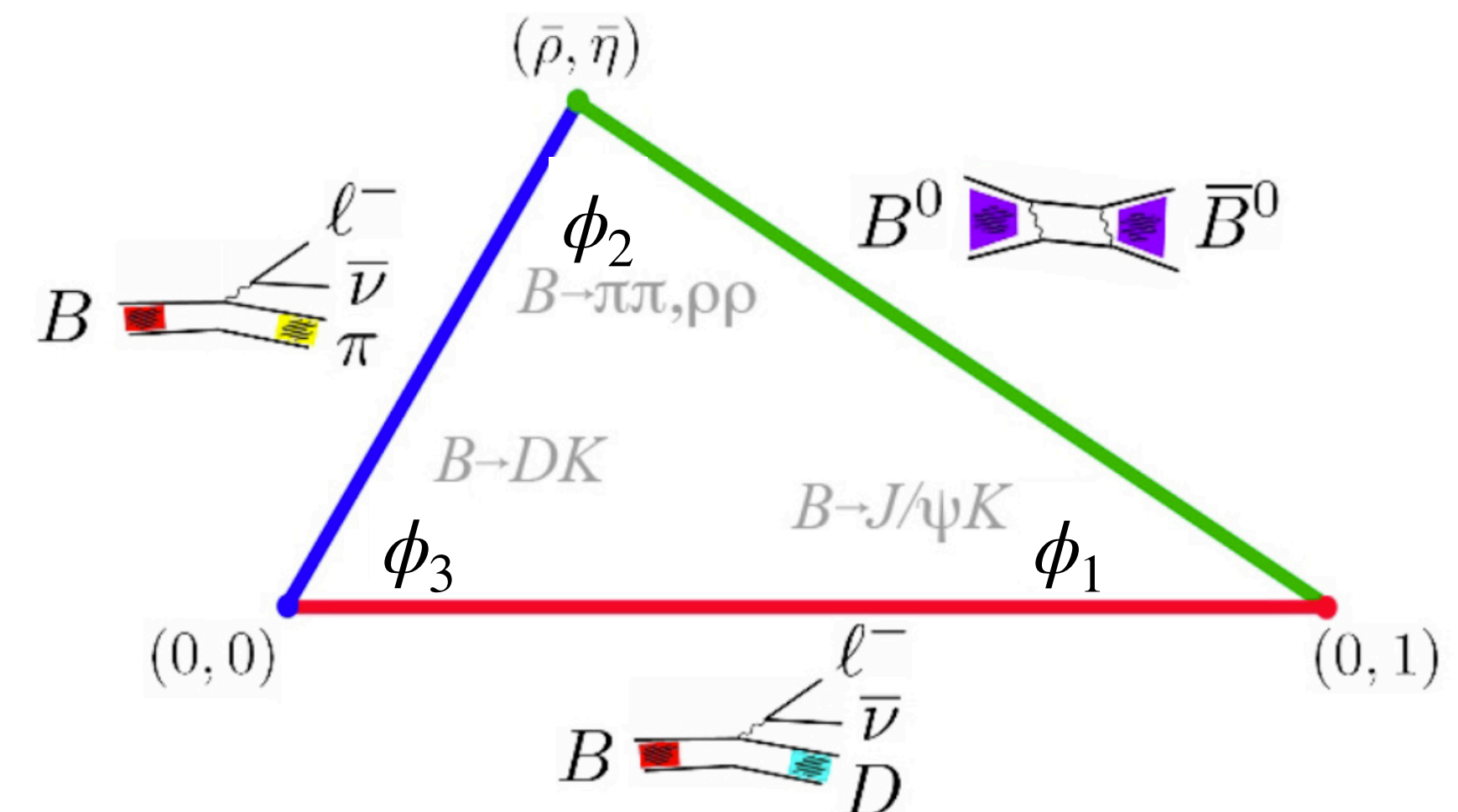
- need extra sources of CPV. Hint of NP?

CKM matrix and the unitary triangle

$$\begin{pmatrix} u \\ c \\ t \end{pmatrix} \leftarrow W^\pm \rightarrow \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

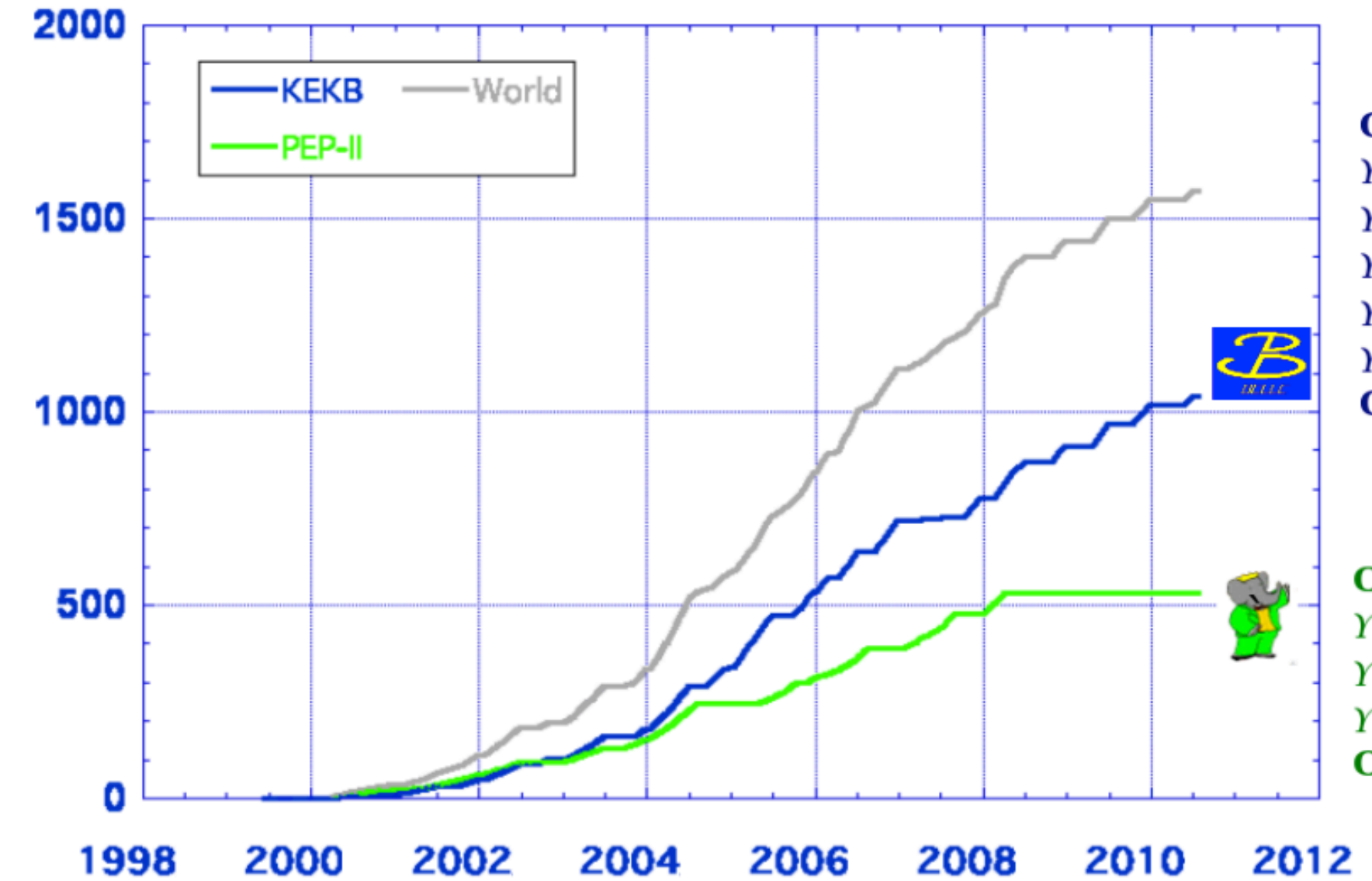
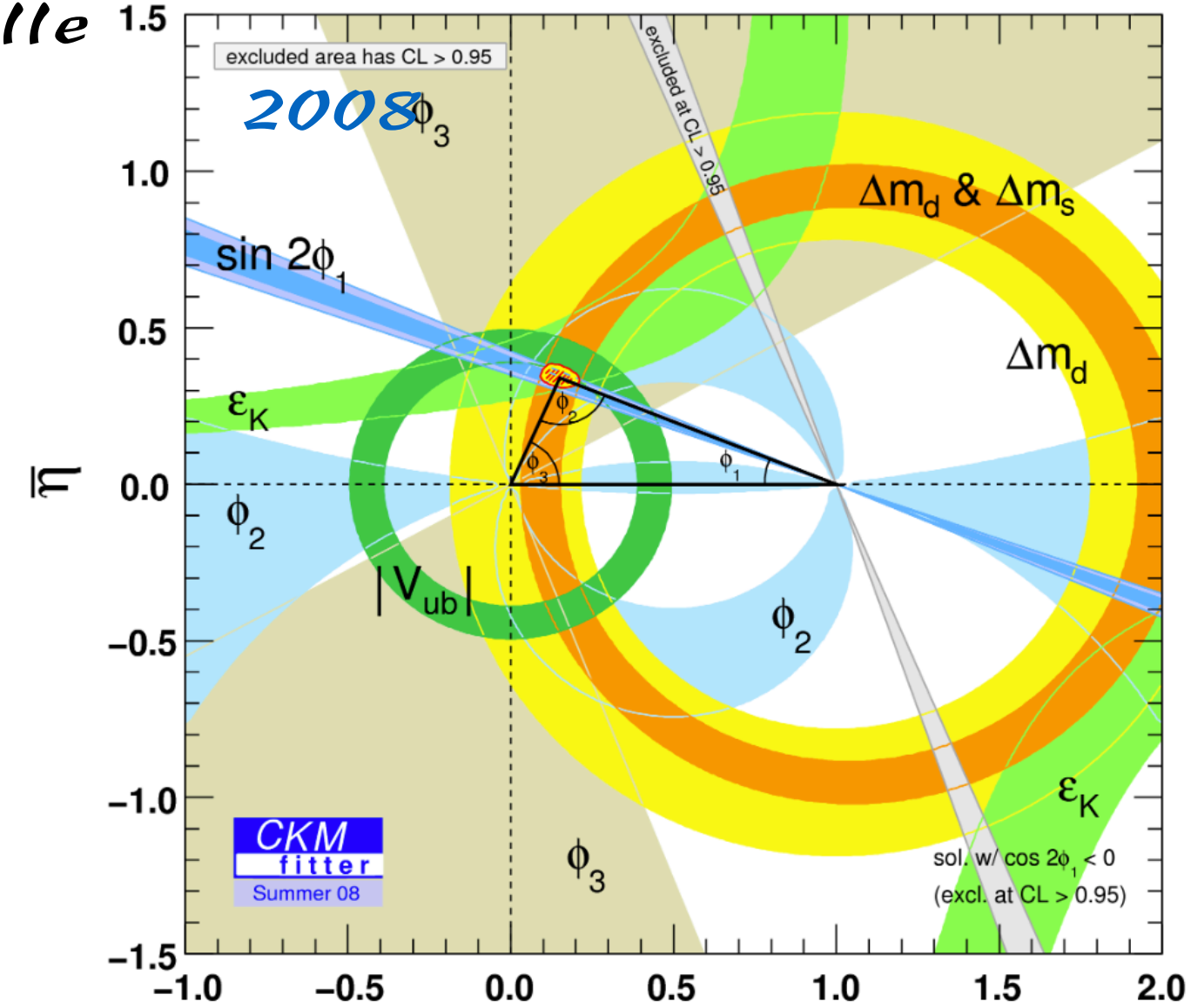
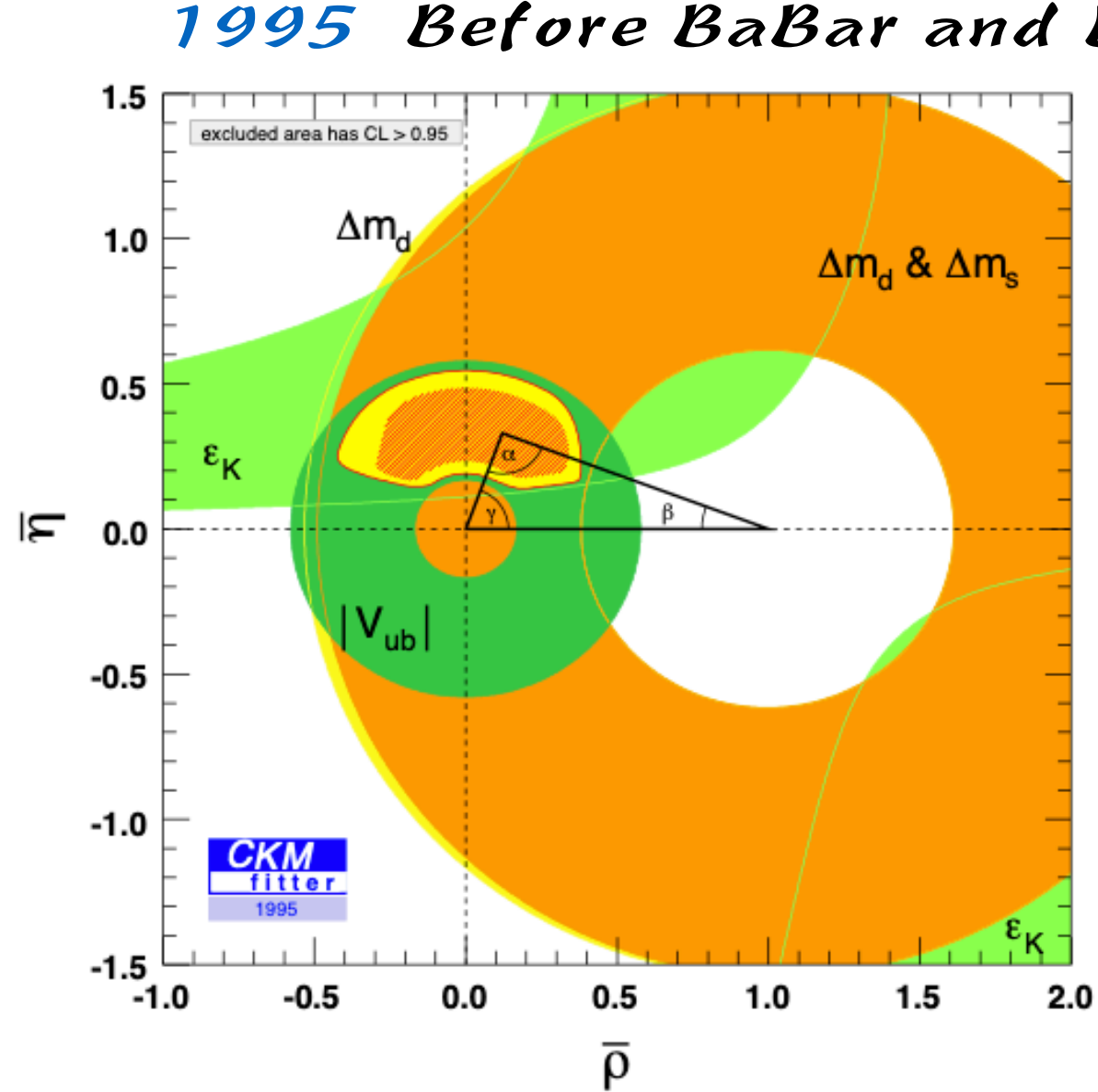
- CKM matrix connects u - and d -type quarks via weak force
- In SM, CKM matrix is unitary: four free parameter, one of them is the complex phase, the only one source of CPV in quark sector in SM!
- One way to examine this CKM matrix: examine the unitarity:

$$\sum_i V_{ik} V_{il}^* = \sum_i V_{ki} V_{li}^* = \delta_{kl}$$
- One “popular” case: $V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$



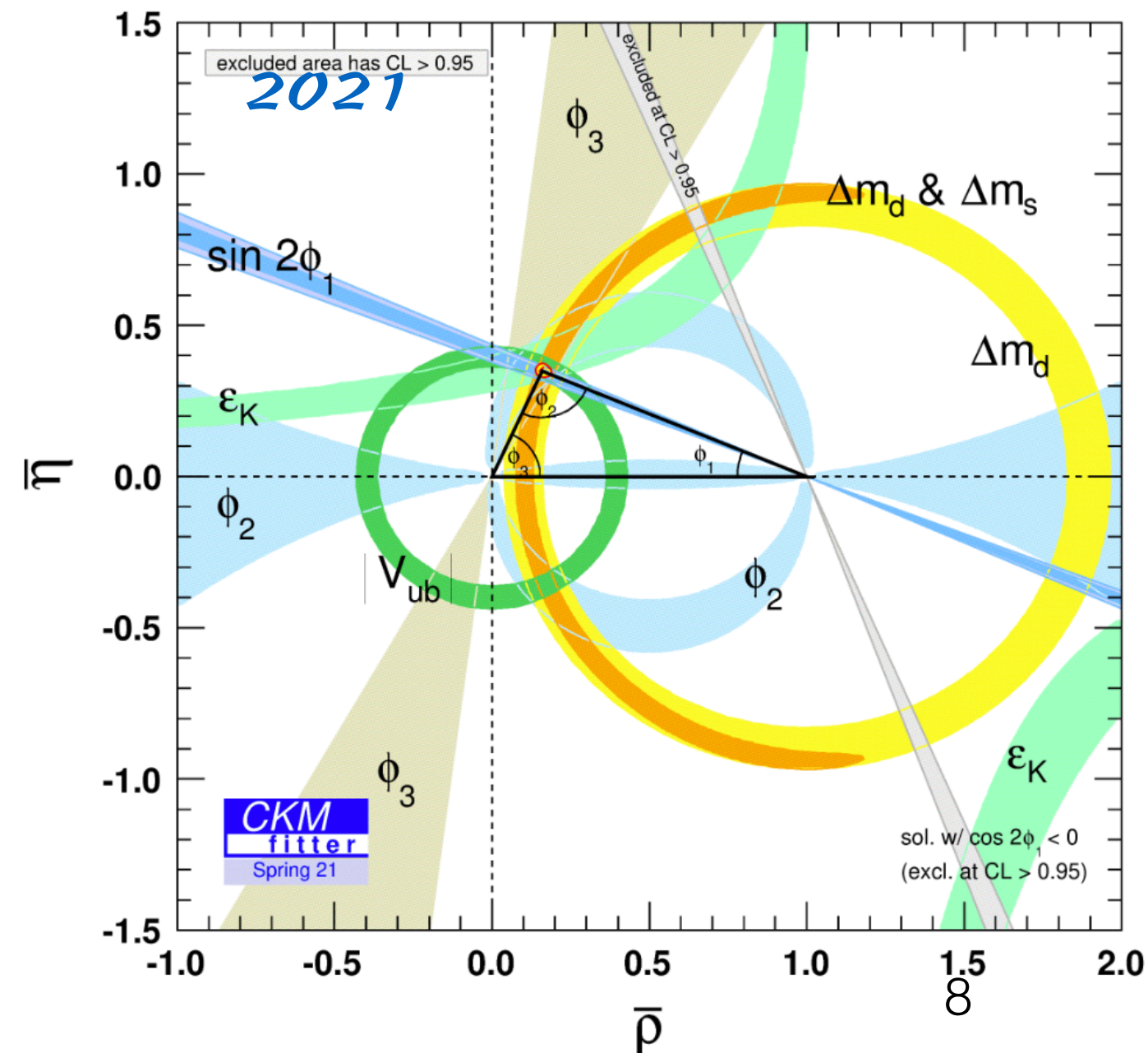
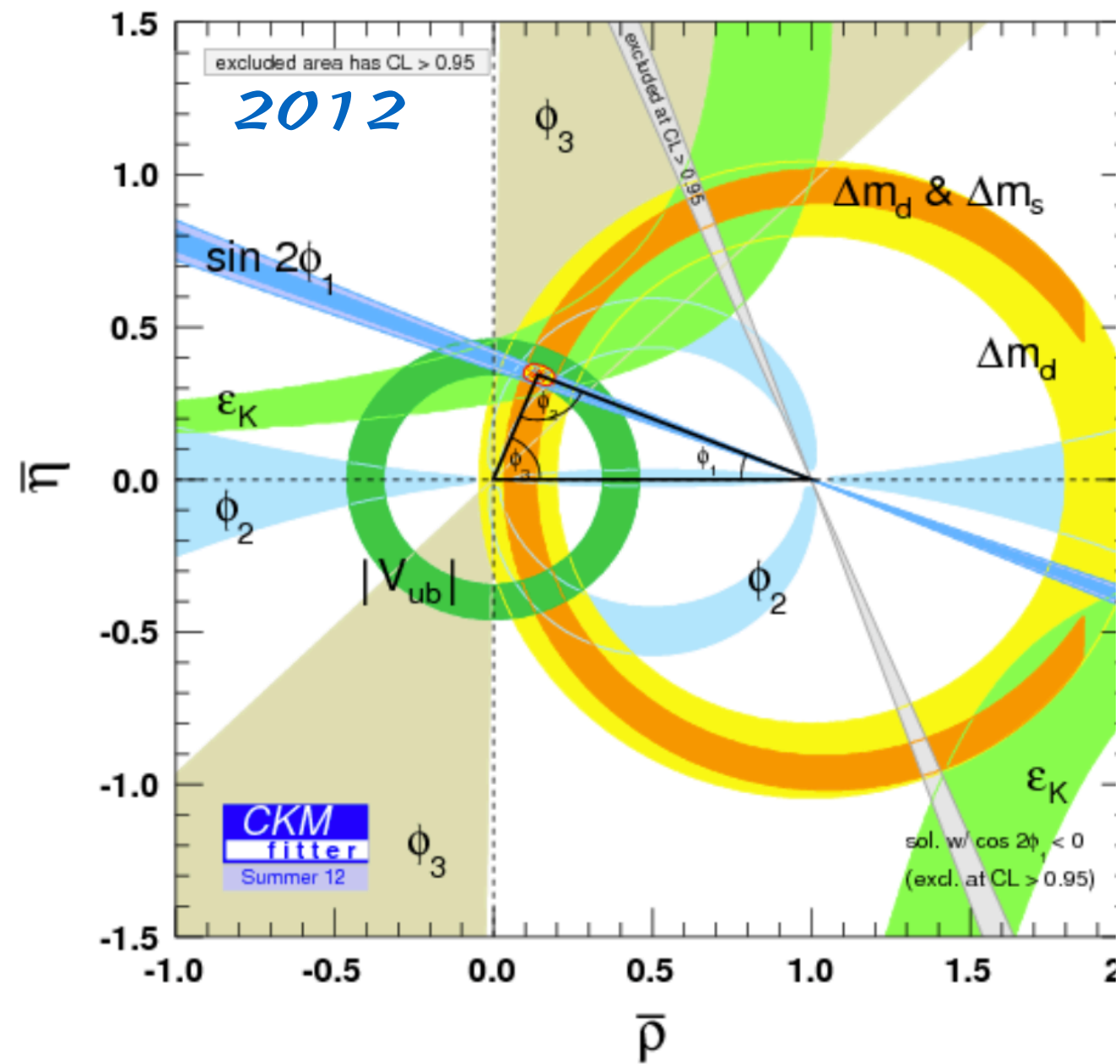
Is the triangle closed? (Hint of New Physics?)

1995 Before BaBar and Belle



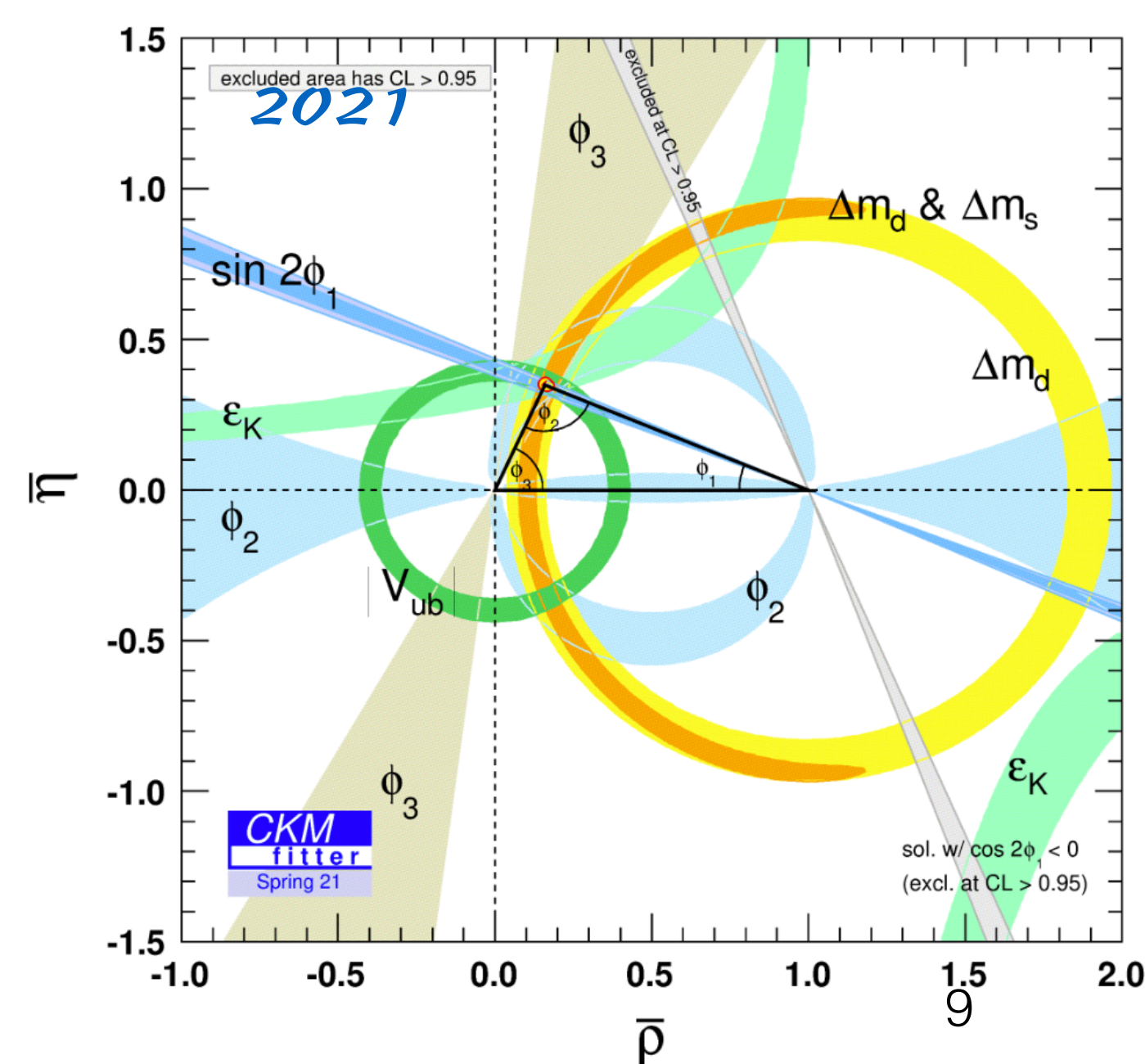
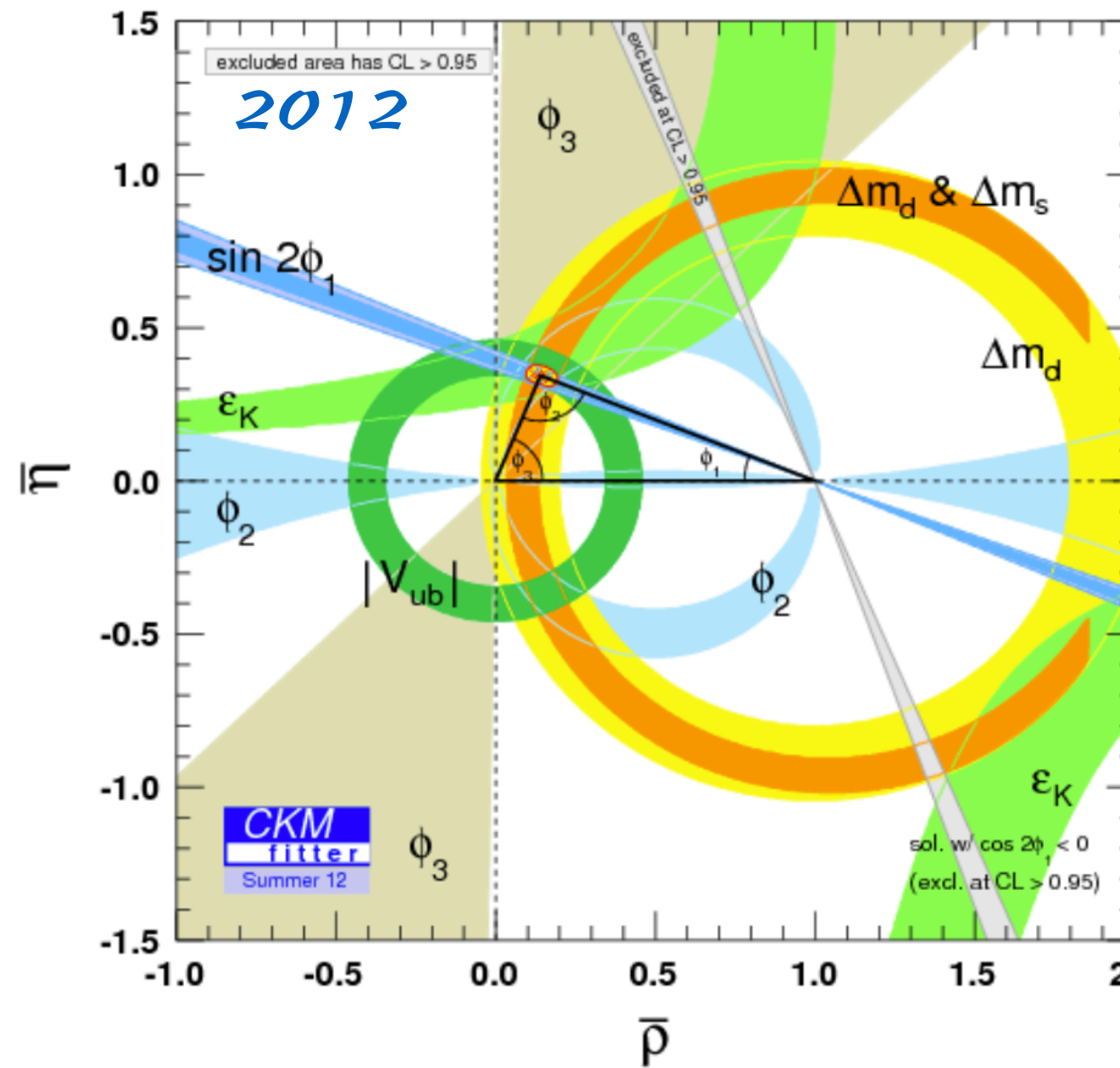
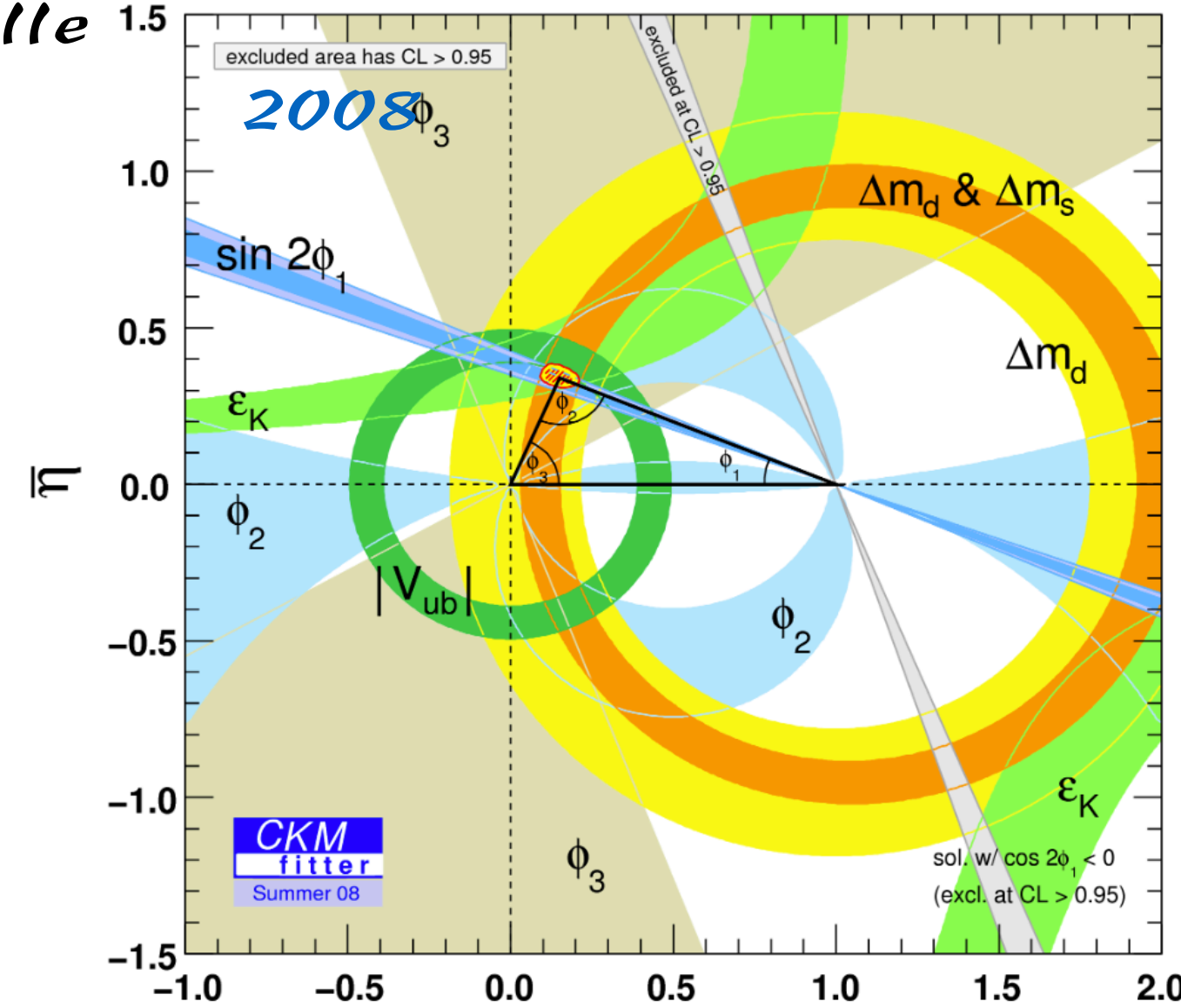
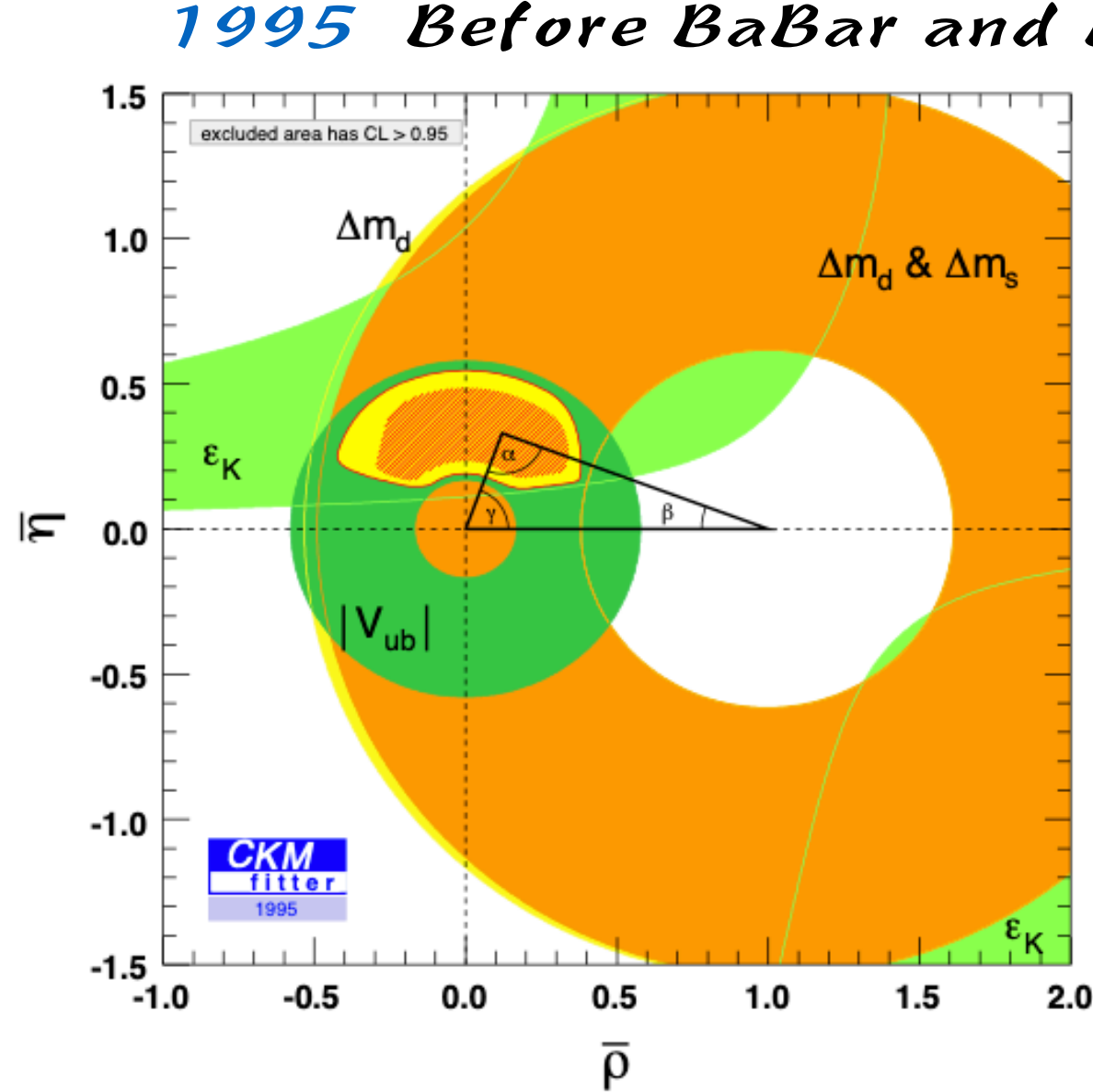
> 1 ab⁻¹
On resonance:
 $Y(5S): 121 \text{ fb}^{-1}$
 $Y(4S): 711 \text{ fb}^{-1}$
 $Y(3S): 3 \text{ fb}^{-1}$
 $Y(2S): 24 \text{ fb}^{-1}$
 $Y(1S): 6 \text{ fb}^{-1}$
Off reson./scan:
 $\sim 100 \text{ fb}^{-1}$

~ 550 fb⁻¹
On resonance:
 $Y(4S): 433 \text{ fb}^{-1}$
 $Y(3S): 30 \text{ fb}^{-1}$
 $Y(2S): 14 \text{ fb}^{-1}$
Off resonance:
 $\sim 54 \text{ fb}^{-1}$



Is the triangle closed? (Hint of New Physics?)

1995 Before BaBar and Belle



- With results from BaBar, Belle, and LHCb's Run1,2 data, the triangle is still closed.

- $\phi_1 = \beta = \arg\left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right), (22.2 \pm 0.7)^\circ$

- $\phi_2 = \alpha = \arg\left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*}\right), (85.2^{+4.8}_{-4.3})^\circ$

- $\phi_3 = \gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right), (66.2^{+3.4}_{-3.6})^\circ$
HFLAV

- With much more data from LHCb and Belle II, we could shrink the uncertainty, test this triangle and look for hints from new physics.

Outline

- Why CPV is interesting and what is CKM matrix
- **About γ/ϕ_3**
- SuperKEKB and Belle II
- All γ/ϕ_3 results from Belle and Belle II
- Discussion and outlook

About ϕ_3

$$V_{CKM} = \begin{matrix} & \begin{matrix} d & s & b \end{matrix} \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta + \frac{i}{2}\eta\lambda^2) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 - i\eta A^2\lambda^4 & A\lambda^2(1 + i\eta\lambda^2) \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} \end{matrix} + \mathcal{O}(\lambda^6) \quad (\sim 10^{-4})$$

Wolfenstein expansion in powers of the Cabibbo angle, λ , up to λ^5

$$\phi_3 = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right) = \arg\left(-\frac{V_{ub}^*}{V_{cb}^*}\right)$$

Zero
phase in
 V_{ud}, V_{cd}

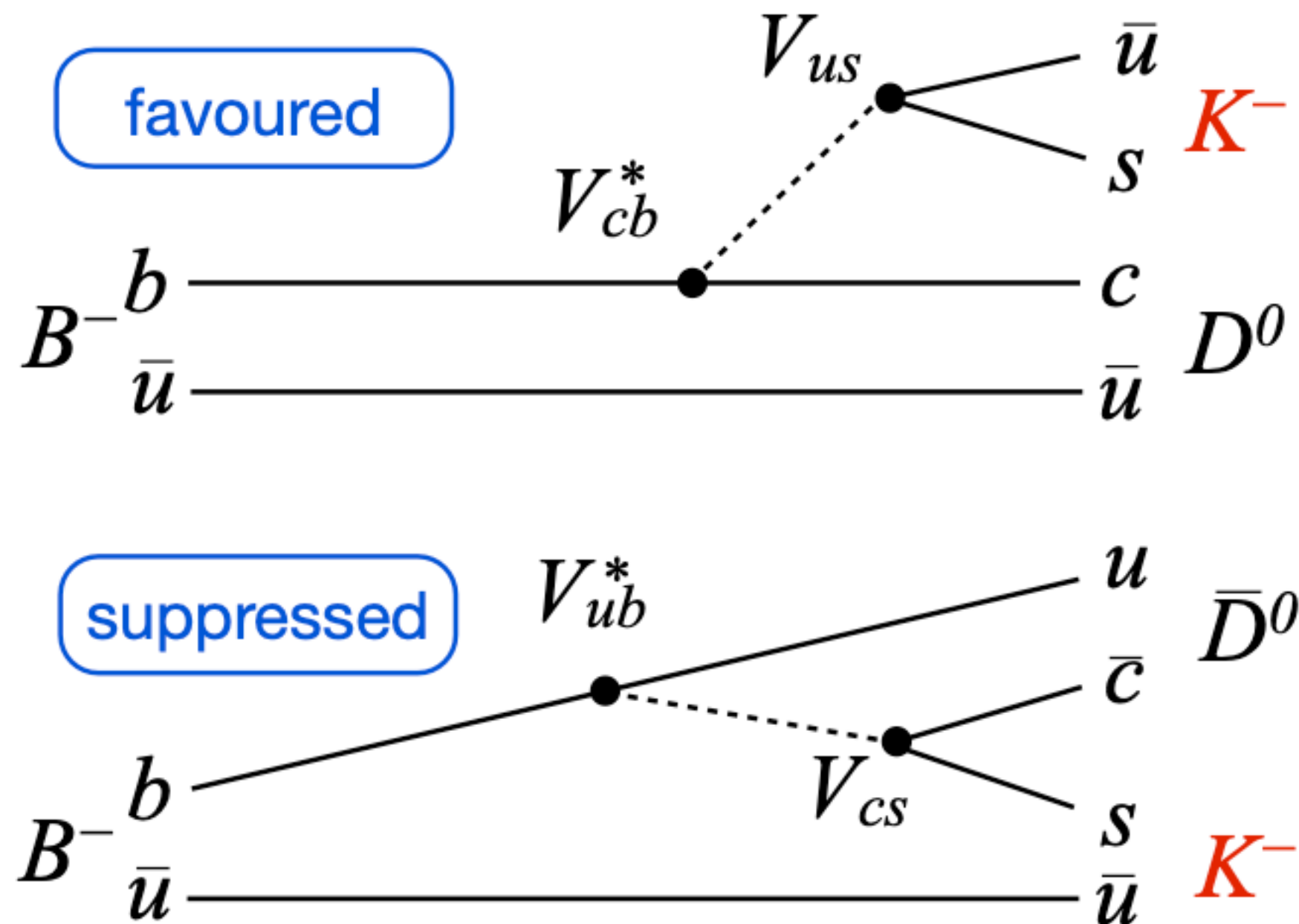
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Zero phase in V_{ud}, V_{cd}

$$\phi_3 = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right) = \arg\left(-\frac{V_{ub}^*}{V_{cb}^*}\right)$$



relative amplitude:

weak phase difference:

$$\left| \frac{V_{cs} V_{ub}^*}{V_{us} V_{cb}^*} \right| f_{col}$$

$$\arg\left(-\frac{V_{cs} V_{ub}^*}{V_{us} V_{cb}^*}\right)$$

$$= r_B \approx 0.1$$

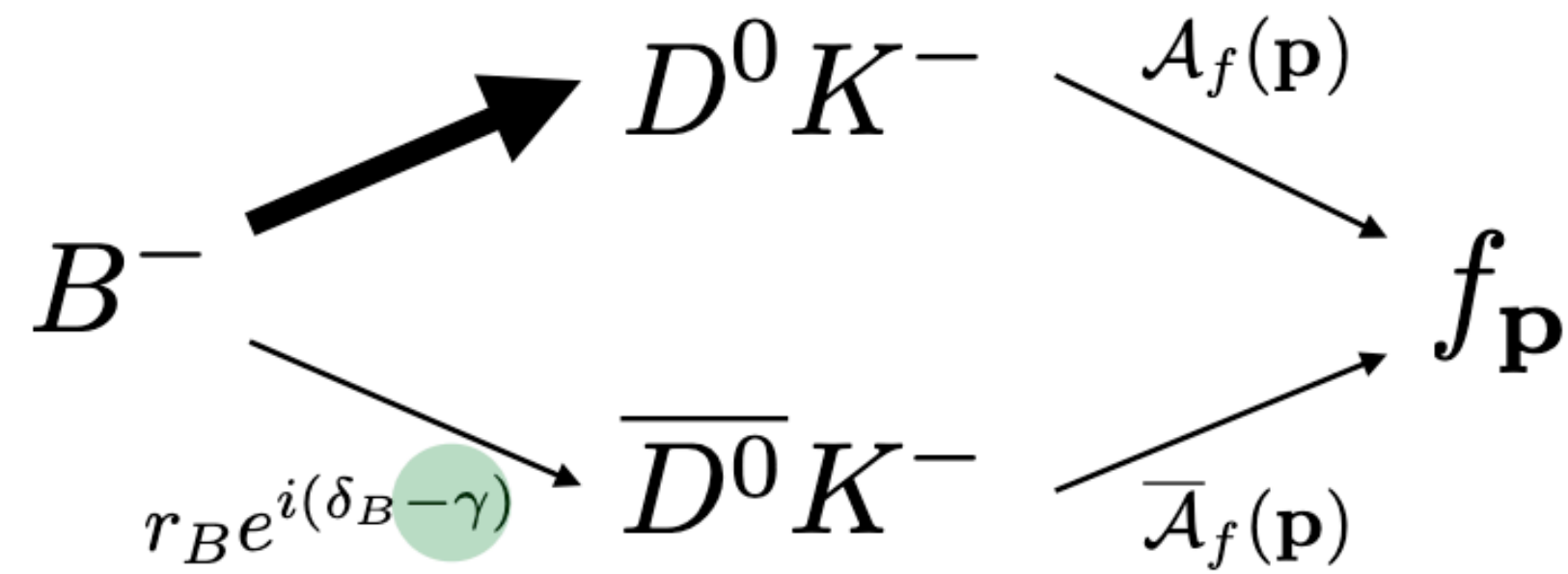
$$= \arg\left(-\frac{V_{ub}^*}{V_{cb}^*}\right)$$

relative strong phase:

$$= \delta_B$$

$$= \phi_3$$

About ϕ_3

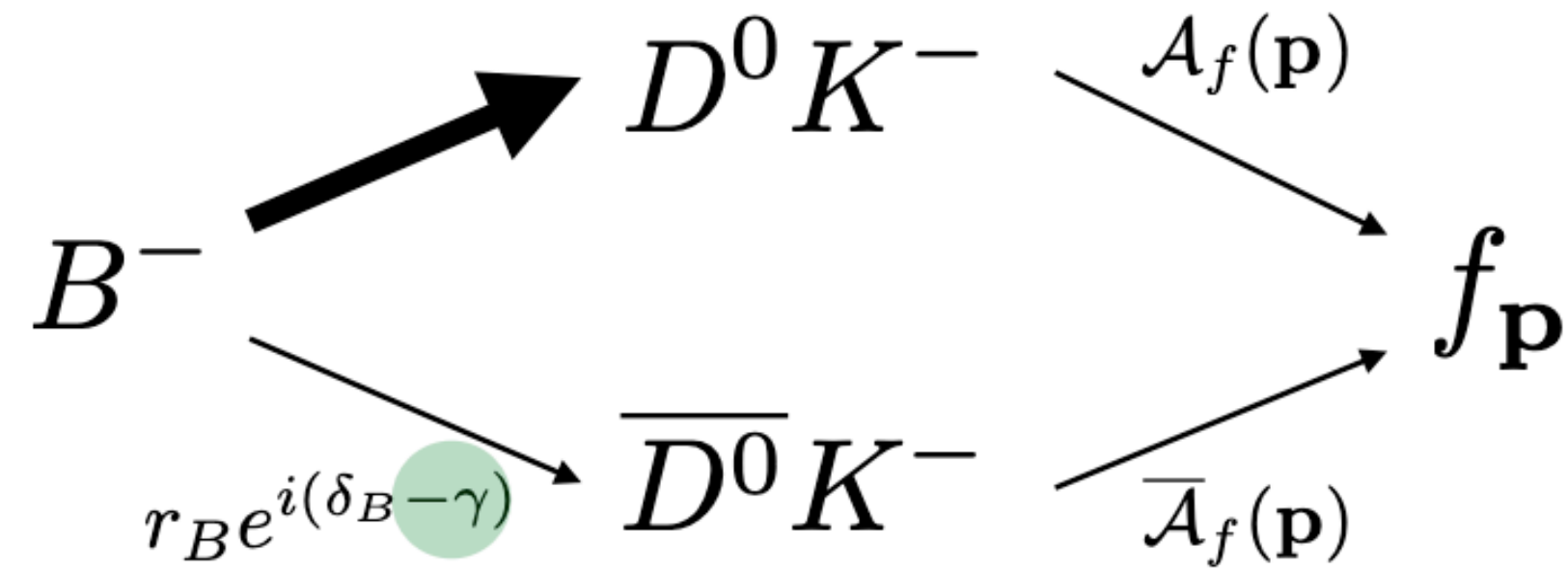


Current W.A.: [HFLAV]

- $\phi_3 = (66.2_{-3.6}^{+3.4})^\circ$
- $r_B(DK^-) = (0.0994 \pm 0.0026)$
- $\delta_B(DK^-) = (127.7_{-3.9}^{+3.6})^\circ$
- $r_B(D\pi^-) = (0.0049 \pm 0.0006)$
- $\delta_B(D\pi^-) = (294_{-11}^{+9.7})^\circ$

- Also need measure r_B, δ_B at same time.
- Need consider the D decays, e.g. strong-phase difference.
 - CLEO-c and BESIII provides model-independent external inputs.
- Depends on the D decay final states, different methods:
 - **BPGGSZ**: self conjugated multi-body decays, e.g. $K_S^0 \pi^+ \pi^-, K_S^0 \pi^+ \pi^- \pi^0, \pi^+ \pi^- \pi^+ \pi^-$
 - **GLW**: CP eigenstates, e.g. $K_S^0 \pi^0, K^+ K^-$
 - **ADS**: CF and DCS decays, e.g. $K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^\pm \pi^\mp$
 - **GLS**: SCS decays, e.g. $K_S^0 K^\mp \pi^\pm$

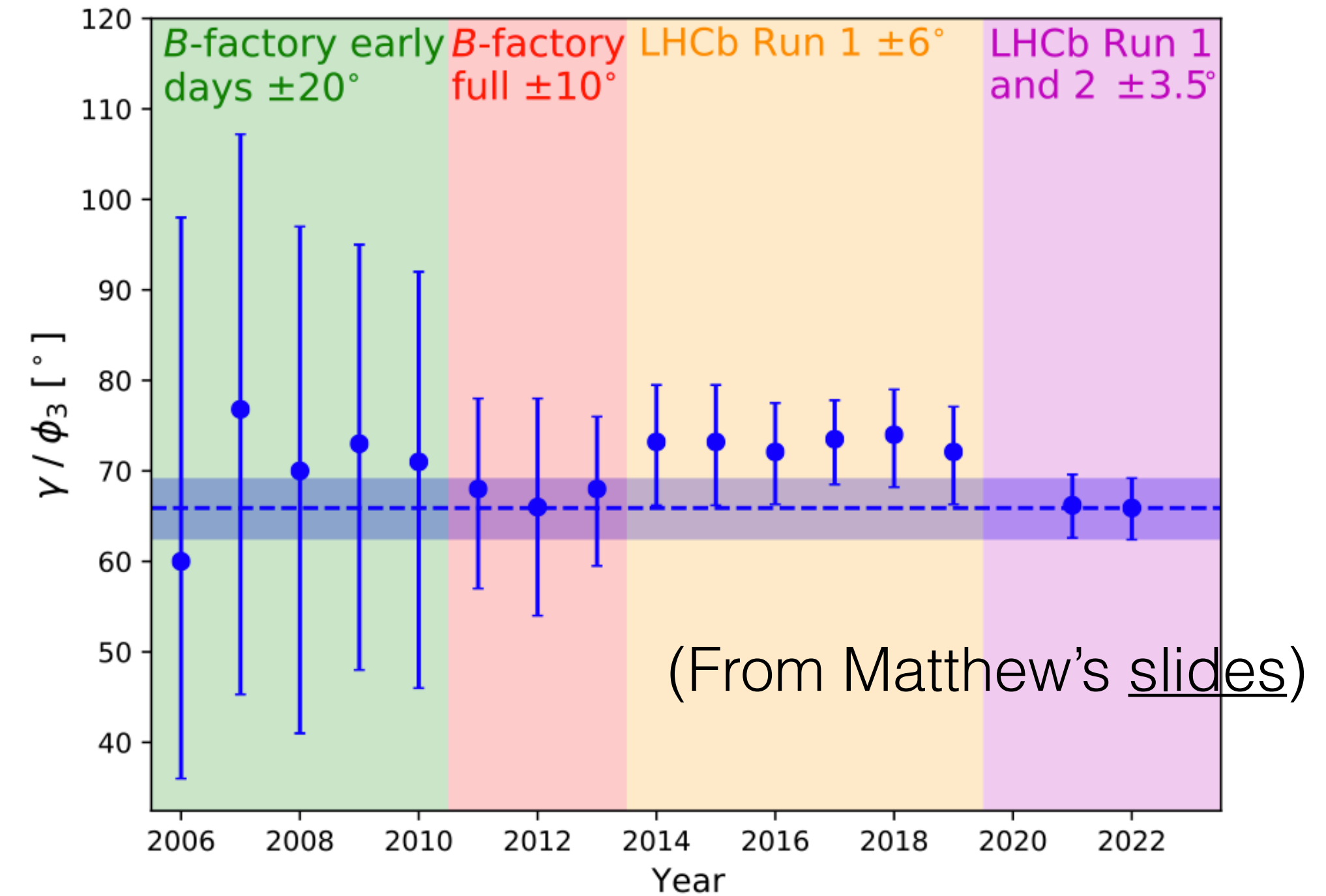
About ϕ_3



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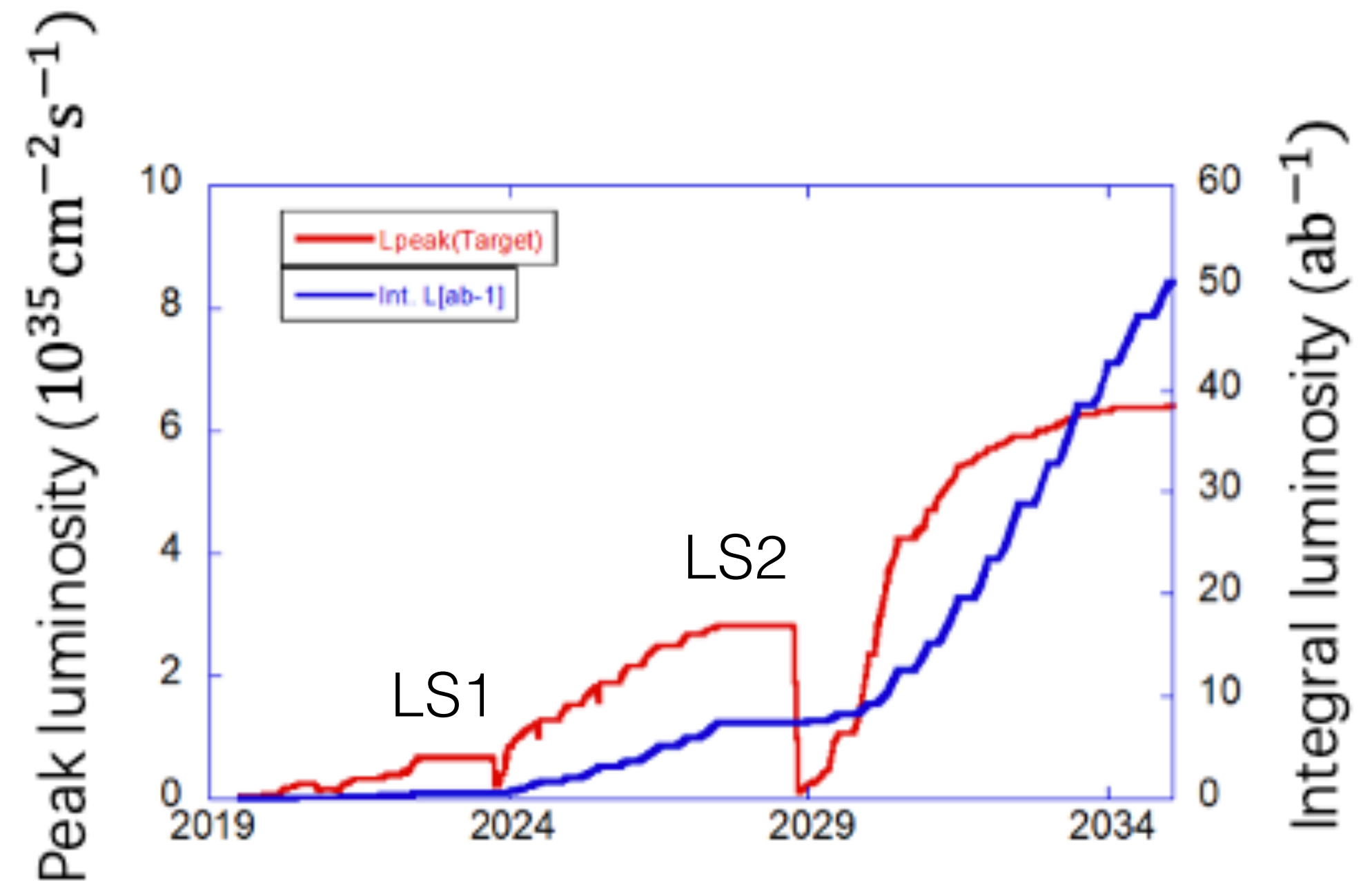
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- Now the w.a. of ϕ_3 is dominated by LHCb.

About ϕ_3

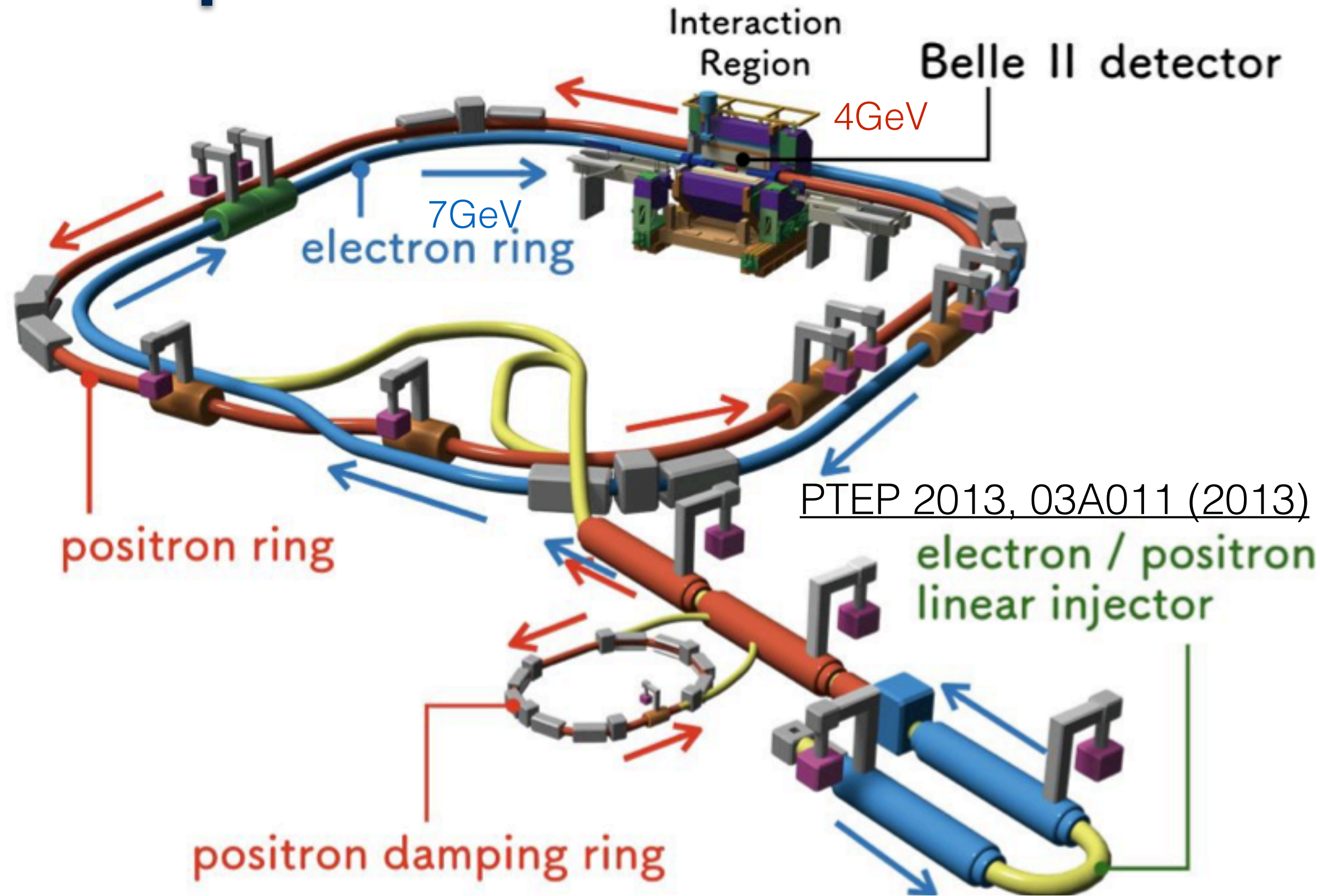
- Theoretically clean, non-tree SM contribute $\sim 10^{-7}$ [arXiv:1308.5663]
 - Current W.A.: $\phi_3 = (66.2_{-3.6}^{+3.4})^\circ$ [HFLAV], statistically uncertainty dominated.
 - More B data in the next decades
 - LHCb expect 1.5° by end of Run 3 ($\sim 22 \text{ fb}^{-1}$), $<1^\circ$ by end of Run 4 ($\sim 50 \text{ fb}^{-1}$), $\sim 0.4^\circ$ in Phase II upgrade ($\sim 300 \text{ fb}^{-1}$). [arXiv:1709.10308, CERN-LHCC-2017-003]
 - Belle II expect 1.5° with 50 ab^{-1} [2020 snowmass].
- > In the future, ϕ_3 can be a “**candle**” of SM.



Outline

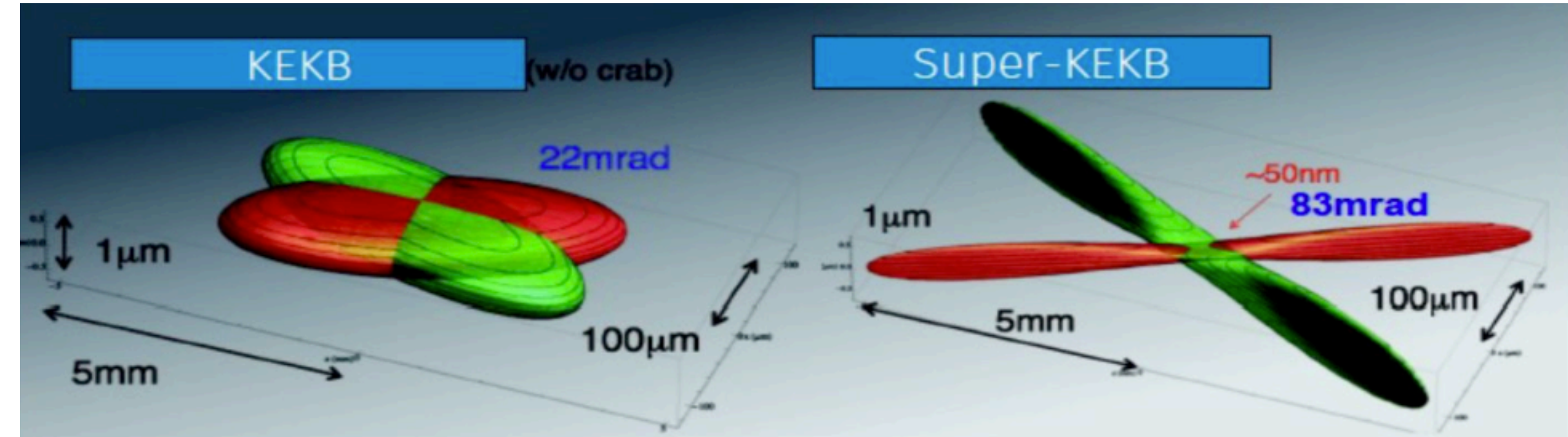
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SuperKEKB



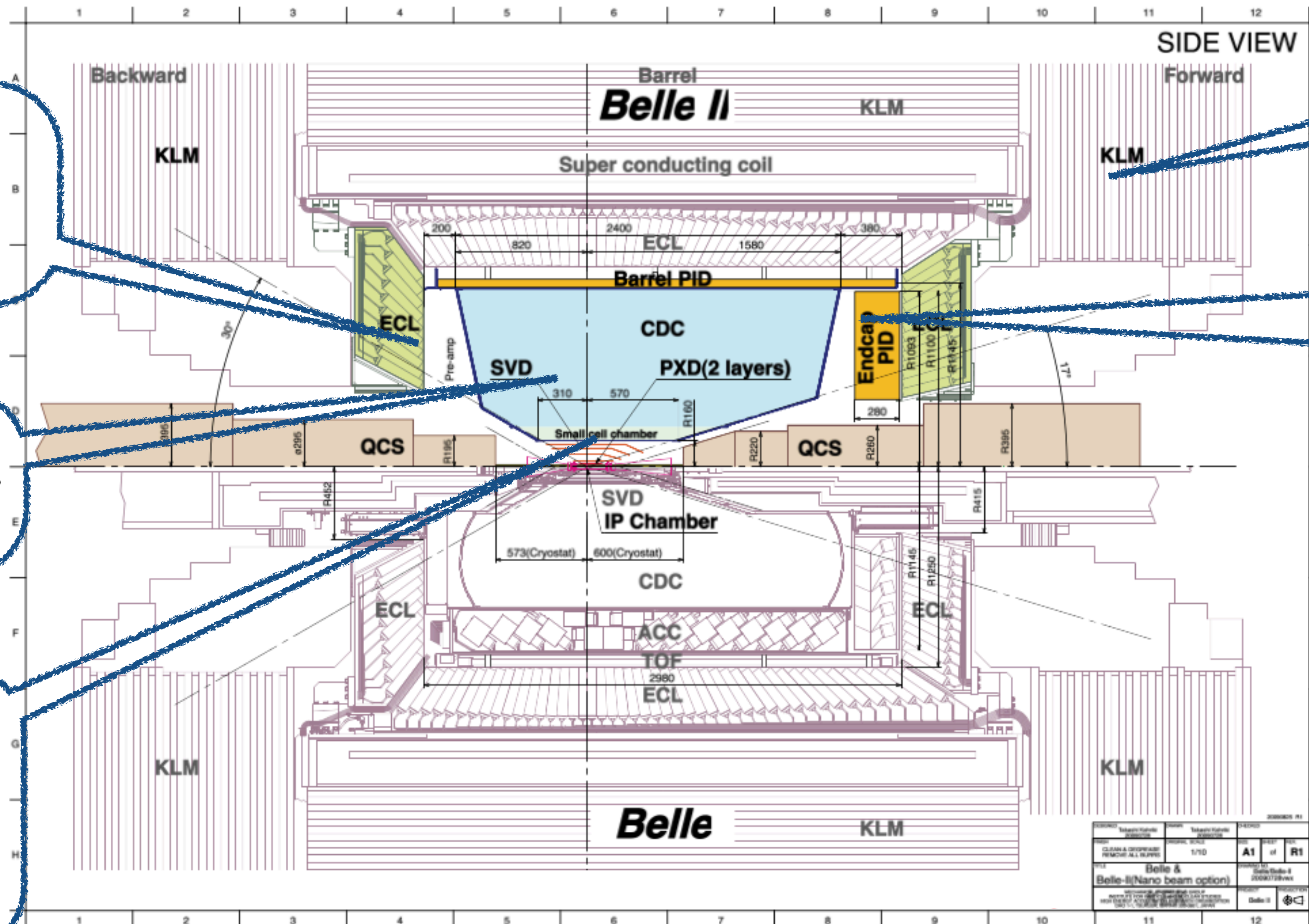
Machine parameters as of June 8th 2022, with the design values in ()

Parameter	LER	HER	unit
Beam current	1321 (3600)	1099 (2600)	mA
# of bunches		2249 (2500)	
Bunch current	0.587	0.489	mA
β_x^*/β_y^*	80/1.0 (32/0.27)	60/1.0 (25/0.30)	mm
Beam-Beam Parameter ξ_y	0.0407 (0.088)	0.0279 (0.081)	
σ_y^*	0.215 (0.048)	0.215 (0.062)	μm
tunes (x/y)	44.525/46.589	45.532/43.573	
Specific luminosity($\times 10^{31}$)		7.21	$\text{cm}^{-2}\text{s}^{-1}/\text{mA}^2$
Luminosity($\times 10^{34}$)		4.65 (60)	



- Asymmetric e^+e^- collider at KEK
- Design instant luminosity: $6.5 \times 10^{35} \text{cm}^{-2}\text{s}^{-1}$
- Nano-beam collision, crab waist scheme
- Instant luminosity record of $4.7 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$ (x2 of KEKB's peak luminosity)

Belle and Belle II detector



ECL
 CsI(Tl)+waveform sampling
 Energy resolution: 1.6~4%

CDC
 Track efficiency: ~99%
 dE/dx resolution: 5%
 Pt resolution: 0.4%

VXD
 Inner 2 layers: pixel detector (PXD)
 Outer 4 layers: strip sensor (SVD)
 Vertex resolution: 15 μm

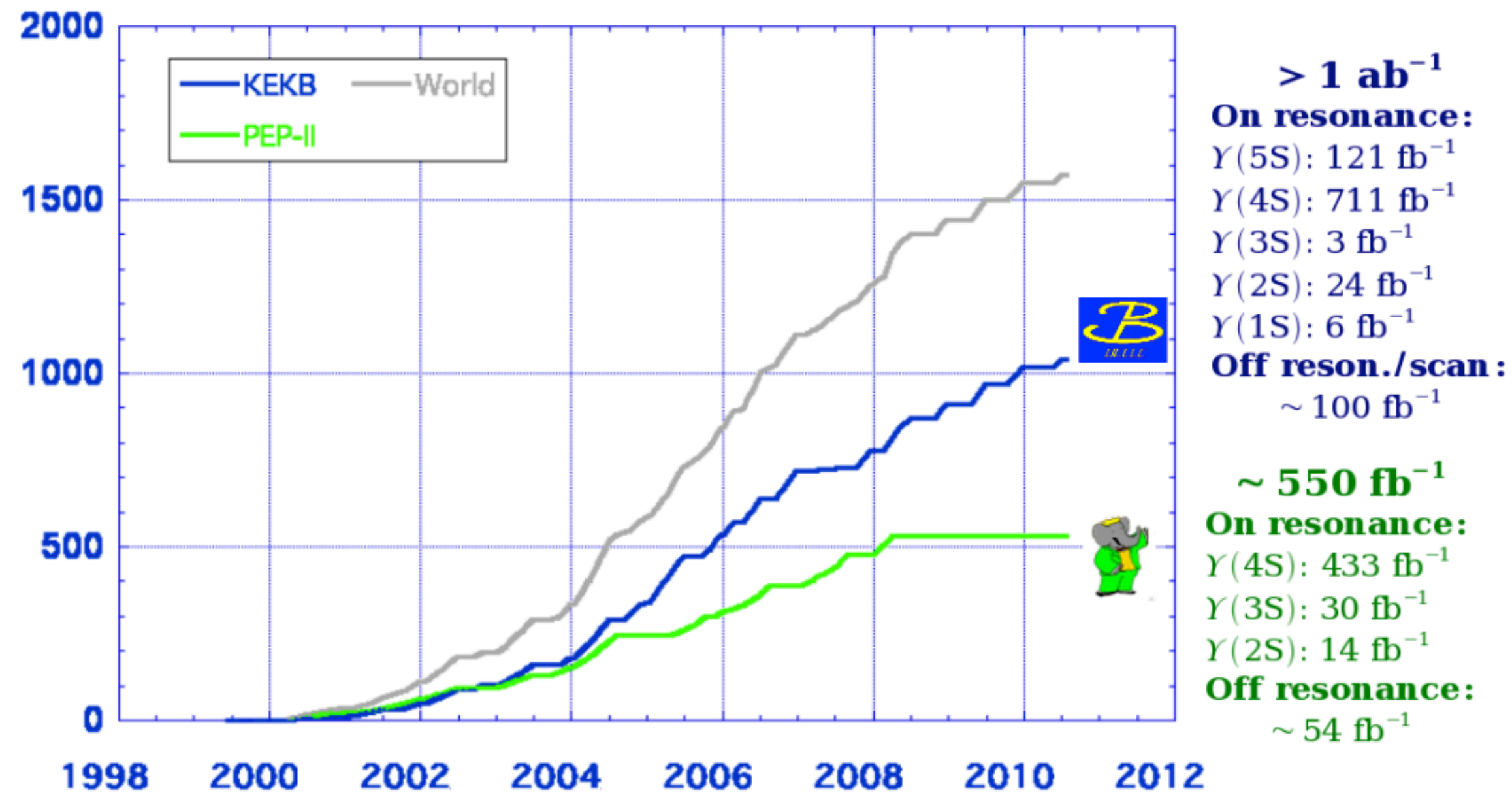
KLM
 Outer barrel: Resistive Plate Counter (RPC)
 Endcap/inner barrel: Scintillator

PID
 Barrel: Time-Of-Propagation counters(TOP)
 Endcap: ARICH

- Not just Belle “too”.
- A brand new detector.
- Only re-use magnet, calorimeter crystals.

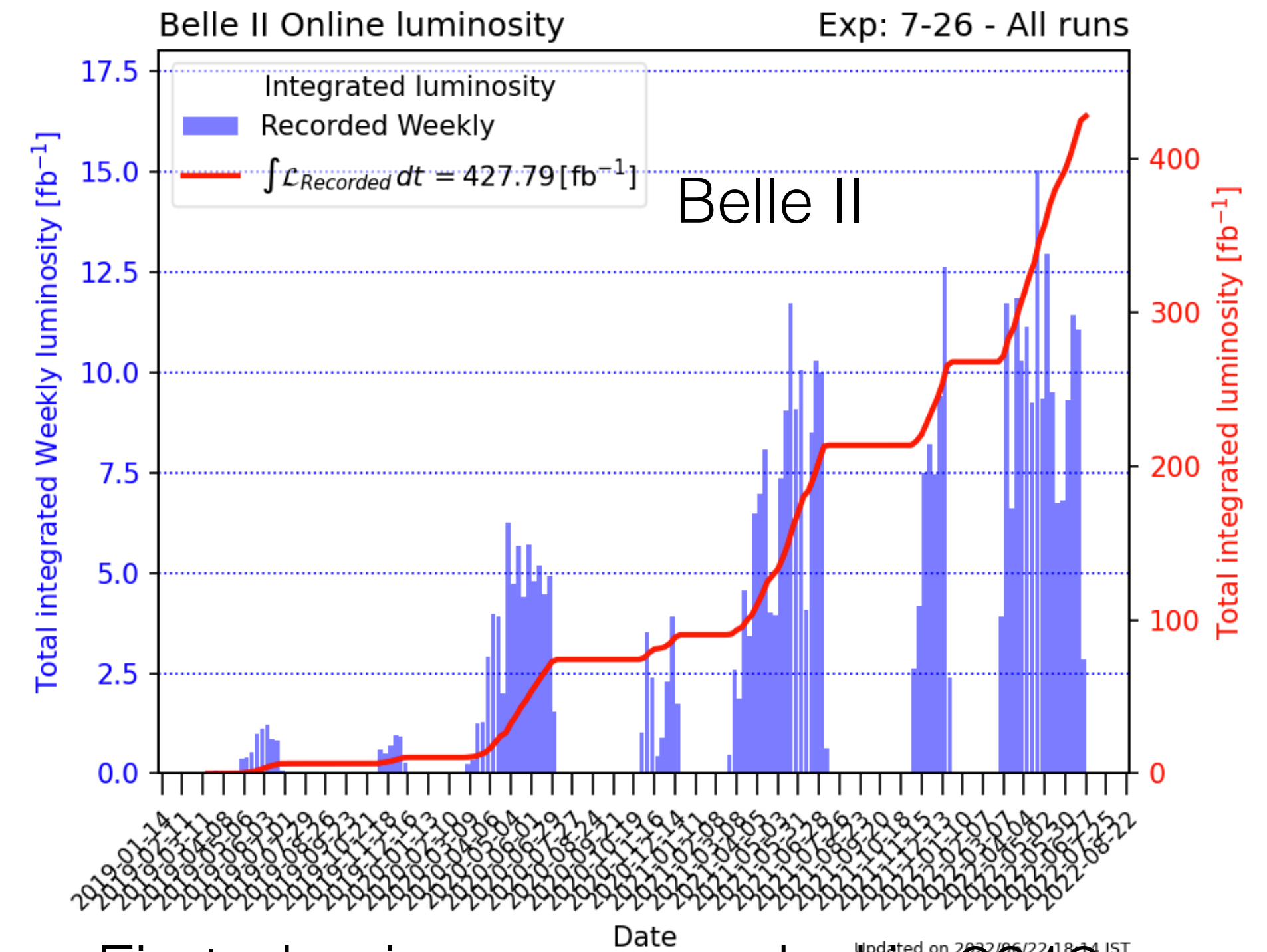
REVISION	DESCRIPTION	DATE	BY	CHK
1	INITIAL DESIGN	1/10	A1	R1
Belle & Belle-II(Nano beam option)				
DATE: 2008/01/10				
DRAWN BY: [unintelligible]				
CHECKED BY: [unintelligible]				
DATE: [unintelligible]				

Belle and Belle II data sets



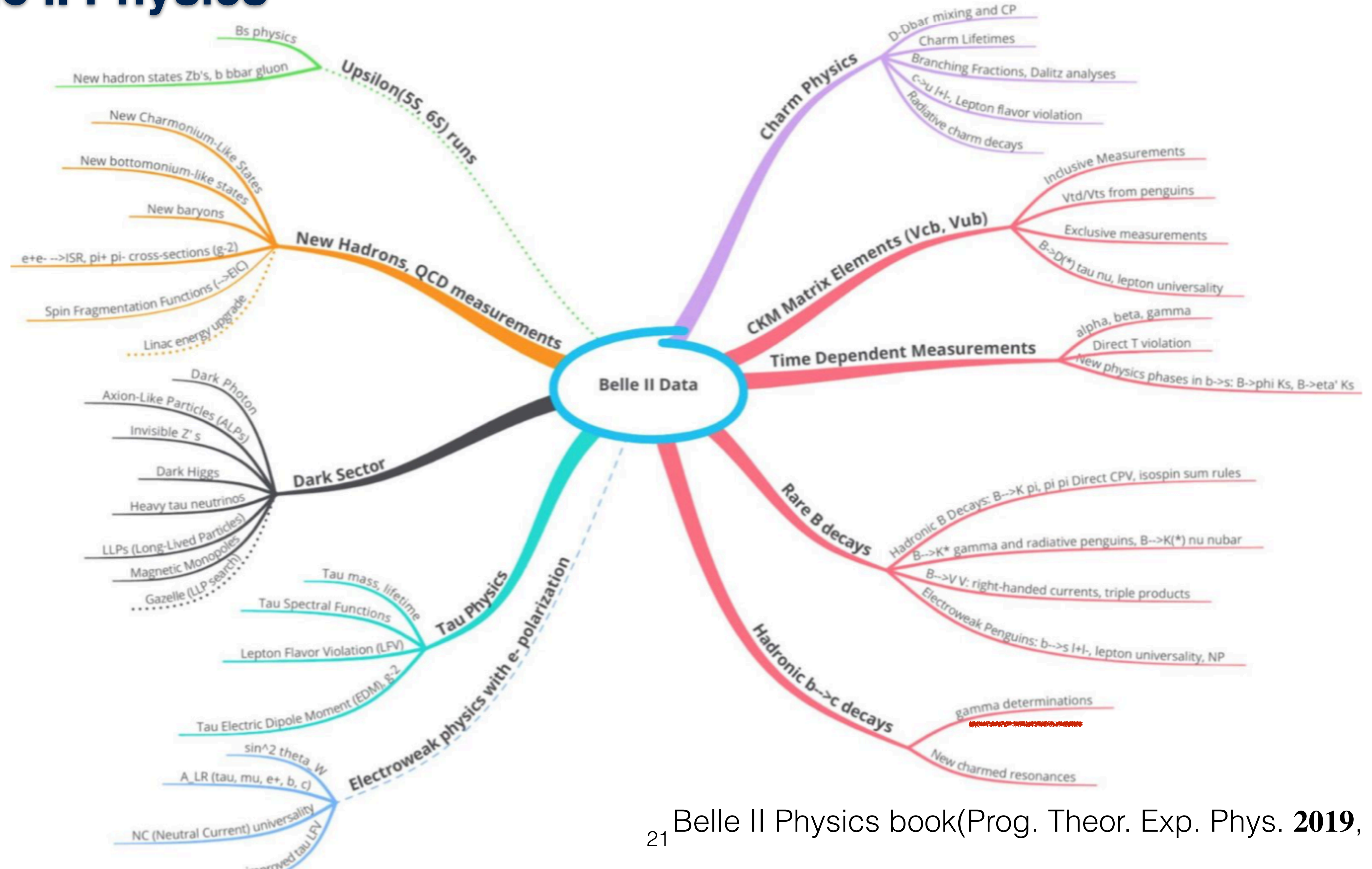
711 fb⁻¹ @ $\Upsilon(4S)$ from Belle

Total recorded integrated luminosity before Long Shutdown 1



- First physics run recorded in 2019
 - **362**/fb at $\Upsilon(4S)$ (goal: 50/ab)
 - 42/fb off-resonance, 60 MeV below $\Upsilon(4S)$
 - 19/fb energy scan between 10.6 to 10.8 GeV for bottomonium and exotic spectroscopy study.

Belle II Physics



Belle II Collaboration



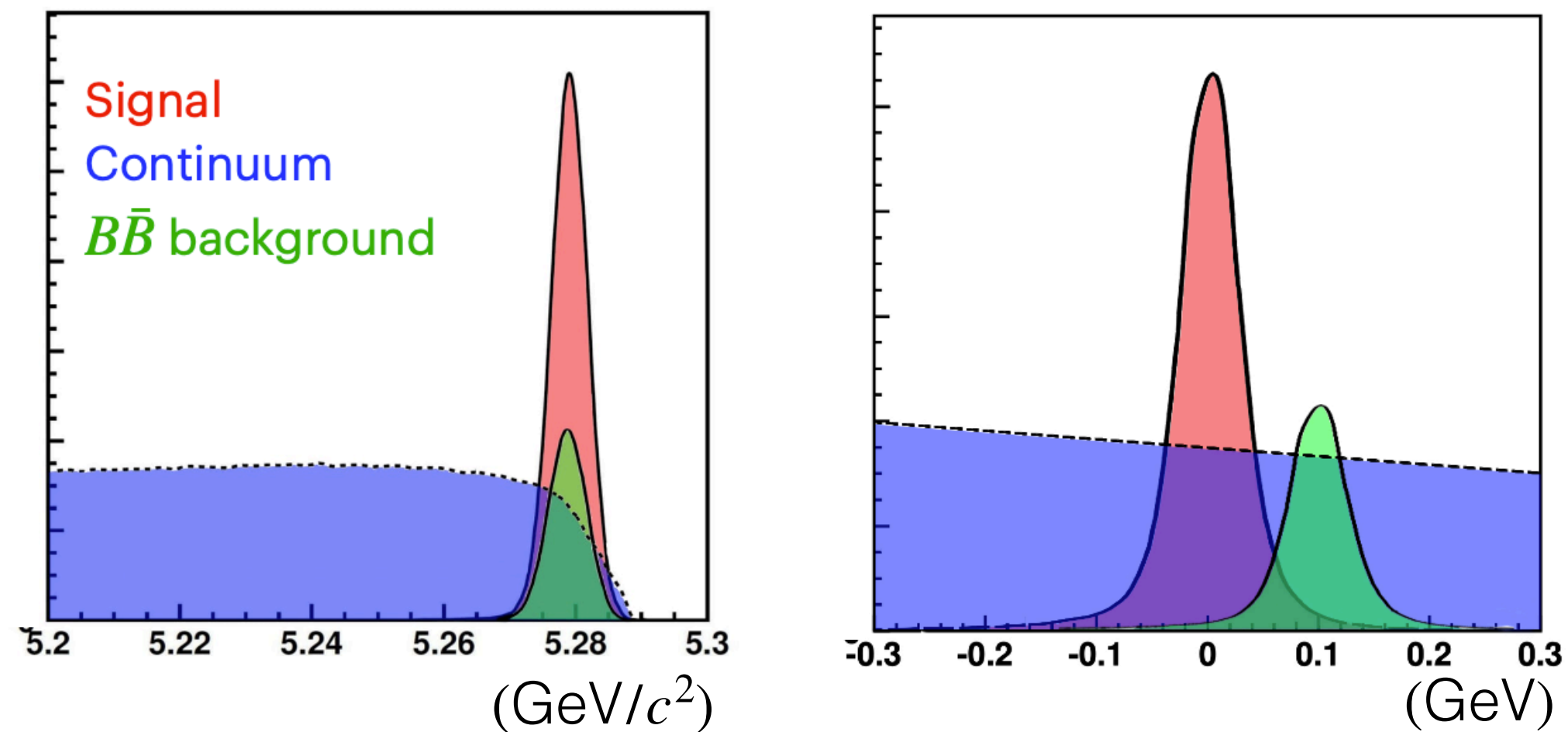
- 26 countries and regions, 123 institutions, ~1100 collaborators

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Similar analysis flow

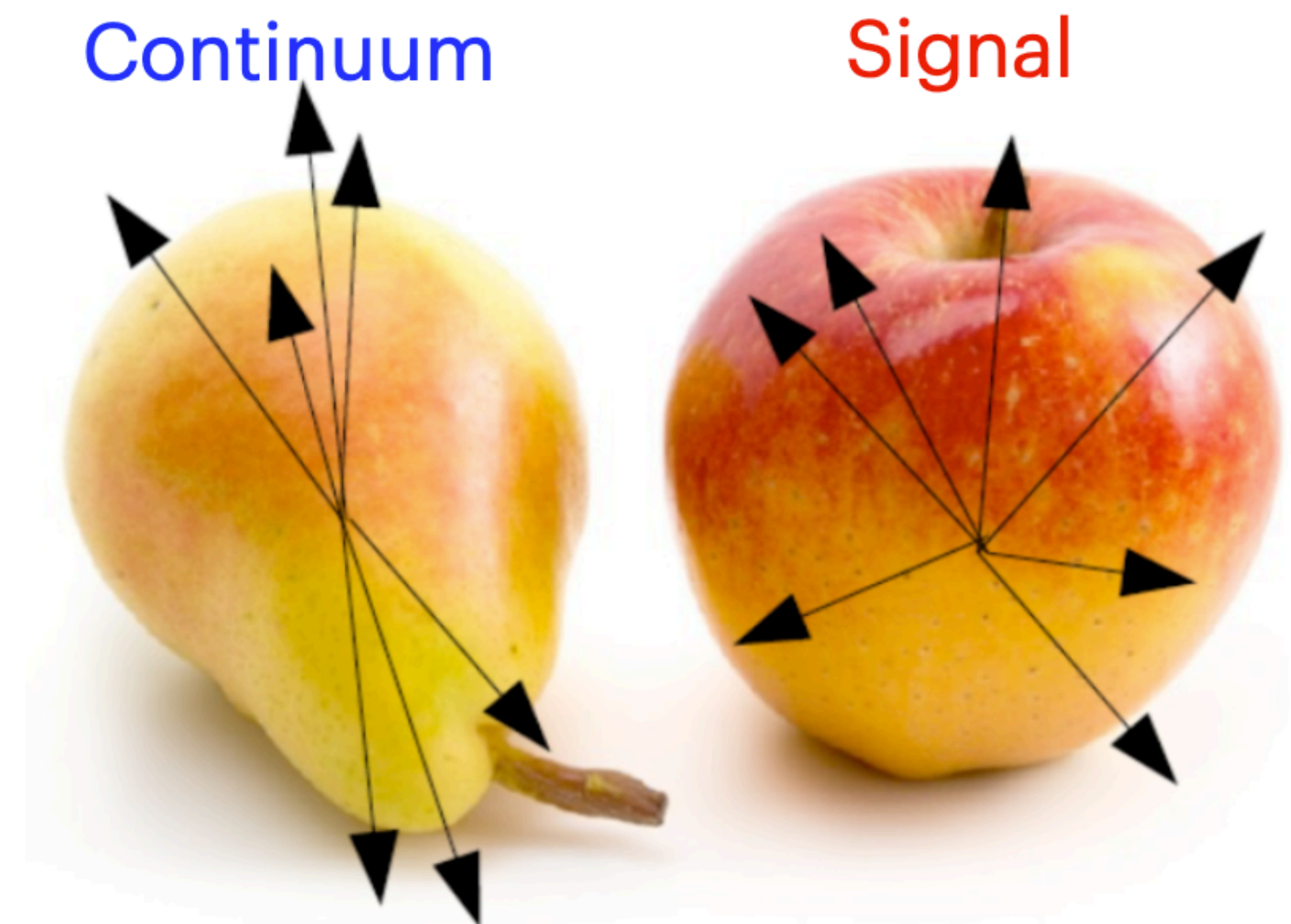
- e^+e^- collide at $\Upsilon(4S)$, just above $B\bar{B}$ threshold: low background and well-known knowledge of initial state



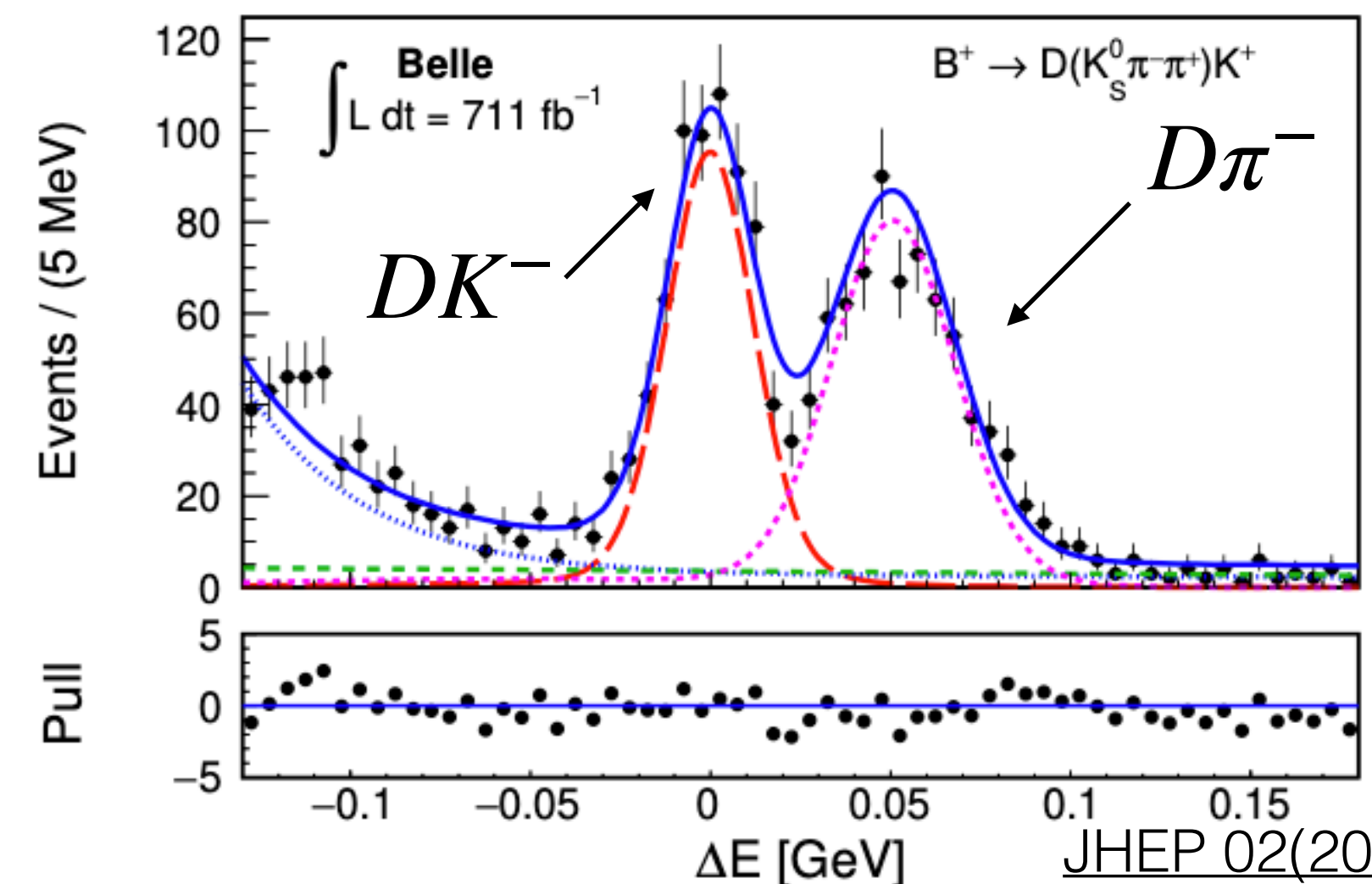
$$M_{bc} = \sqrt{s/4 - p_B^{*2}}$$

$$\Delta E = E_B^* - \sqrt{s}/2$$

- Use event shape to identify continuum background.



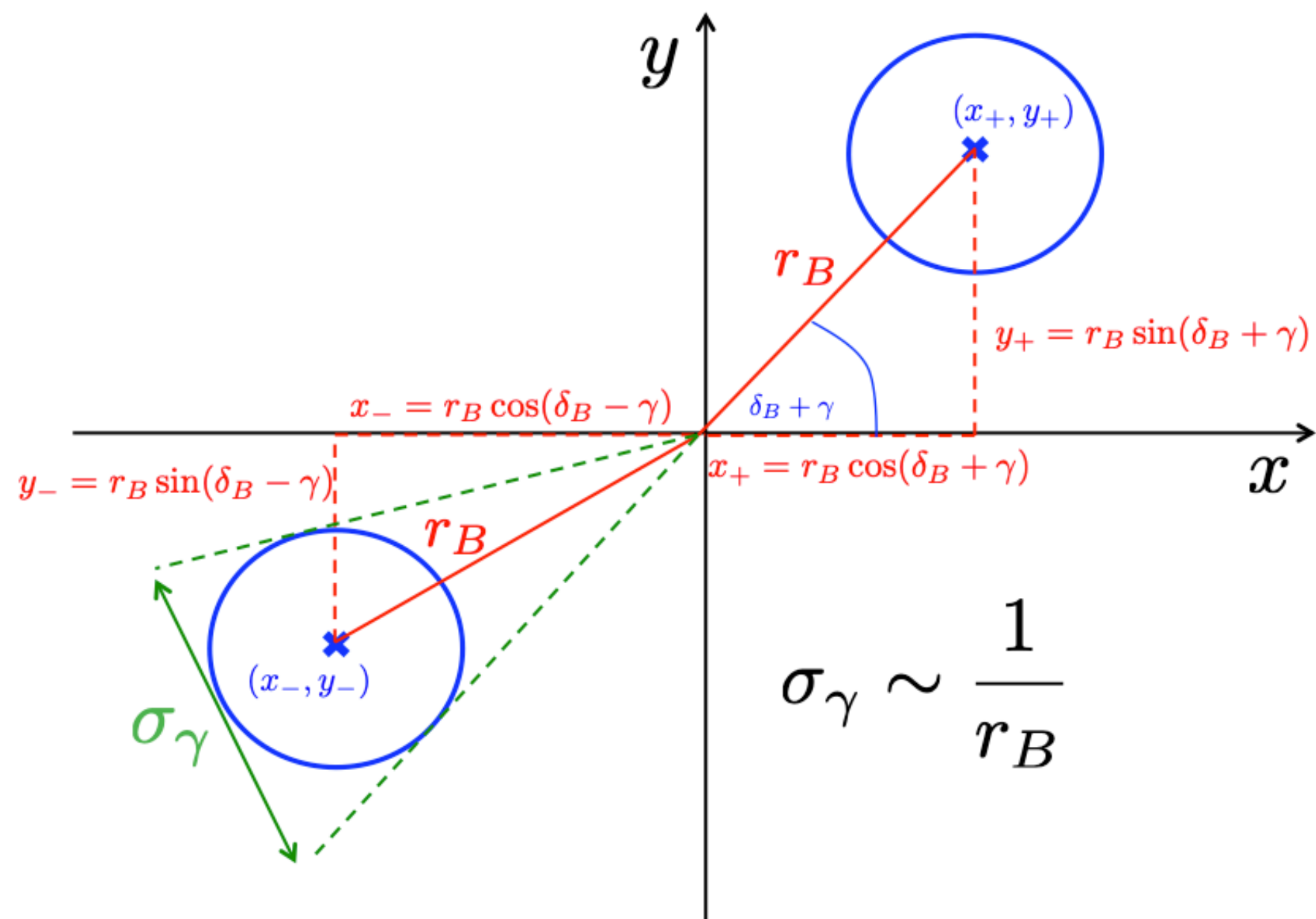
Extract signal on ΔE and BDT output.



BPGGSZ method (golden channel)

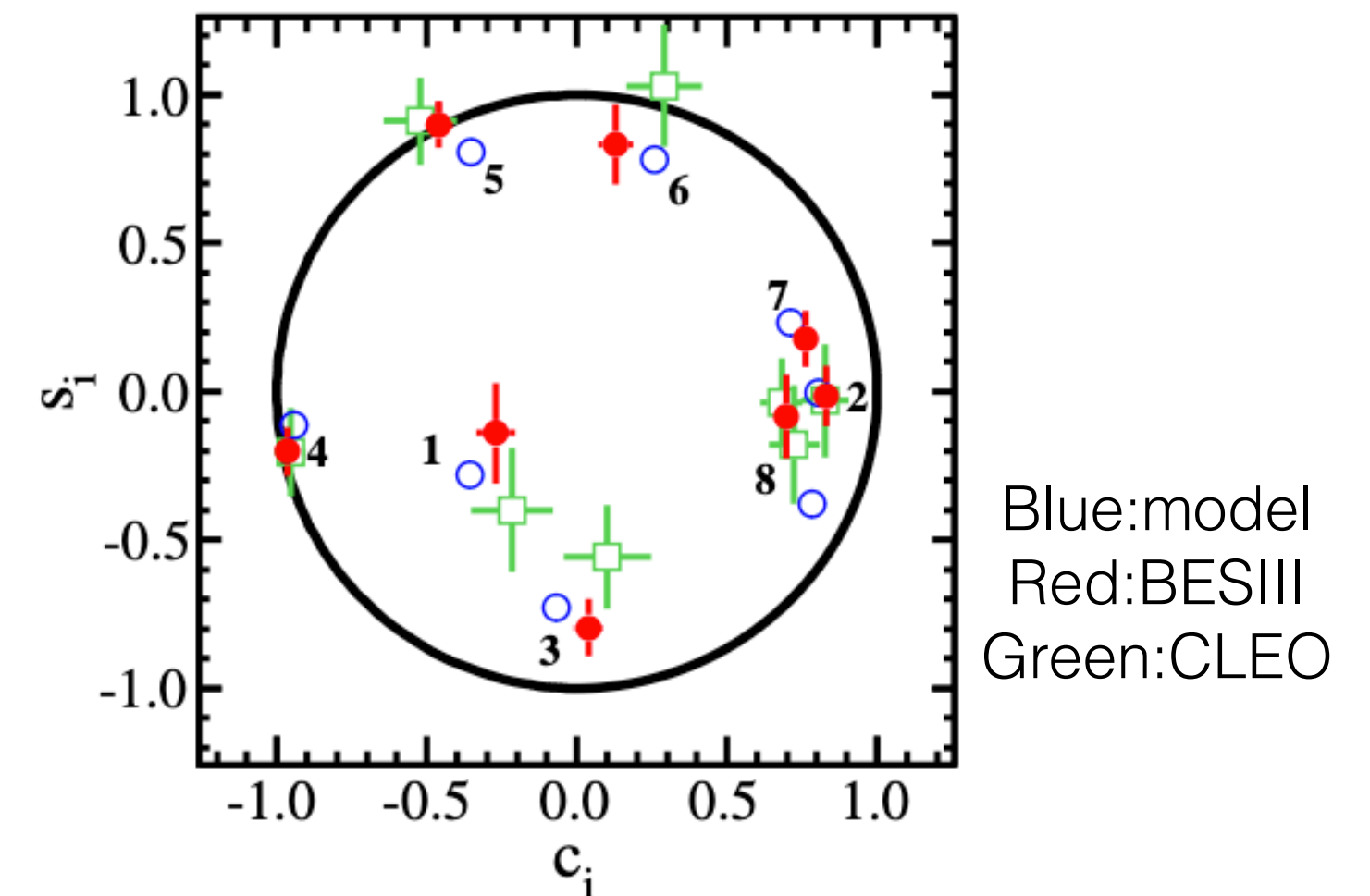
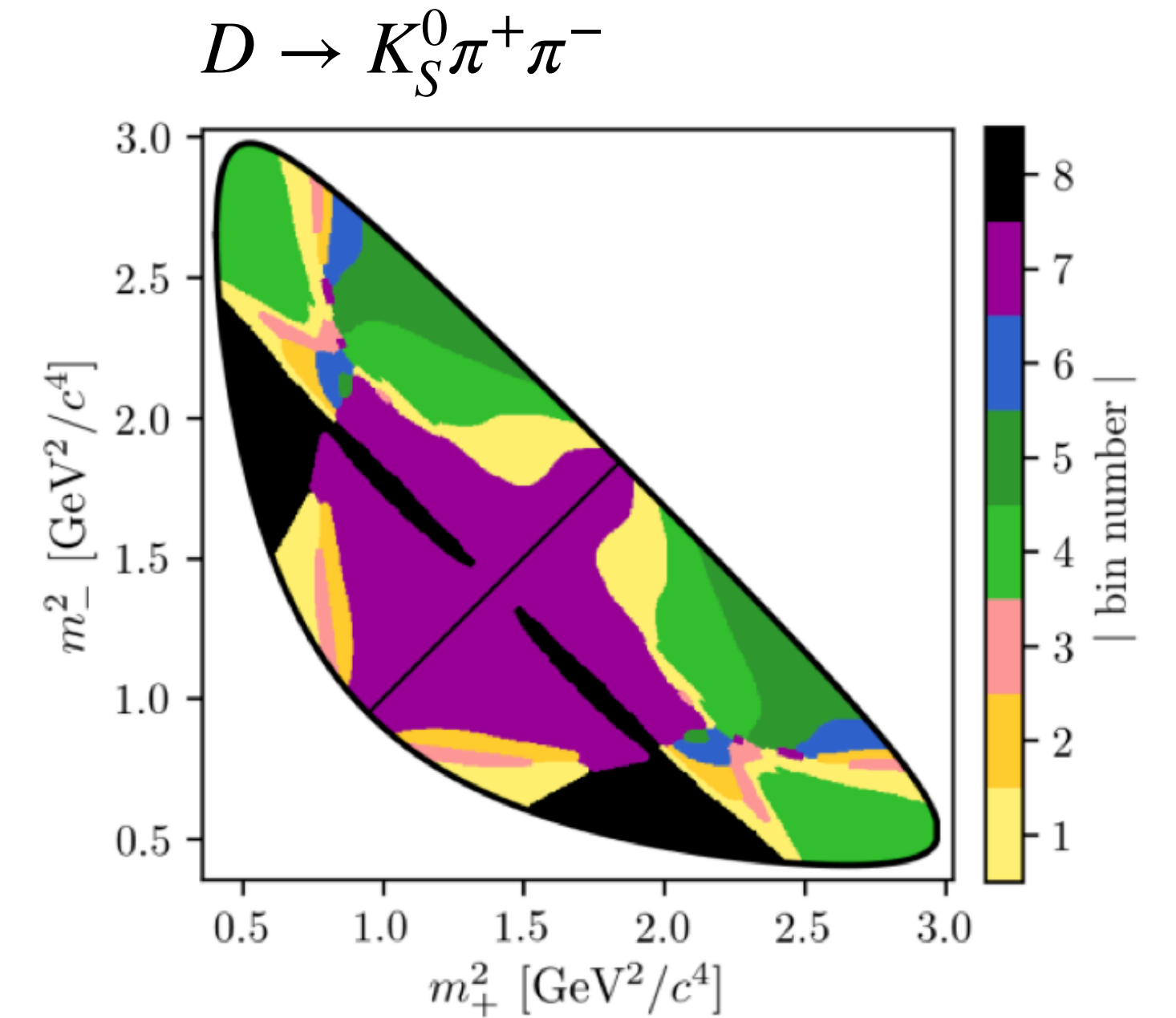
- D decays to self conjugated multi-body final states.
- Binned way to gain more sensitivity from interference between various partial waves in local region(bin).
- D information, $|A|_i, c_i, s_i$, are measured by CLEO-c and BESIII.

$$d\Gamma_{B\pm}(\mathbf{x}) = A_{(\pm,\mp)}^2 + r_B^2 A_{(\mp,\pm)}^2 + 2A_{(\pm,\mp)}A_{(\mp,\pm)} \left[\underbrace{r_B \cos(\delta_B \pm \gamma)}_{x_{\pm}} \underbrace{\cos(\delta_{D(\pm,\mp)})}_{c_i} + \underbrace{r_B \sin(\delta_B \pm \gamma)}_{y_{\pm}} \underbrace{\sin(\delta_{D(\pm,\mp)})}_{s_i} \right]$$

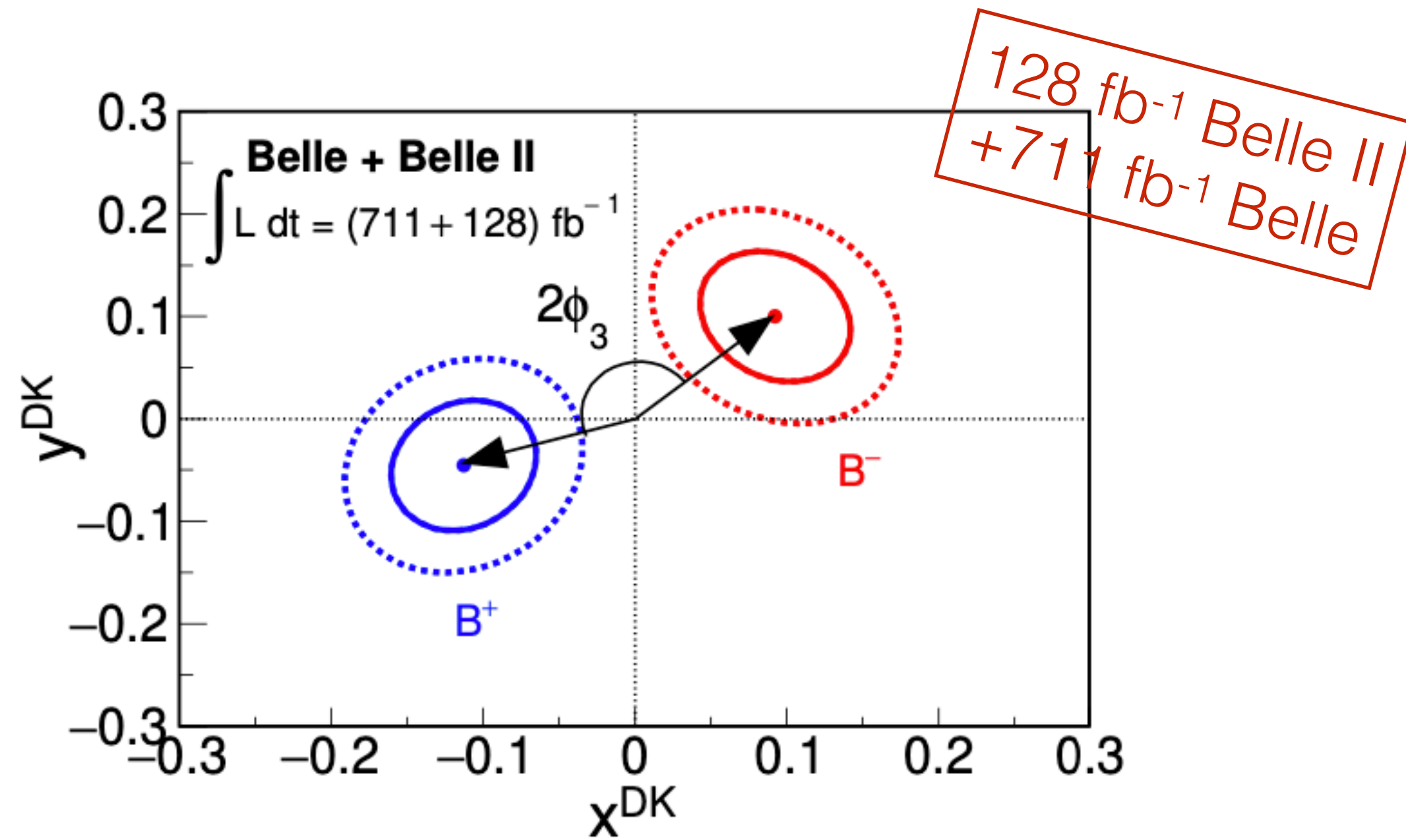


$$\sigma_{\gamma} \sim \frac{1}{r_B}$$

- ϕ_3 's precision highly depends on the r_B 's value!
- Large r_B -> large interference in B->DK-> more sensitive to ϕ_3 .



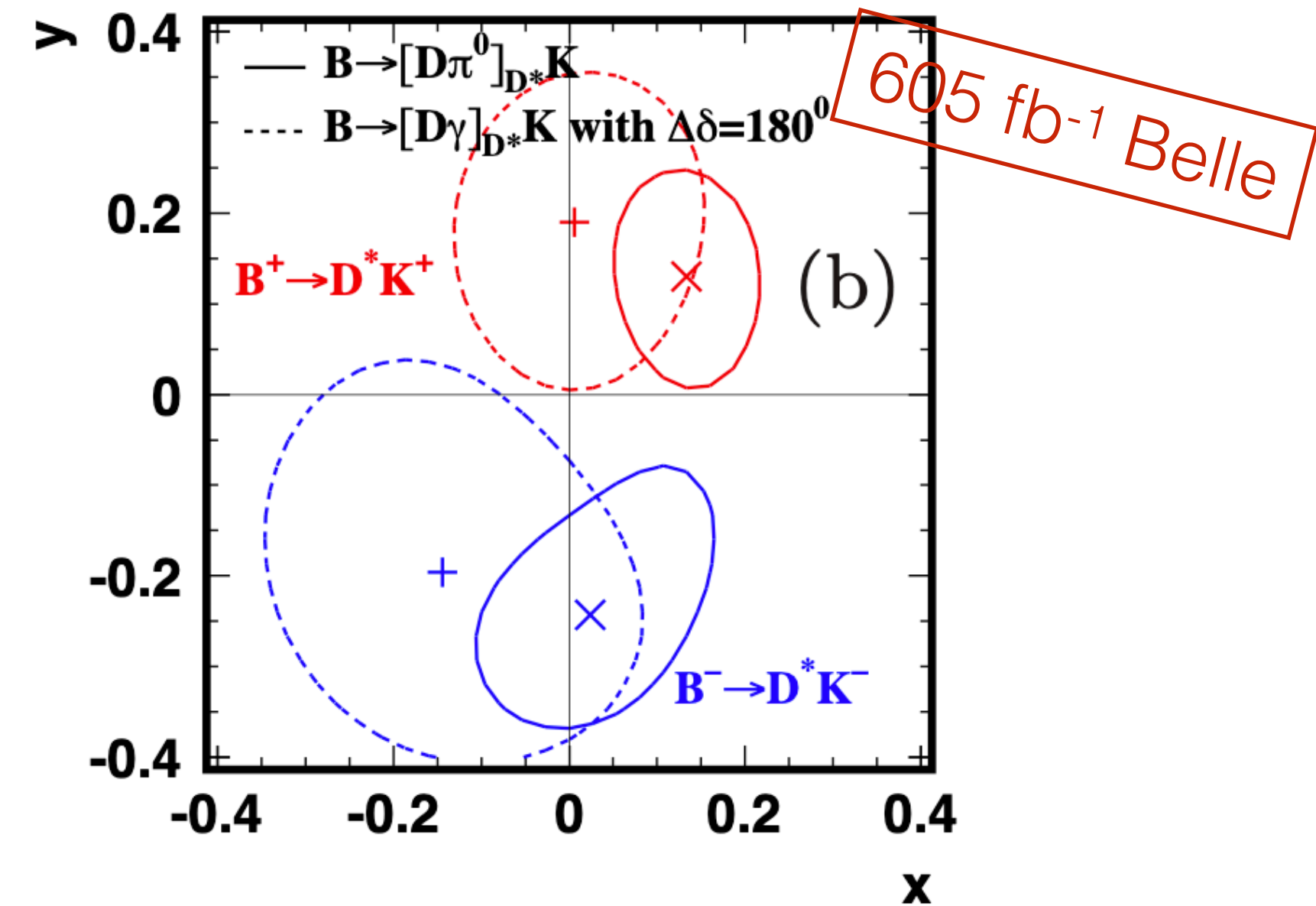
BPGGSZ results from Belle and Belle II



$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 h^+ h^-$
JHEP 02(2022)063

$(78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ$
 Stat Syst ci/si

LHCb got $(68.7^{+5.2}_{-5.1})^\circ$
JHEP 02(2021)169



$B^+ \rightarrow D^* h^+, D \rightarrow K_S^0 \pi^+ \pi^-$
Phys. Rev. D 81 (2010) 112002

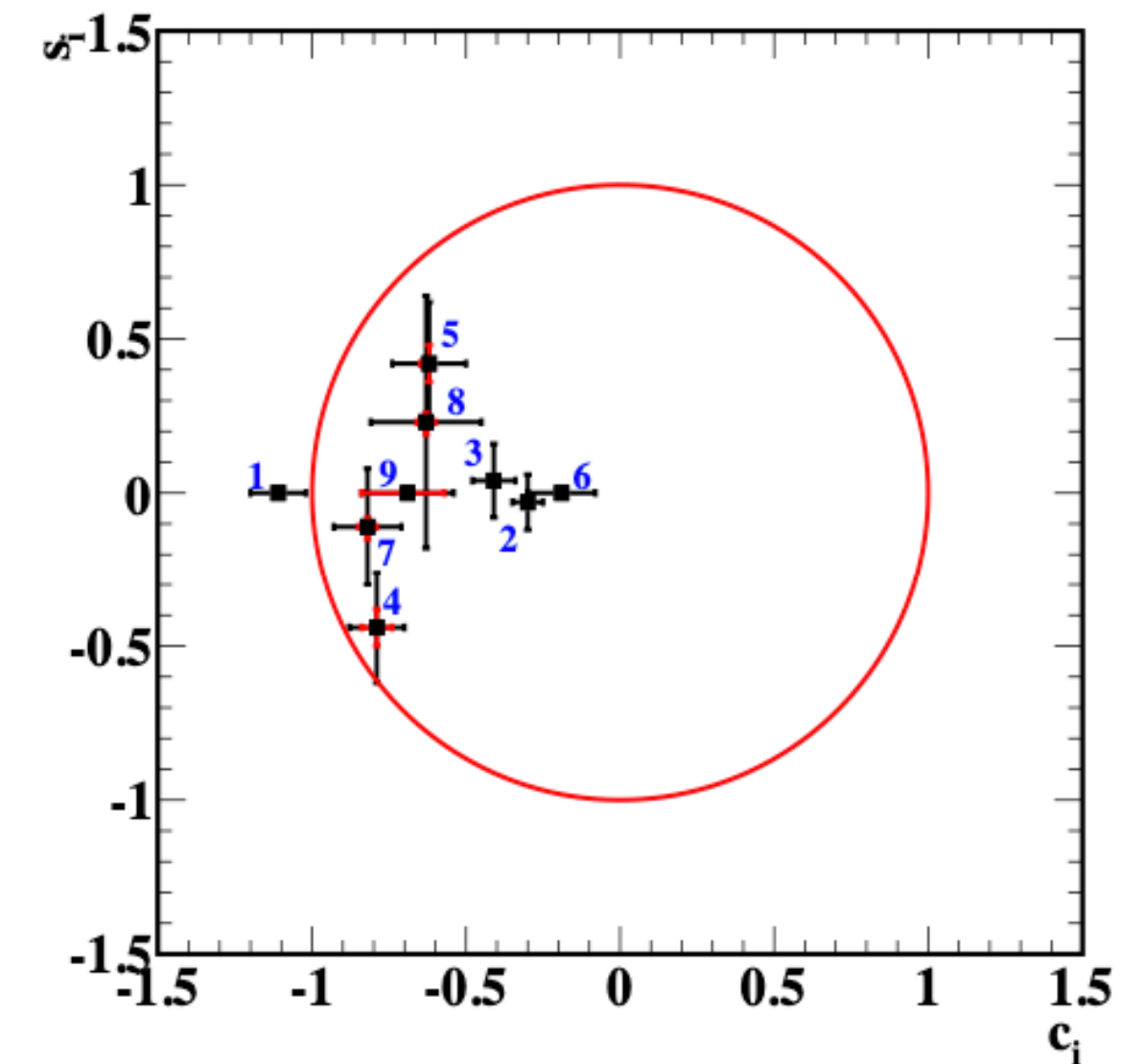
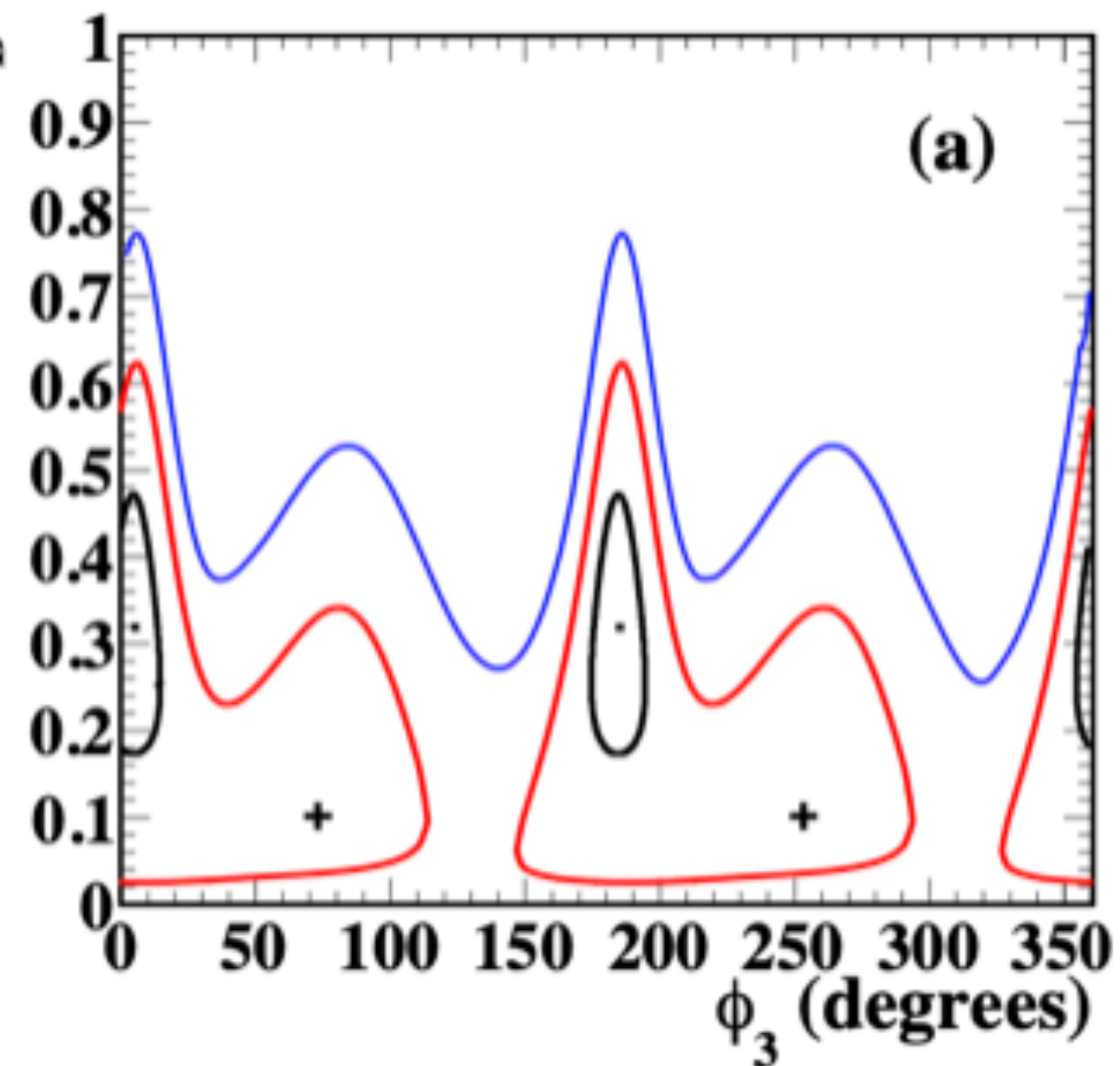
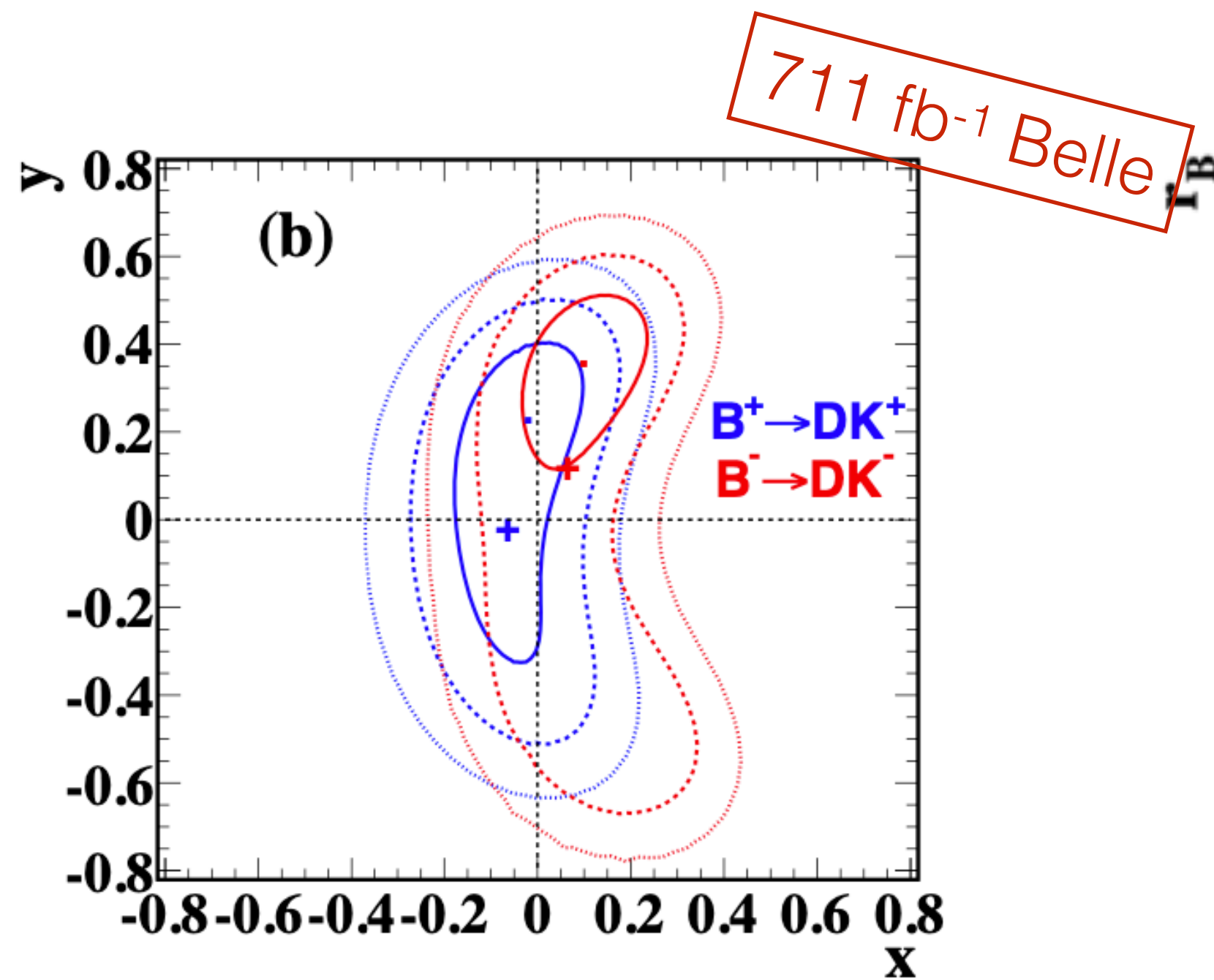
$(73.9^{+18.9}_{-20.2} \pm 4.2 \pm 8.9)^\circ$

LHCb got $(69 \pm 14)^\circ$
Preliminary on LP 2023

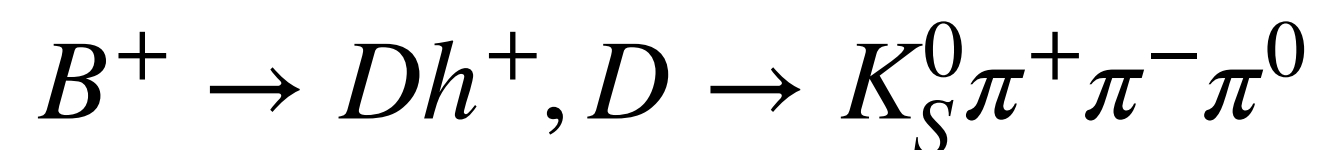
BPGGSZ results from Belle and Belle II

$$N_i^\pm = h_B [K_{\pm i} + r_B^2 K_{\mp i} + \sqrt{K_i K_{-i}} (x_\pm c_i \pm y_\pm s_i)], \quad x_\pm = r_B \cos(\delta_B \pm \phi_3)$$

$$y_\pm = r_B \sin(\delta_B \pm \phi_3)$$



CLEO-c JHEP 01 (2018) 082



JHEP 10(2019)178

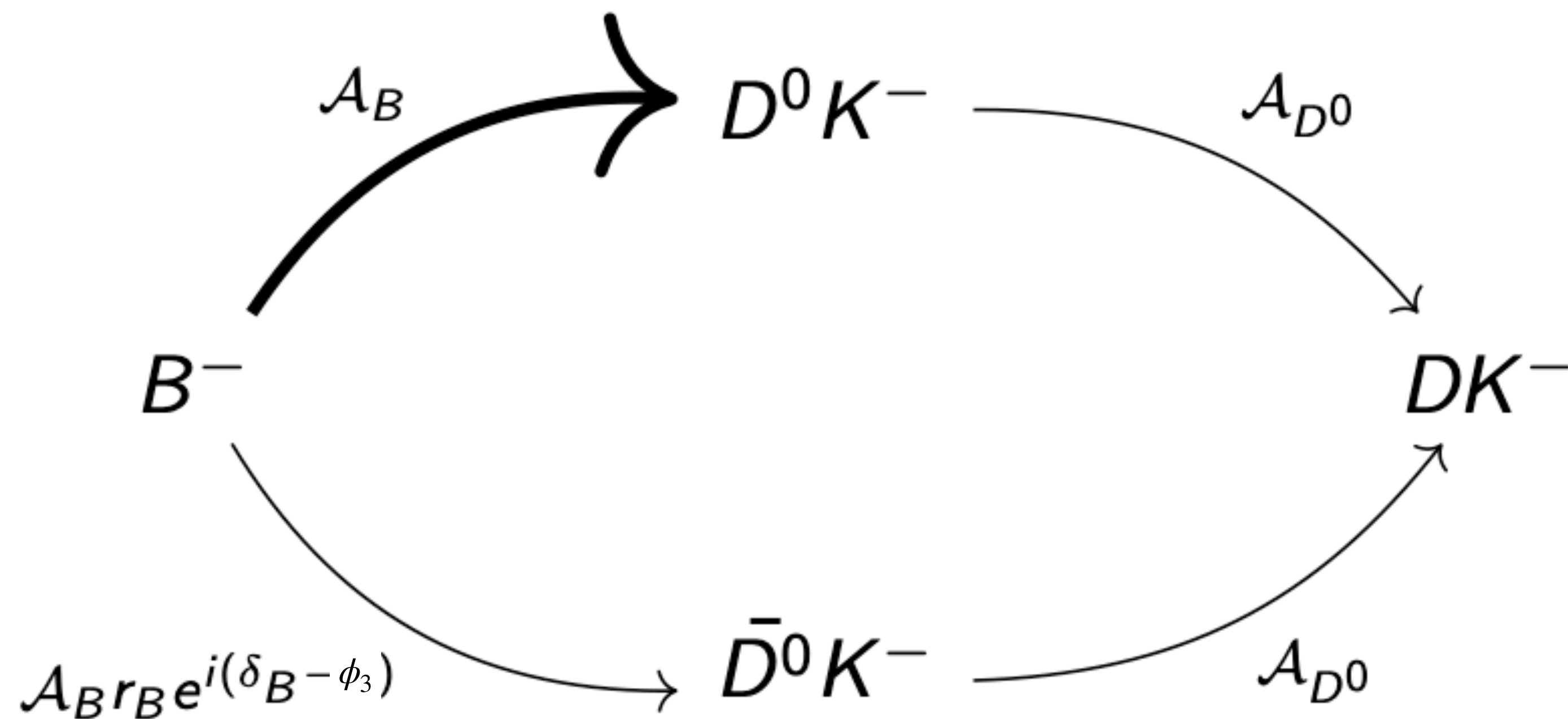
$$(5.7_{-8.8}^{+10.2} \pm 3.5 \pm 5.7)^\circ$$

Binning scheme of $D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$ is **not** optimized for ϕ_3 .

Less sensitive. Some s_i are 0, so large uncertainty of y .

Looking for the optimized scheme and c_i/s_i from BESIII!

GLW methods



- D decays to CP eigenstates, e.g. K^+K^- (CP+) $K_S^0\pi^0$ (CP-).
- Size of CPV $\sim r_B$ (10%).

- Observables:

$$R_{CP\pm} = \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm}K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}K^+)}{\mathcal{B}(B^- \rightarrow D^0K^-) + \mathcal{B}(B^+ \rightarrow \bar{D}^0K^+)},$$

$$= 1 + r_B^2 + 2\eta_{CP} r_B \cos(\delta_B) \cos(\phi_3),$$

$$A_{CP\pm} = \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm}K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm}K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm}K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}K^+)},$$

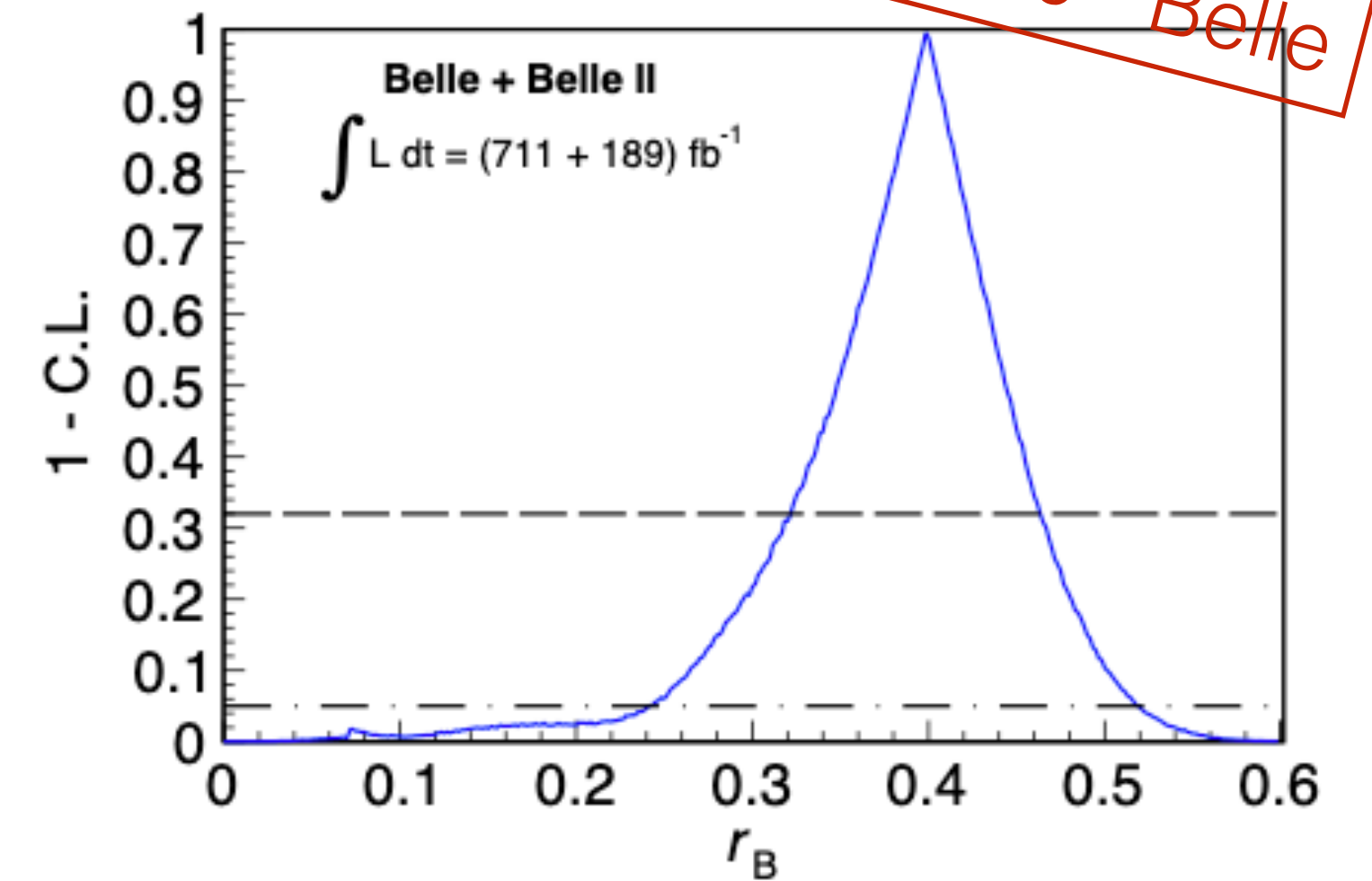
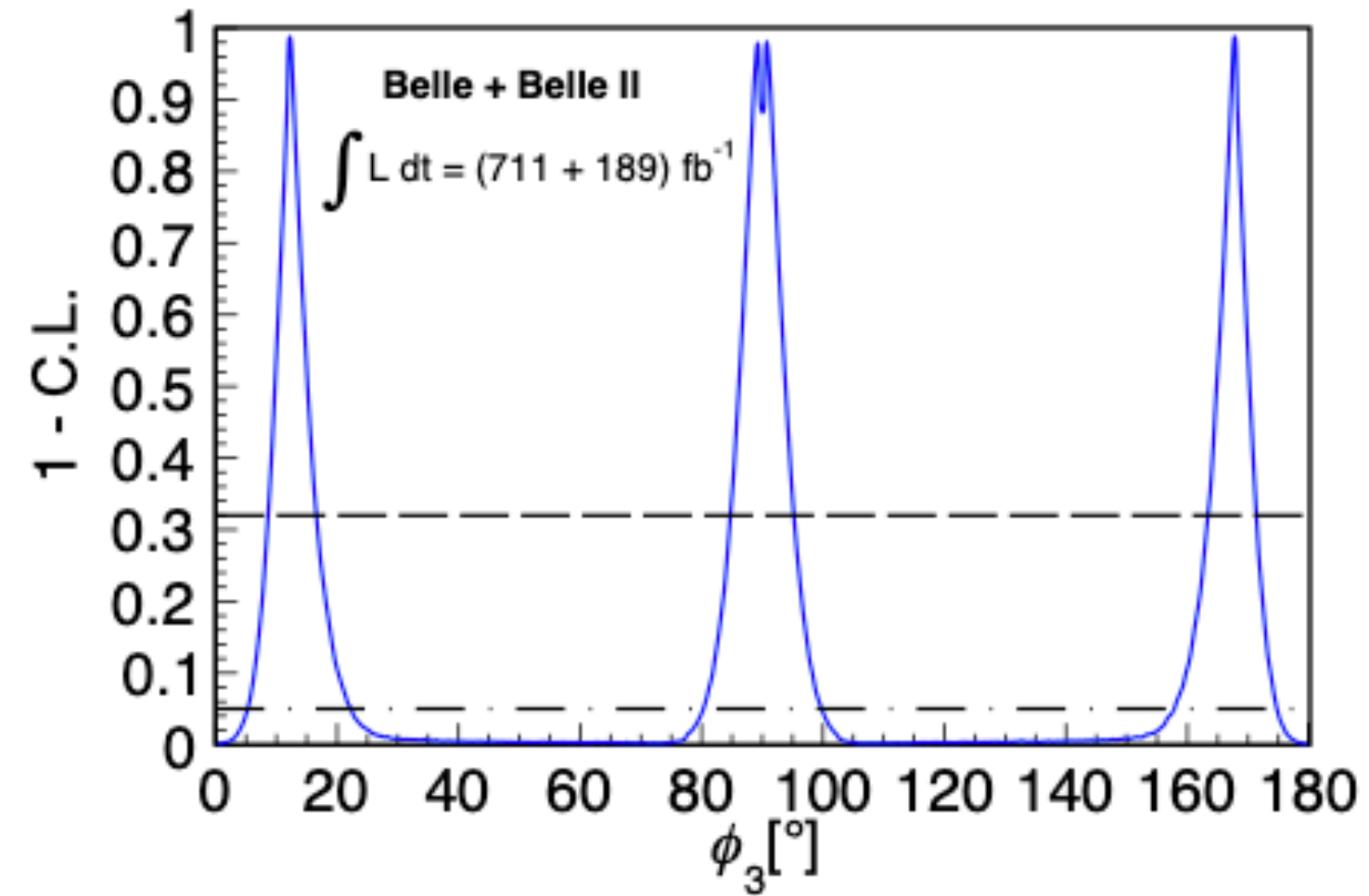
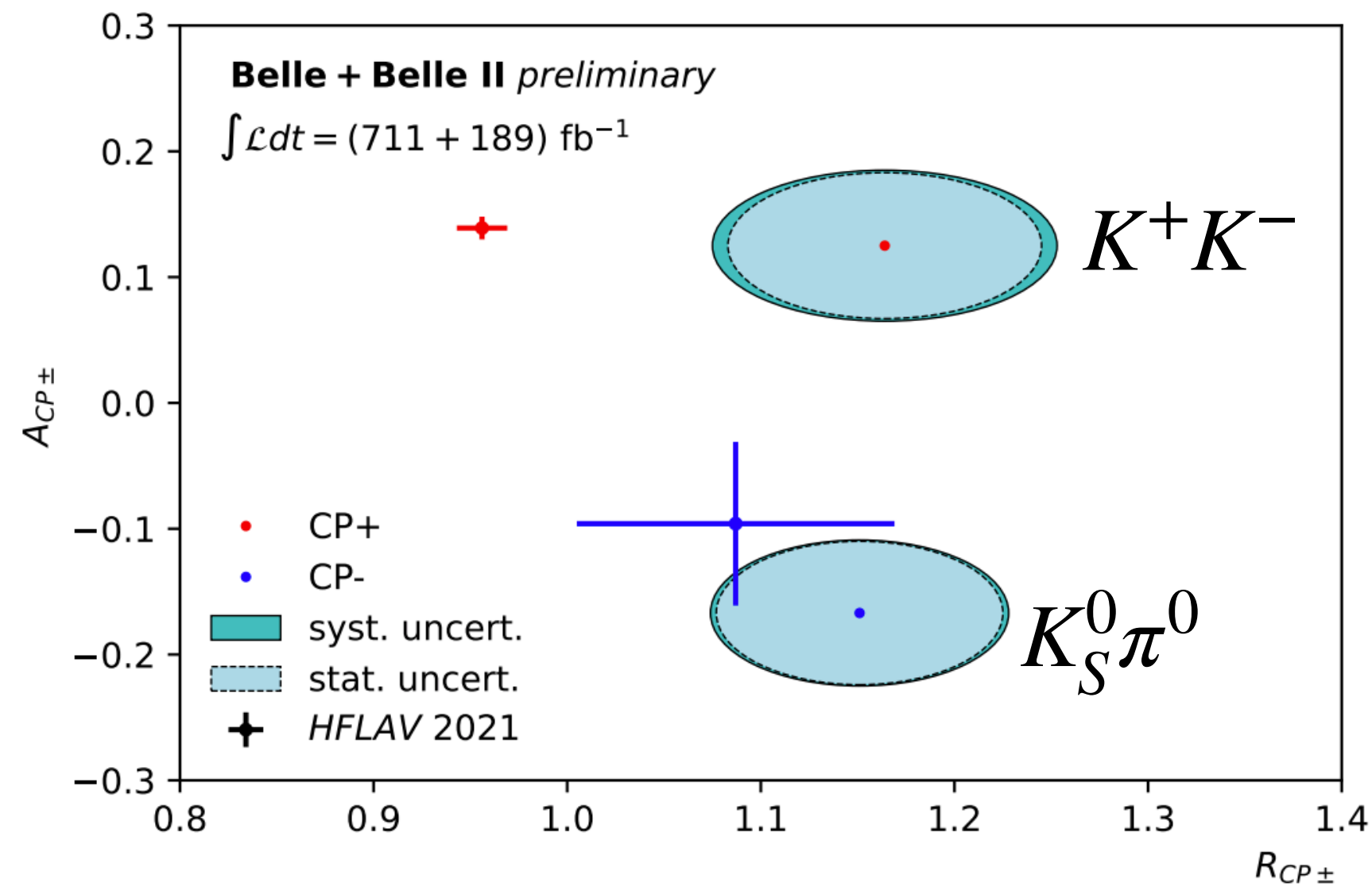
$$= 2\eta_{CP} r_B \sin(\delta_B) \sin(\phi_3) / R_{CP\pm}.$$

- Can't determine ϕ_3 from GLW only:
 $(\phi_3, \delta_B) \leftrightarrow (\delta_B, \phi_3)$ or $(\delta_B - \pi, \phi_3 - \pi)$..

GLW results from Belle and Belle II

$$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 \pi^0, K^+ K^-$$

arXiv:2308.05048 submit to JHEP



189 fb⁻¹ Belle II
 +711 fb⁻¹ Belle

$$B^+ \rightarrow D^* K^+, D \rightarrow K_S^0 \pi^0, K^+ K^-, \pi^+ \pi^-, K_S^0 \phi, K_S^0 \omega,$$

Phys. Rev. D 73 (2006) 051106

$$\mathcal{A}_1^* = -0.20 \pm 0.22(\text{stat}) \pm 0.04(\text{sys})$$

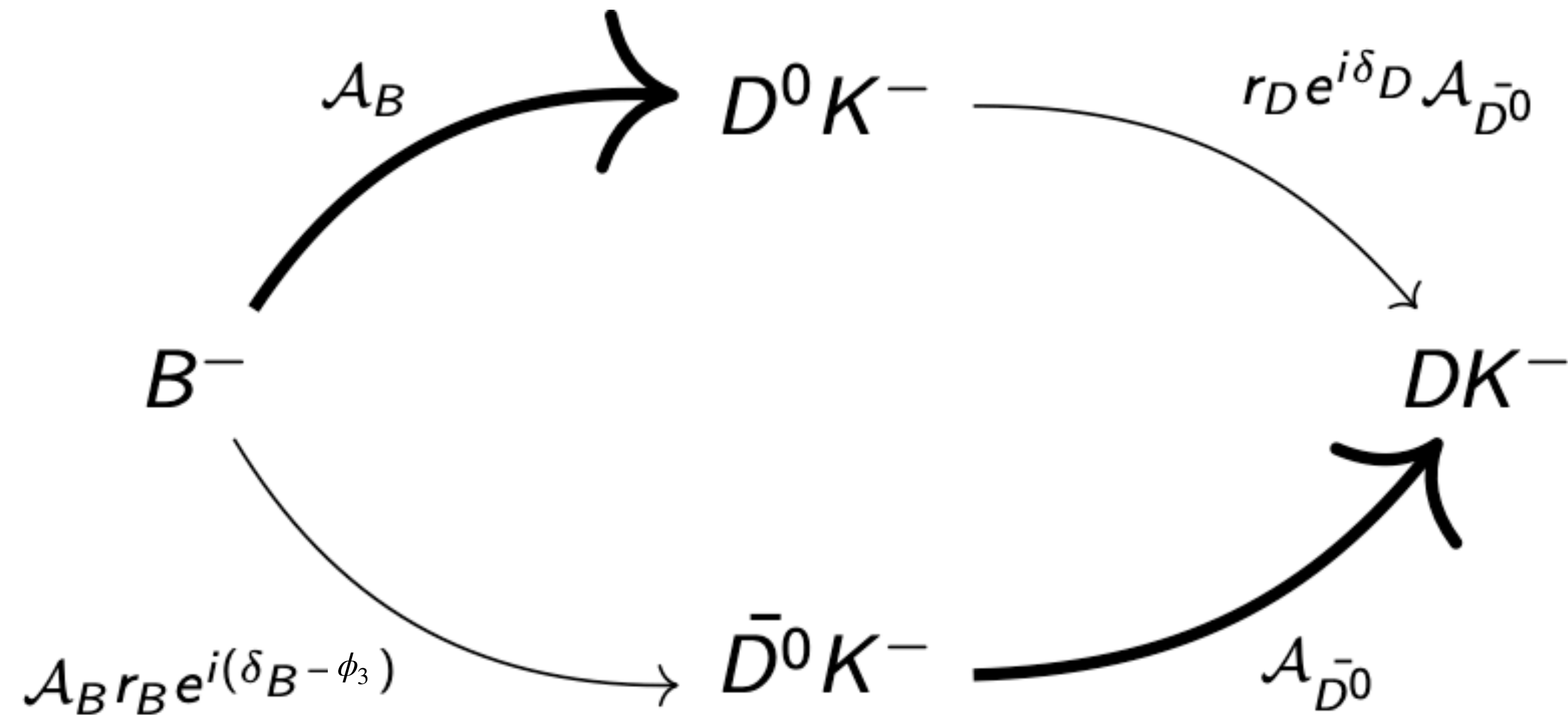
$$\mathcal{A}_2^* = 0.13 \pm 0.30(\text{stat}) \pm 0.08(\text{sys}),$$

$$\mathcal{R}_1^* = 1.41 \pm 0.25(\text{stat}) \pm 0.06(\text{sys})$$

$$\mathcal{R}_2^* = 1.15 \pm 0.31(\text{stat}) \pm 0.12(\text{sys}).$$

250 fb⁻¹ Belle

ADS methods



- Observables:

$$R_{\text{ADS}}^{K\pi} = \frac{\mathcal{B}(B^- \rightarrow [f]_D K^-) + \mathcal{B}(B^+ \rightarrow [\bar{f}]_D K^+)}{\mathcal{B}(B^- \rightarrow [\bar{f}]_D K^-) + \mathcal{B}(B^+ \rightarrow [f]_D K^+)},$$

$$= r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \phi_3,$$

$$A_{\text{ADS}}^{K\pi} = \frac{\mathcal{B}(B^- \rightarrow [f]_D K^-) - \mathcal{B}(B^+ \rightarrow [\bar{f}]_D K^+)}{\mathcal{B}(B^- \rightarrow [f]_D K^-) + \mathcal{B}(B^+ \rightarrow [\bar{f}]_D K^+)},$$

$$= 2r_B r_D \sin(\delta_B + \delta_D) \sin \phi_3 / R_{\text{ADS}},$$

- D decays to CF/DCS eigenstates, e.g. $K^+ \pi^-, K^+ \pi^- \pi^0$
- Would be best if $r_D/r_B \sim 1$, then similar amplitude \rightarrow enhanced interference.

- For both $K^+ \pi^-, K^+ \pi^- \pi^0$, $\delta_D \sim 180^\circ$, then similar to GLW. Can't determine ϕ_3 from ADS only.

ADS results from Belle

$$B^+ \rightarrow Dh^+, D \rightarrow K^+\pi^-$$

Phys. Rev. Lett. 106 (2011) 231803

711 fb⁻¹ Belle

$$\mathcal{R}_{DK} = [1.63_{-0.41}^{+0.44}(\text{stat})_{-0.13}^{+0.07}(\text{syst})] \times 10^{-2},$$

$$\mathcal{R}_{D\pi} = [3.28_{-0.36}^{+0.38}(\text{stat})_{-0.18}^{+0.12}(\text{syst})] \times 10^{-3},$$

$$\mathcal{A}_{DK} = -0.39_{-0.28}^{+0.26}(\text{stat})_{-0.03}^{+0.04}(\text{syst}),$$

$$\mathcal{A}_{D\pi} = -0.04 \pm 0.11(\text{stat})_{-0.01}^{+0.02}(\text{syst}),$$

$$B^+ \rightarrow Dh^+, D \rightarrow K^+\pi^-\pi^0$$

Phys. Rev. D 88 (2013) 9, 091104

711 fb⁻¹ Belle

$$R_{DK} = [1.98 \pm 0.62(\text{stat.}) \pm 0.24(\text{syst.})] \times 10^{-2},$$

$$R_{D\pi} = [1.89 \pm 0.54(\text{stat.})_{-0.25}^{+0.22}(\text{syst.})] \times 10^{-3}.$$

$$A_{DK} = 0.41 \pm 0.30(\text{stat.}) \pm 0.05(\text{syst.}),$$

$$A_{D\pi} = 0.16 \pm 0.27(\text{stat.})_{-0.04}^{+0.03}(\text{syst.}).$$

GLS results from Belle and Belle II

$B^\pm \rightarrow DK^\pm, D\pi^\pm$ with $D \rightarrow K_S^0 K^\pm \pi^\mp$: SS: same-sign, OS: opposite sign.

Two sets of results: in full D phase space and in the K^*K region (expected large δ_D).

Observe 4 Acp and 3 BR ratios.

362 fb⁻¹ Belle II
+711 fb⁻¹ Belle

In K^*K region:

$$A_{SS}^{DK} = \frac{2r_B^{DK} r_D \kappa_D \sin(\delta_B^{DK} - \delta_D) \sin \phi_3}{1 + (r_B^{DK})^2 r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} - \delta_D) \cos \phi_3},$$

$$A_{OS}^{DK} = \frac{2r_B^{DK} r_D \kappa_D \sin(\delta_B^{DK} + \delta_D) \sin \phi_3}{(r_B^{DK})^2 + r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} + \delta_D) \cos \phi_3},$$

$$A_{SS}^{D\pi} = \frac{2r_B^{D\pi} r_D \kappa_D \sin(\delta_B^{D\pi} - \delta_D) \sin \phi_3}{1 + (r_B^{D\pi})^2 r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} - \delta_D) \cos \phi_3},$$

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$$R_{SS}^{DK/D\pi} = R \frac{1 + (r_B^{DK})^2 r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} - \delta_D) \cos \phi_3}{1 + (r_B^{D\pi})^2 r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} - \delta_D) \cos \phi_3},$$

$$R_{OS}^{DK/D\pi} = R \frac{(r_B^{DK})^2 + r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} + \delta_D) \cos \phi_3}{(r_B^{D\pi})^2 + r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} + \delta_D) \cos \phi_3},$$

$$R_{SS/OS}^{D\pi} = \frac{1 + (r_B^{D\pi})^2 r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} - \delta_D) \cos \phi_3}{(r_B^{D\pi})^2 + r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} + \delta_D) \cos \phi_3}.$$

$$A_{SS}^{DK} = 0.055 \pm 0.119 \pm 0.020,$$

$$A_{OS}^{DK} = 0.231 \pm 0.184 \pm 0.014,$$

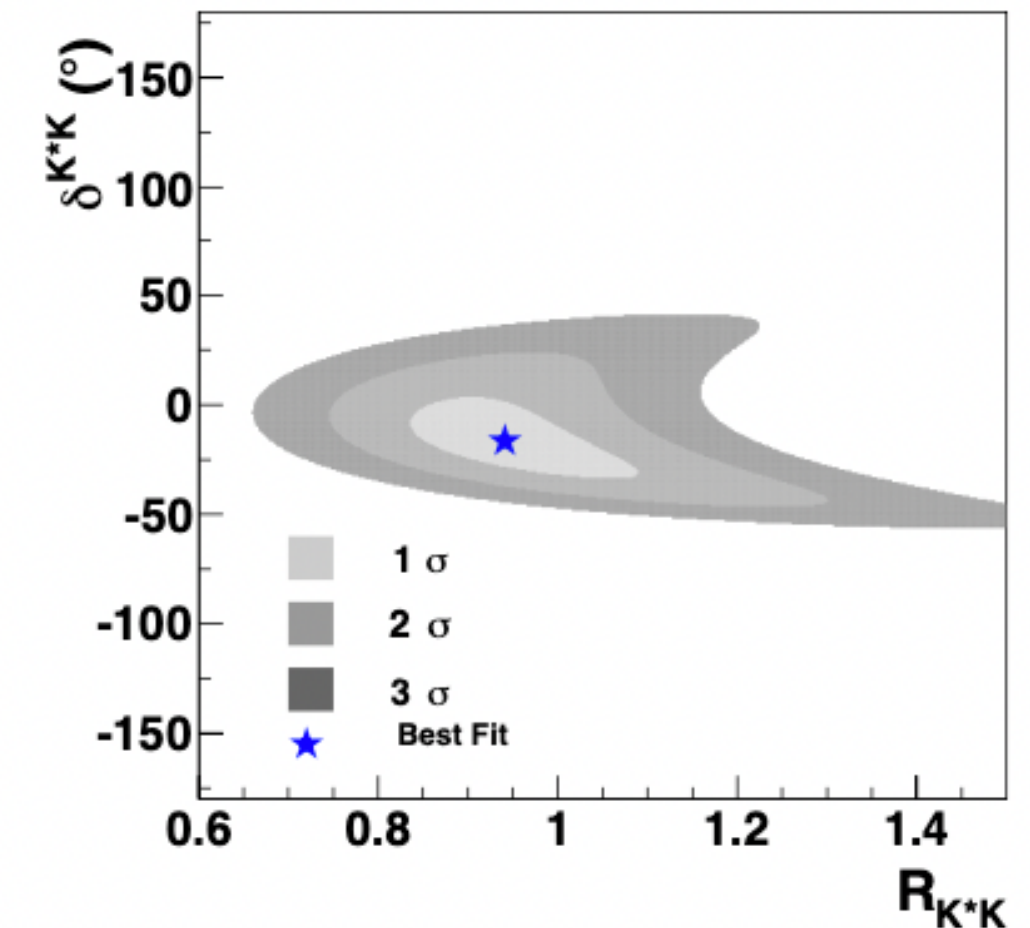
$$A_{SS}^{D\pi} = 0.046 \pm 0.029 \pm 0.016,$$

$$A_{OS}^{D\pi} = 0.009 \pm 0.046 \pm 0.009,$$

$$R_{SS}^{DK/D\pi} = 0.093 \pm 0.012 \pm 0.005,$$

$$R_{OS}^{DK/D\pi} = 0.103 \pm 0.020 \pm 0.006,$$

$$R_{SS/OS}^{D\pi} = 2.412 \pm 0.132 \pm 0.019,$$



Outline

- Why CPV is interesting and what is CKM matrix
- About γ/ϕ_3
- SuperKEKB and Belle II
- All γ/ϕ_3 results from Belle and Belle II
- **Discussion and outlook**

Combination at Belle & Belle II?

HFLAV doesn't think there is a Belle's ϕ_3 .

(*) Belle presented in 2012 a preliminary combination of their results, but this remains unpublished after more than two years and therefore we do not list it.

<p>BaBar obtain $\gamma = (69^{+17}_{-16})^\circ$ $r_B(DK^+) = 0.092^{+0.013}_{-0.012}$ $\delta_B(DK^+) = (105^{+16}_{-17})^\circ$ $r_B(D^*K^+) = 0.0106^{+0.019}_{-0.036}$ $\delta_B(D^*K^+) = (294^{+21}_{-31})^\circ$ $r_B(DK^{*+}) = 0.143^{+0.048}_{-0.049}$ (*) $\delta_B(DK^{*+}) = (101 \pm 43)^\circ$ (*) PRD 87 (2013) 052015 </p>	<p>LHCb obtain $\gamma = (67 \pm 4)^\circ$ $r_B(DK^+) = 0.0989 \pm 0.0050$ $\delta_B(DK^+) = (131.2^{+5.1}_{-5.9})^\circ$ $r_B(D^*K^+) = 0.191^{+0.045}_{-0.038}$ $\delta_B(D^*K^+) = (332^{+8}_{-10})^\circ$ $r_B(DK^{*+}) = 0.092^{+0.018}_{-0.033}$ $\delta_B(DK^{*+}) = (40^{+92}_{-20})^\circ$ $r_B(DK^{*0}) = 0.221^{+0.044}_{-0.047}$ $\delta_B(DK^{*0}) = (187^{+21}_{-23})^\circ$ $r_B(DK\pi\pi) = 0.081^{+0.025}_{-0.027}$ $\delta_B(DK\pi\pi) = (351^{+9}_{-37})^\circ$ $r_B(D_s K) = 0.30 \pm 0.09$ $\delta_B(D_s K) = (355^{+17}_{-16})^\circ$ $\delta_B(D\pi) = (17^{+29}_{-17})^\circ$ LHCb-CONF-2018-002, LHCb-CONF-2020-003</p>
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- Belle II now have three ϕ_3 -results: $B^+ \rightarrow Dh^+$, $D \rightarrow K_S^0 h^+ h^-$, $K_S^0 \pi^0$, $K^+ K^-$, $K_S^0 K^\pm \pi^\mp$
- It's time to have a Belle(II)'s ϕ_3 now, especially we can have a better feeling on the coming Belle II data.

Some discussion about ϕ_3 combination

- We're working on the combination. Plan to release at CKM conference at September 18-22, 2023.
- Now, let's discuss with all public information...

Some discussion about ϕ_3 combination

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- Now, let's discuss with all public information...
- From the golden channel
 $B^+ \rightarrow Dh^+, D \rightarrow K_S^0 h^+ h^-$ (JHEP 02(2022)063):

$$\begin{aligned}\phi_3 &= (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ, \\ \underline{r_B^{DK}} &= 0.129 \pm 0.024 \pm 0.001 \pm 0.002, \\ \delta_B^{DK} &= (124.8 \pm 12.9 \pm 0.5 \pm 1.7)^\circ, \\ r_B^{D\pi} &= 0.017 \pm 0.006 \pm 0.001 \pm 0.001, \\ \delta_B^{D\pi} &= (341.0 \pm 17.0 \pm 1.2 \pm 2.6)^\circ.\end{aligned}$$

Comparing to W.A.: [HFLAV]

$$\begin{aligned}\phi_3 &= (65.9_{-3.5}^{+3.3})^\circ \\ r_B(DK^-) &= (0.0994 \pm 0.0026) \\ \delta_B(DK^-) &= (127.7_{-3.9}^{+3.6})^\circ \\ r_B(D\pi^-) &= (0.0049 \pm 0.0006) \\ \delta_B(D\pi^-) &= (294_{-11}^{+9.7})^\circ\end{aligned}$$

- Large r_B observed now, so if future Belle II's data favor the w.a. r_B , the ϕ_3 's precision will be worse a bit with same data size.

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- $(\delta_B(D\pi) + \delta_D) \sim 180^\circ$, $\cos(\delta_B(D\pi) + \delta_D)$'s uncertainty is much smaller than expected -> unexpected precision from ADS method. Not true anymore with w.a. $\delta_B(D\pi)$.

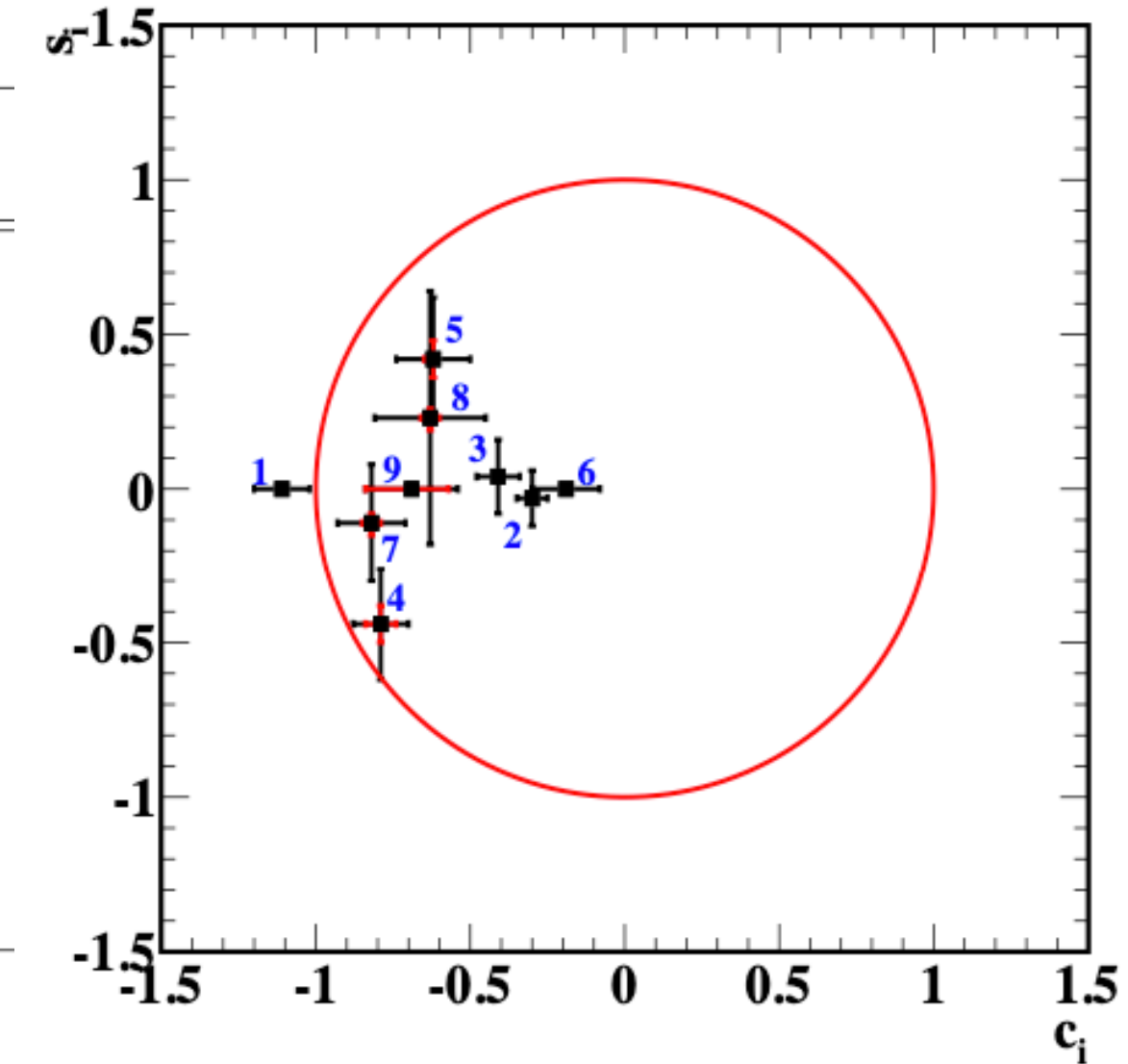
Updates expect in near future

$$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 \pi^+ \pi^- \pi^0 \left((5.7_{-8.8}^{+10.2} \pm 3.5 \pm 5.7)^\circ \right)$$

, currently only CLEO's ci,si, binning scheme is available, which is **not** optimized for ϕ_3 .

$$\text{Large Br: } 5.2\%; \quad F_+ \sim 0.3, \quad \sum c_i \sqrt{T_i \bar{T}_i} \sim -0.2$$

Bin	Bin region	m_L (GeV/c ²)	m_U (GeV/c ²)
1	$m_{\pi^+\pi^-\pi^0} \approx m_\omega$	0.762	0.802
2	$m_{K_S^0\pi^-} \approx m_{K^{*-}}$ &	0.790	0.994
	$m_{\pi^+\pi^0} \approx m_{\rho^+}$	0.610	0.960
3	$m_{K_S^0\pi^+} \approx m_{K^{*+}}$ &	0.790	0.994
	$m_{\pi^-\pi^0} \approx m_{\rho^-}$	0.610	0.960
4	$m_{K_S^0\pi^-} \approx m_{K^{*-}}$	0.790	0.994
5	$m_{K_S^0\pi^+} \approx m_{K^{*+}}$	0.790	0.994
6	$m_{K_S^0\pi^0} \approx m_{K^{*0}}$	0.790	0.994
7	$m_{\pi^+\pi^0} \approx m_{\rho^+}$	0.610	0.960
8	$m_{\pi^-\pi^0} \approx m_{\rho^-}$	0.610	0.960
9	Remainder	-	-



We expect an optimized binning scheme and a precise ci/si from BESIII's 8fb⁻¹(~ 10 times than CLEO's).

Expect a more “normal” result from this channel.

By Toy MC, @50/ab, from $B^+ \rightarrow Dh^+, D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$,

- with current Ti/ci/si, $\sim 5^\circ$
- With Kspipi's Ti/ci/si, $\sim 2^\circ$

Updates expect in future

Extra channels: (<https://confluence.desy.de/display/BI/Physics+BtoCharm>)

$B^+ \rightarrow Dh^+, D \rightarrow K_L \pi^+ \pi^-$: Unique to Belle/BelleII

$B^+ \rightarrow Dh^+, D \rightarrow K^- \pi^+ \pi^- \pi^+$: BESIII tells the local information.

$B^+ \rightarrow Dh^+, D \rightarrow K^- K^+ \pi^0 / \pi^- \pi^+ \pi^0$: BESIII will measure the local information.

$B^+ \rightarrow Dh^+, D \rightarrow \pi^- \pi^+ \pi^0 \pi^0$: Belle/BelleII's advantage

$B^+ \rightarrow Dh^+, D \rightarrow K^- \pi^+ \pi^0$: local information? Will also be helpful for mixing study.

~6° @50/ab; may better with optimized bins

New novel methods when we have 20 ab^{-1} ?

Un-binned way (Fourier analysis) in $B^+ \rightarrow Dh^+, D \rightarrow K_S \pi^+ \pi^-$ [[Eur.Phys.J.C 78 \(2018\) 2, 121](#)]

Combined fit between B data and charm data (BESIII). (LHCb are doing it now.)

...

Determine hadronic parameter independently?

Measure r_B^{DK} solo? Now in all methods, we determine r_B^{DK} , δ_B^{DK} , ϕ_3 simultaneously.

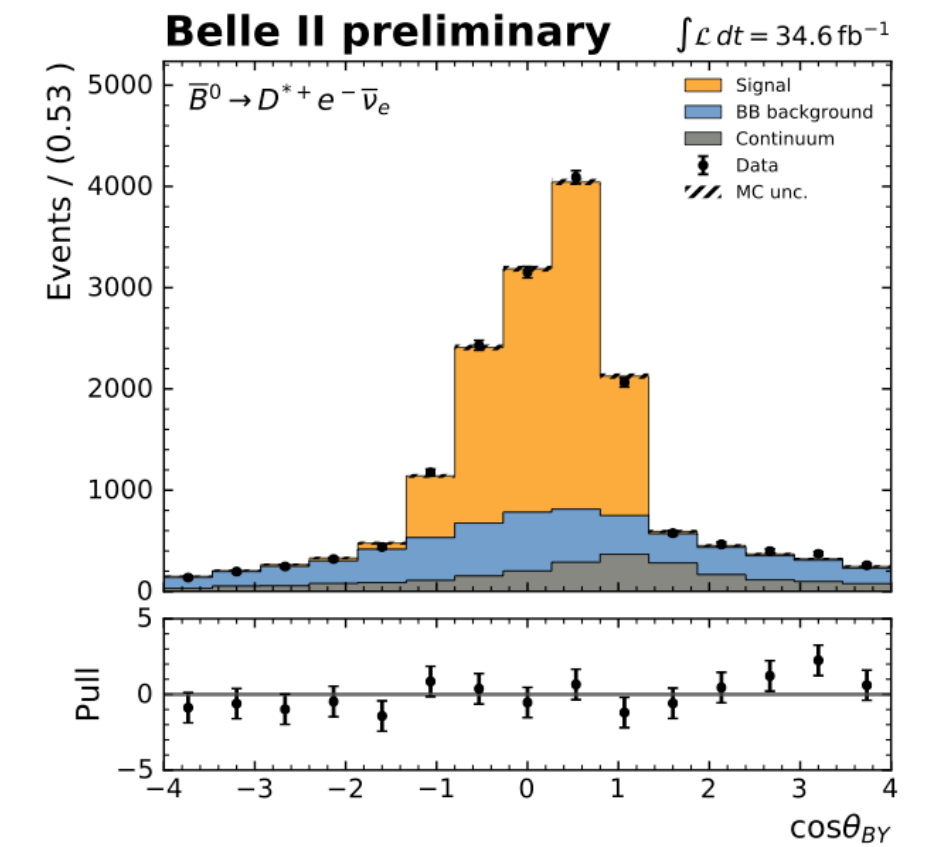
And we know the ϕ_3 's precision highly depends on r_B^{DK} 's value.

Can we determine r_B^{DK} solo? Will be an important extra constrain on ϕ_3 !

Experimentally: $N(B^+ \rightarrow D^0 K^+, D^0 \rightarrow K^- e^+ \nu_e) / N(B^+ \rightarrow \bar{D}^0 K^+, \bar{D}^0 \rightarrow K^+ e^- \bar{\nu}_e)$,

Rough estimation: for CF channel: $N(\text{raw}) / 1 \text{ ab}^{-1} \sim 6500$

- If use hadronic tag (FEI): eff $\sim 0.2\%$? $N(\text{CF}) \sim 600$ at 50 ab^{-1}
- Untag? Fit $\cos\theta_{BY}$, like semi-leptonic study. Maybe more difficult, due to small $p(\nu_e)$.
 $N(\text{CF}) \sim 60000$ at 50 ab^{-1} , 4% precision? Won't be useful.



$$\cos\theta_{BY} = \frac{2E_B^* E_Y^* - M_B^2 - m_Y^2}{2p_B^* p_Y^*}$$

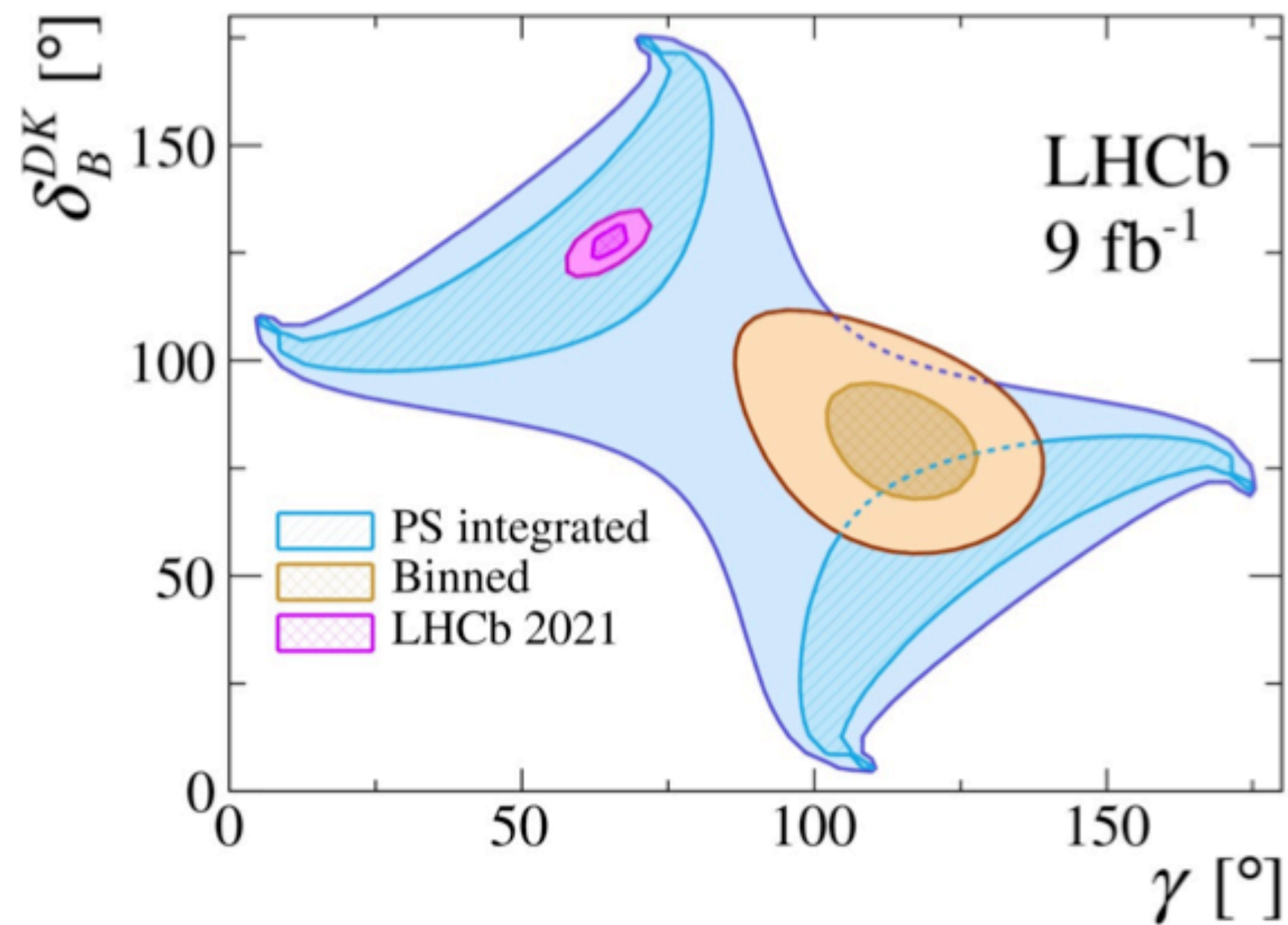
More idea? In paper [arXiv:1606.09129](https://arxiv.org/abs/1606.09129), they use branching ratios and r_B^{DK} to determine $r_B^{D\pi}$ with SU(3) symmetry.

(Before summary) why Belle II still work on ϕ_3 ?

- Almost all channels are full reconstructed. LHCb is a monster...
- ϕ_3 is a basic parameter, as another B-factory, we must give our ϕ_3 , to confirm LHCb's ϕ_3 .

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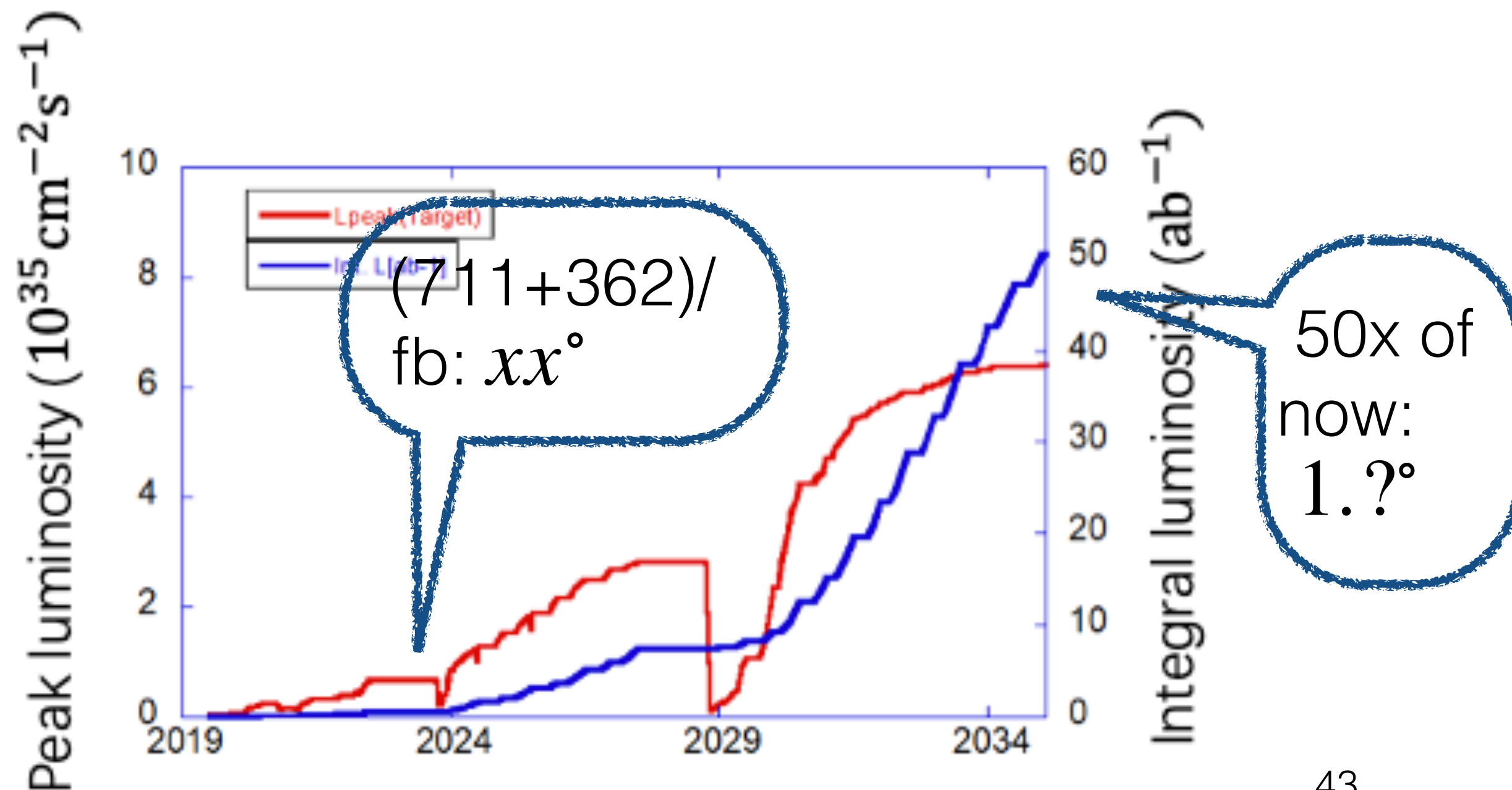
- Almost all channels are full reconstructed. LHCb is a monster...
- ϕ_3 is a basic parameter, as another B-factory, we must give our ϕ_3 , to confirm LHCb's ϕ_3 .
- LHCb has interesting ϕ_3 in some channels. \rightarrow Need Belle II's crosscheck.



Model-dependent $K^+K^-\pi^+\pi^-$
[Eur. Phys. J. **C83** (2023) 547]

(Before summary) why Belle II still work on ϕ_3 ?

- Almost all channels are full reconstructed. LHCb is a monster...



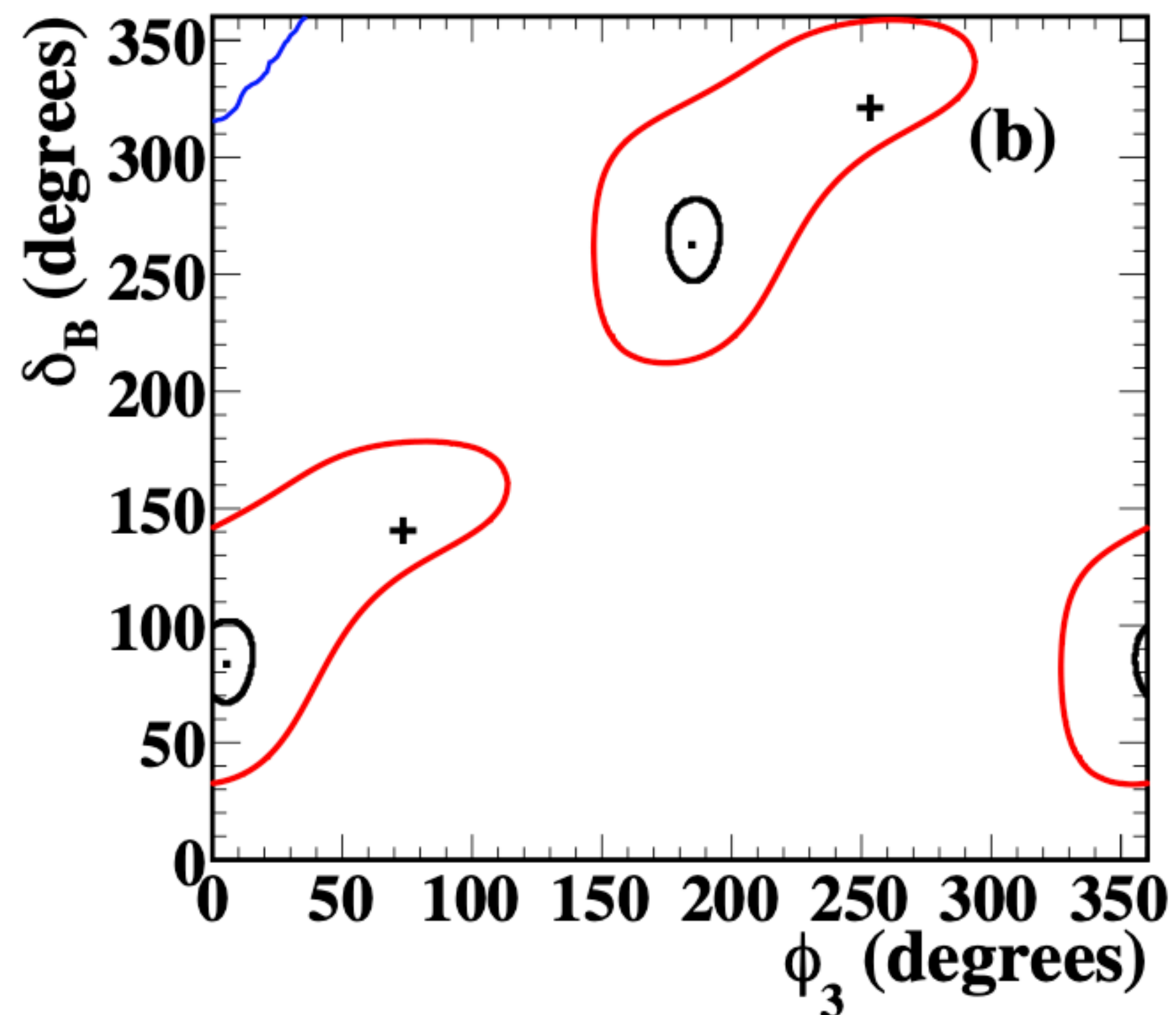
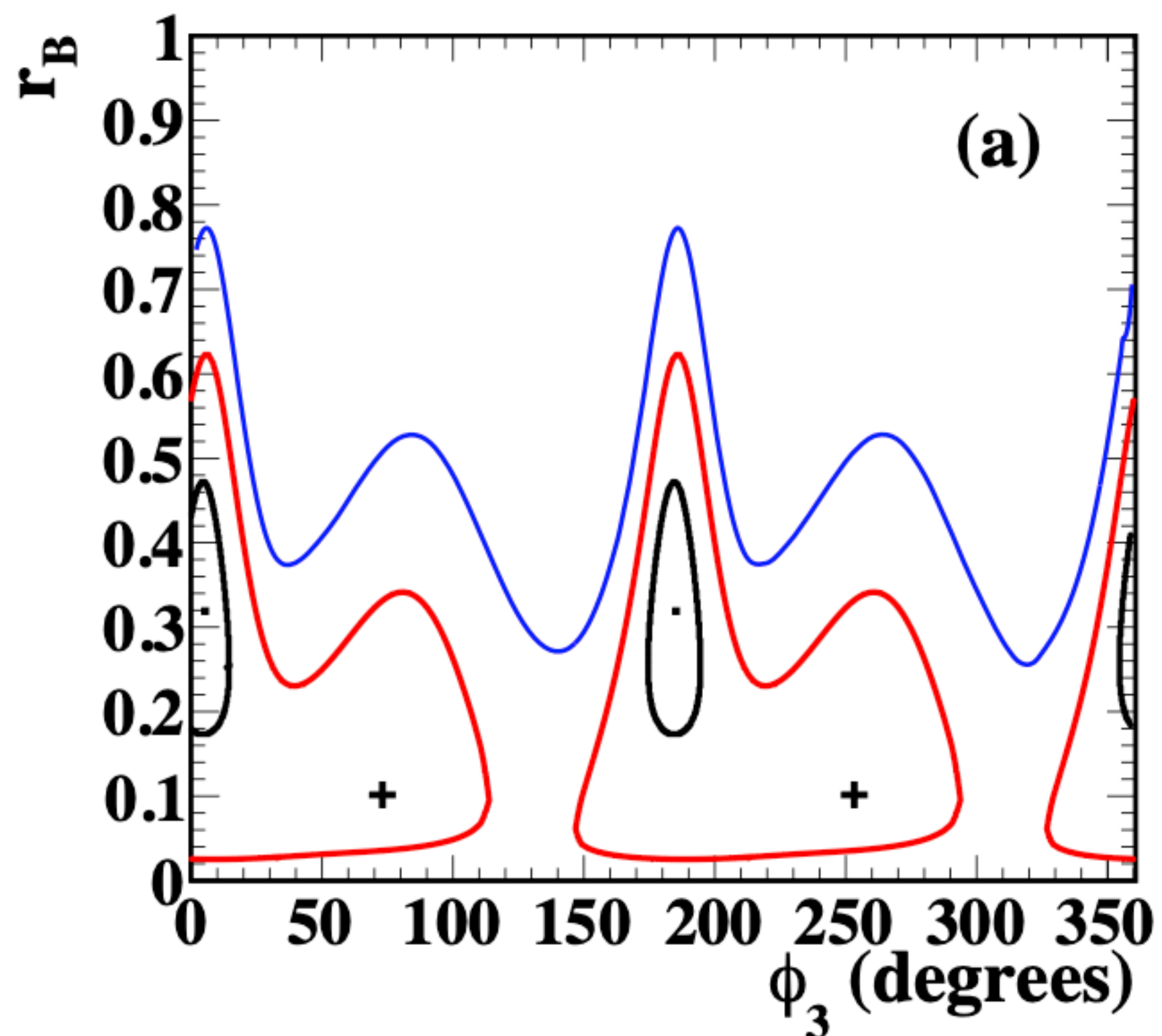
- Still a chance to show same sensitivity to ϕ_3 !

Summary

- Review the γ/ϕ_3 measurement at Belle (II). Discuss about combination of γ/ϕ_3 (CKM conference 2023).
- For future, important channels:
 - $B^+ \rightarrow Dh^+, D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$, need wait BESIII's new binning scheme and ci/si
 - $B^+ \rightarrow Dh^+, D \rightarrow h^+ h^- \pi^0$, BESIII may have local information few years later
 - $B^+ \rightarrow Dh^+, D \rightarrow K_L^0 \pi^+ \pi^-$, Belle II's unique channel.
 - $B^+ \rightarrow Dh^+, D \rightarrow \pi^+ \pi^- \pi^0 \pi^0$, Belle II's advantage.
 - $B^+ \rightarrow Dh^+, D \rightarrow K^- \pi^+ \pi^0$: local information? Will also be helpful for mixing study.
- This CKM angle γ/ϕ_3 is not only B factory's task, also need BESIII's contribution.
- Let's make γ/ϕ_3 a **candle** parameter!

Thank you!

Back-Up



$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| e^{-i\beta} & -|V_{ts}| e^{i\beta_s} & |V_{tb}| \end{pmatrix} + \mathcal{O}(\lambda^5) \sim \begin{pmatrix} 1 & 0.2 & 0.004 \\ 0.2 & 1 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix}$$

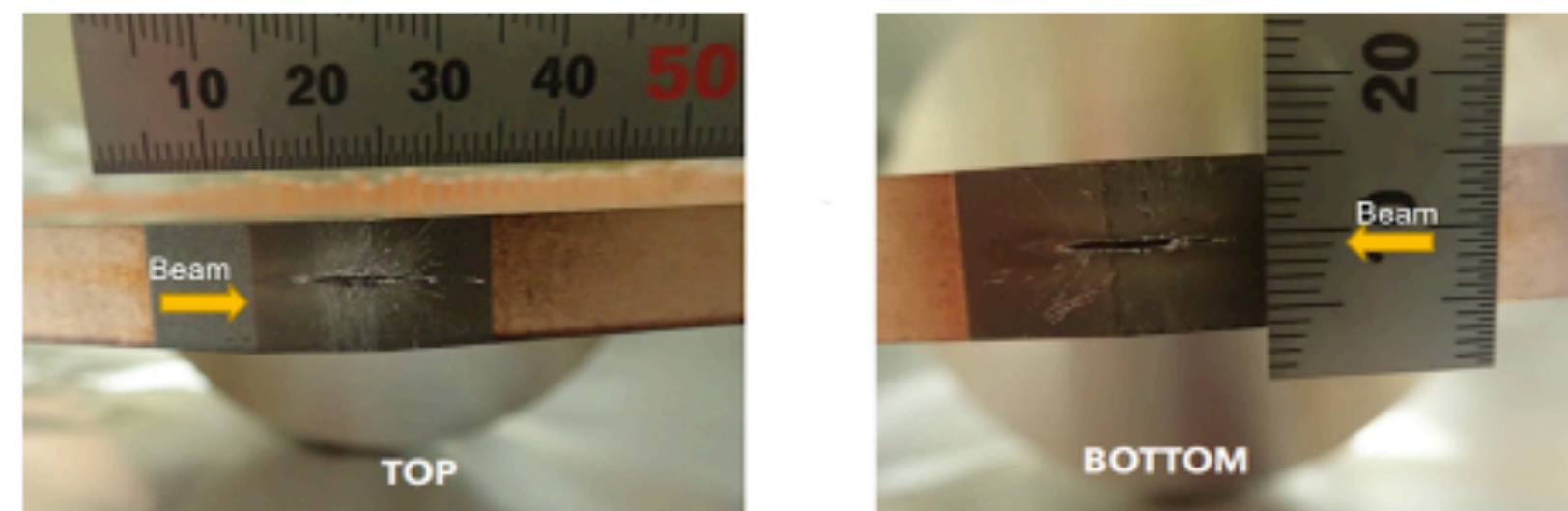
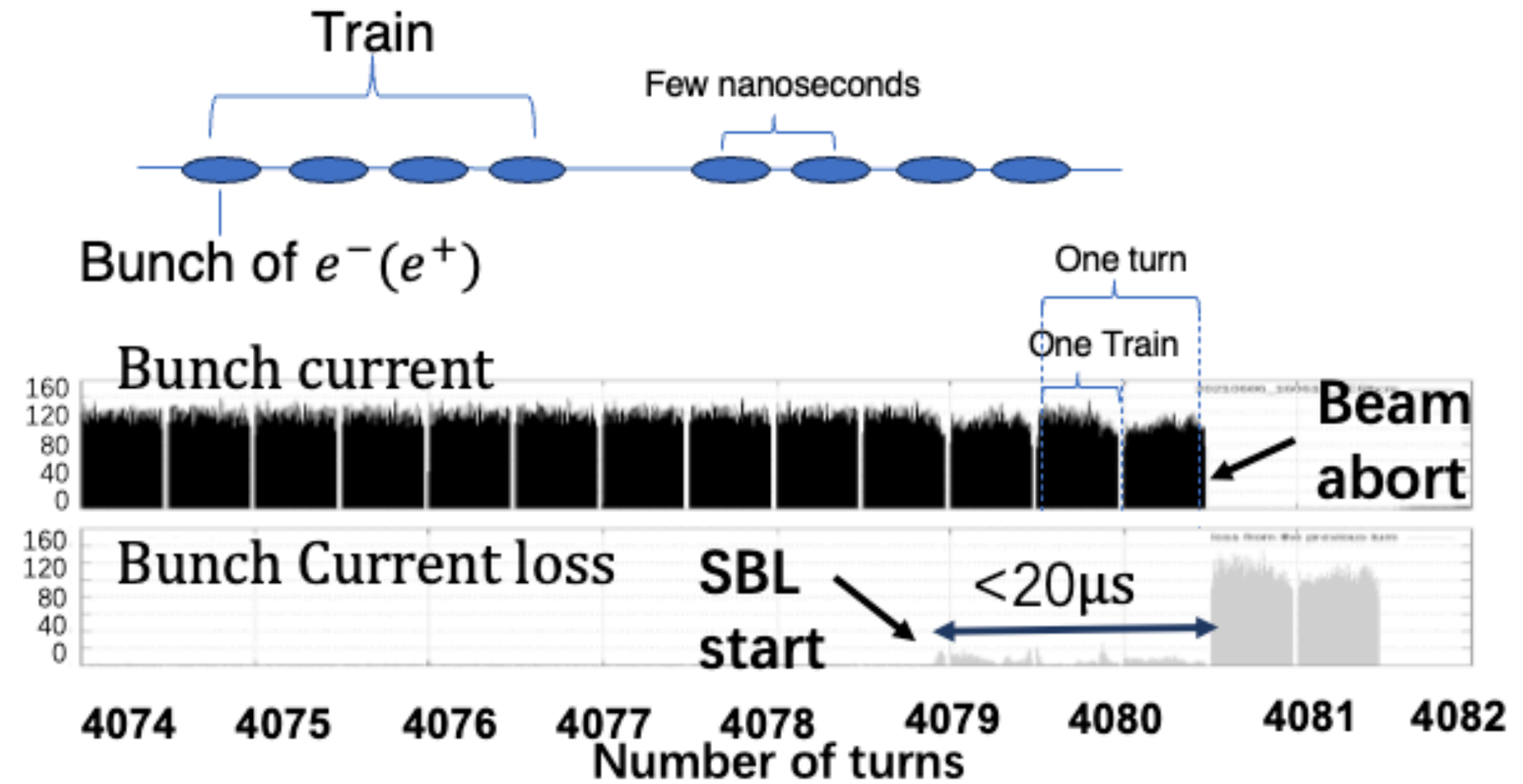
Introduction – Sudden beam loss

Sudden beam loss:

- Fast beam loss within three or four turns (1 turn $\sim 10 \mu\text{s}$)
- Reasons remain unknown
- More likely occurred in LER.

Effects of Sudden beam loss

- Caused severe damage to the vertical collimators
- Caused quenches of final focusing magnets (QCS)
- Resulted in large radiation doses around the interaction region (IR)
- **limited the maximum bunch current**



Collimator head after catastrophic sudden beam loss

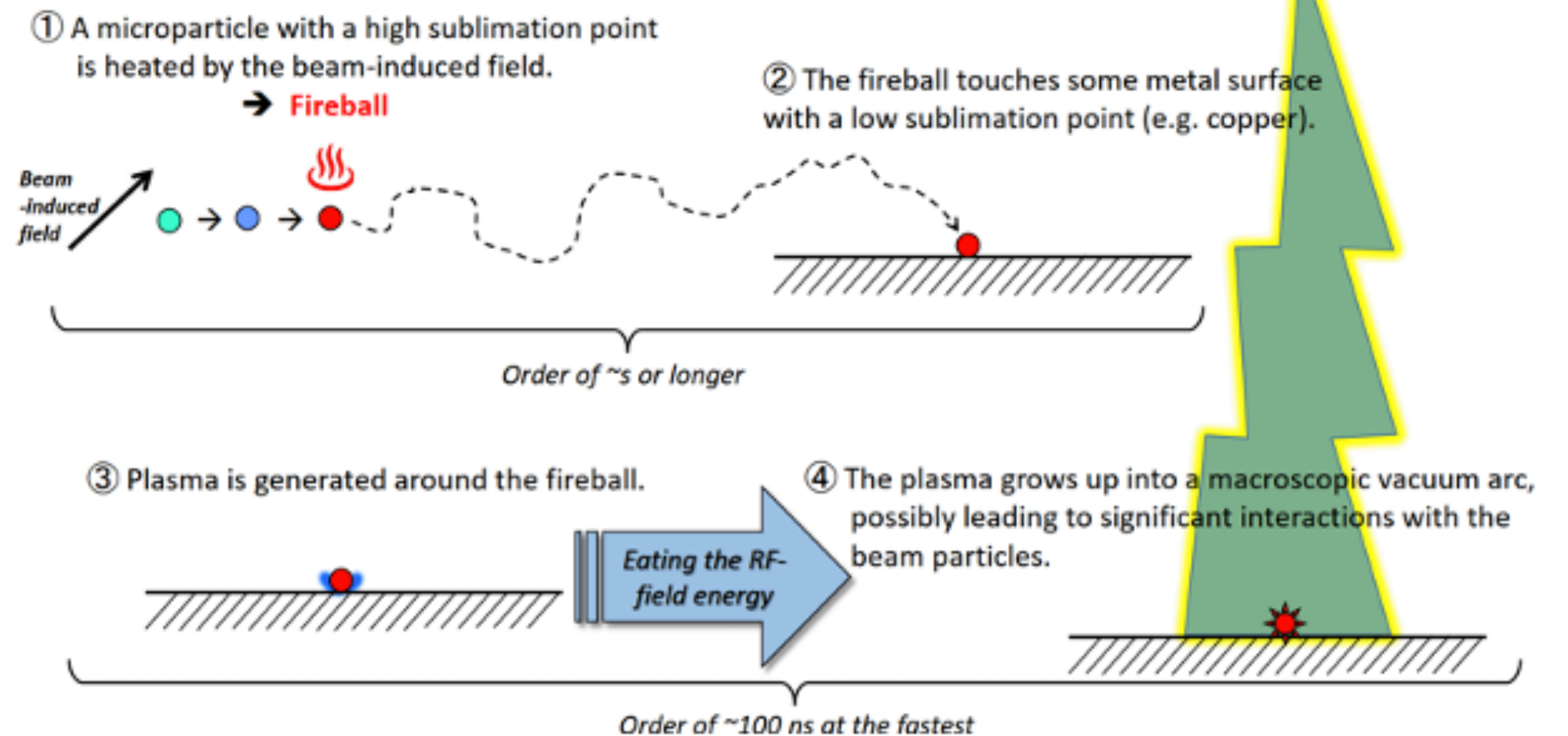
Discussion -- possible cause of Sudden Beam Loss

Can not be attributed to conventional beam instabilities: too fast (less than 3-4 turns) and no beam instabilities observed

May not be due to Beam-dust interaction: examined in simulation, in which the beam particles are lost mainly at the horizontal collimators while what we observed is mainly at vertical collimators.

“Fire ball” Hypotheses has been proposed as a possible reason for sudden beam loss.

Physical process of the “Fireball” hypothesis, leading to fast beam loss



$$d\Gamma_{B^\pm}(\mathbf{x}) = A_{(\pm, \mp)}^2 + r_B^2 A_{(\mp, \pm)}^2 + 2A_{(\pm, \mp)}A_{(\mp, \pm)} \left[\underbrace{r_B \cos(\delta_B \pm \gamma)}_{x_\pm} \underbrace{\cos(\delta_{D(\pm, \mp)})}_{c_i} + \underbrace{r_B \sin(\delta_B \pm \gamma)}_{y_\pm} \underbrace{\sin(\delta_{D(\pm, \mp)})}_{s_i} \right]$$

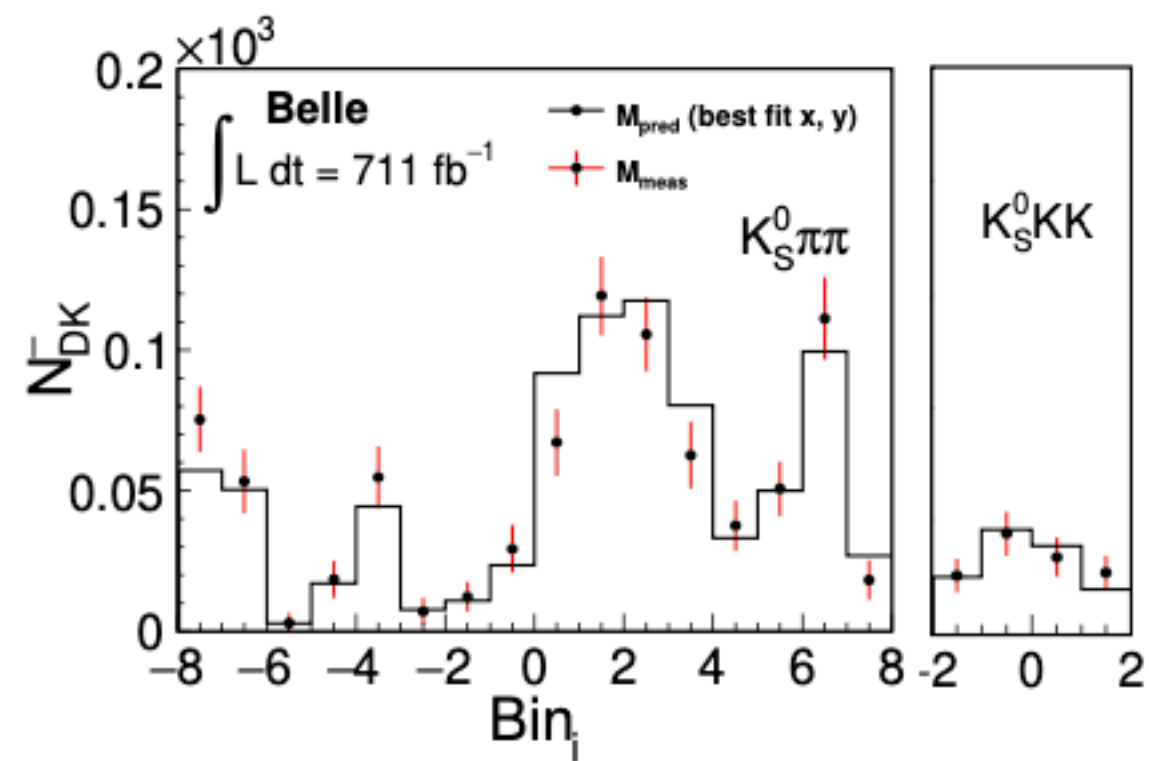
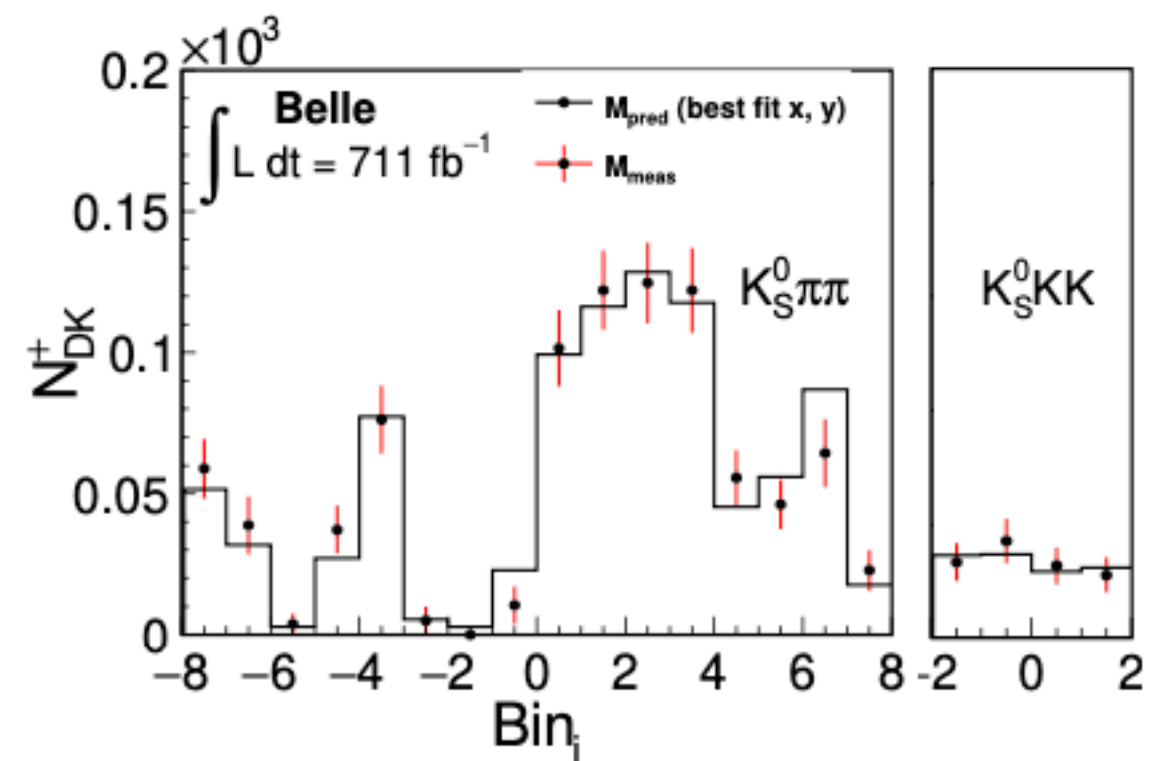
$$N_i^+ = h_{B^+} \left[F_{-i} + \left\{ (x_+^{DK})^2 + (y_+^{DK})^2 \right\} F_i + 2\sqrt{F_i F_{-i}} (x_+^{DK} c_i - y_+^{DK} s_i) \right],$$

$$N_{-i}^+ = h_{B^+} \left[F_i + \left\{ (x_+^{DK})^2 + (y_+^{DK})^2 \right\} F_{-i} + 2\sqrt{F_i F_{-i}} (x_+^{DK} c_i + y_+^{DK} s_i) \right],$$

$$N_i^- = h_{B^-} \left[F_i + \left\{ (x_-^{DK})^2 + (y_-^{DK})^2 \right\} F_{-i} + 2\sqrt{F_i F_{-i}} (x_-^{DK} c_i + y_-^{DK} s_i) \right],$$

$$N_{-i}^- = h_{B^-} \left[F_{-i} + \left\{ (x_-^{DK})^2 + (y_-^{DK})^2 \right\} F_i + 2\sqrt{F_i F_{-i}} (x_-^{DK} c_i - y_-^{DK} s_i) \right],$$





5×10^{-9} , and the small size of the interference, proportional to $r_B \approx c_F |V_{cs} V_{ub}^*| / |V_{us} V_{cb}^*| \approx 0.1$, where $c_F \approx 0.2$ is a color suppression factor [11–13]. Therefore a pre-

$$L = \frac{N_+ N_- f}{4\pi \sigma_x^* \sigma_y^*} R_L$$

Number of positrons in a bunch
Number of electrons in a bunch
Collision frequency of bunches
 $f = n_b f_0$ n_b : No. of bunches
 f_0 : rotation frequency
Horizontal beam size at collision point
Vertical beam size at collision point
geometrical loss factor