

# CP Violation in charm



**Fu-Sheng Yu**  
**Lanzhou University**

24 May, 2019 @ USTC, Hefei

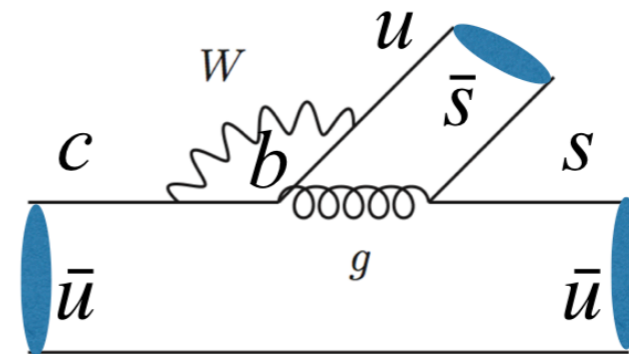
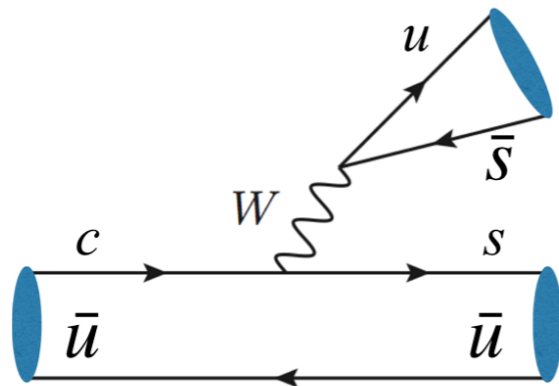
**Thank Wenbiao for invitation !**

# LHCb observes charm CPV

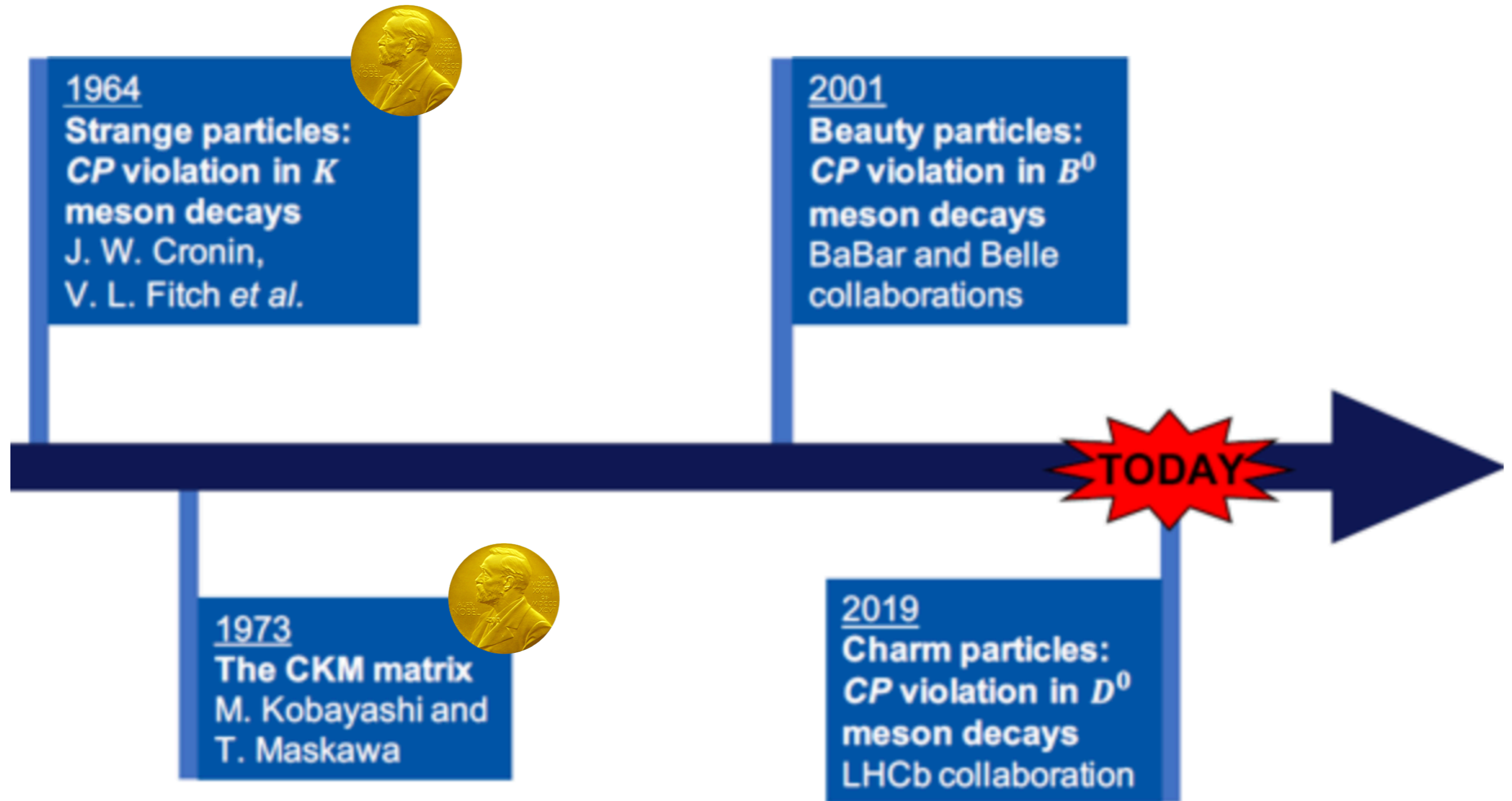
1903.08726

$$\begin{aligned}\Delta A_{CP} &= A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-) \\ &= (-1.54 \pm 0.29) \times 10^{-3}\end{aligned}$$

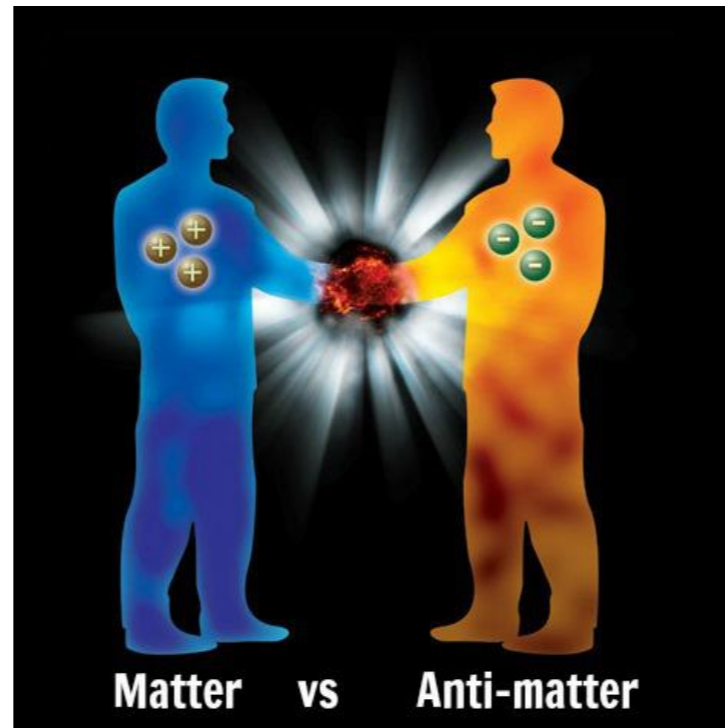
- $> 5\sigma$  , first observation of CPV in charm



# LHCb observes charm CPV



**An important milestone  
in particle physics**



- ❖ Matter-Antimatter asymmetry of the Universe
- ❖ Sakharov conditions: [Sakharov, 1967]
  - 1) C and **CP violation**
  - 2) Baryon number violation
  - 3) Out-of-equilibrium dynamics



# CP violation

- Asymmetry between particle and anti-particle

$$A_{CP}(f; t) \equiv \frac{\Gamma(D^0(t) \rightarrow f) - \Gamma(\bar{D}^0(t) \rightarrow f)}{\Gamma(D^0(t) \rightarrow f) + \Gamma(\bar{D}^0(t) \rightarrow f)}$$

- Non-vanishing  $A_{CP}$  requires two terms of amplitudes, with different weak phases and strong phases

$$A = A_1 e^{i\phi_1} e^{i\delta_1} + A_2 e^{i\phi_2} e^{i\delta_2}$$

$$A_{CP} \approx 2r \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)$$

$$r = \frac{|A_2|}{|A_1|} \ll 1$$

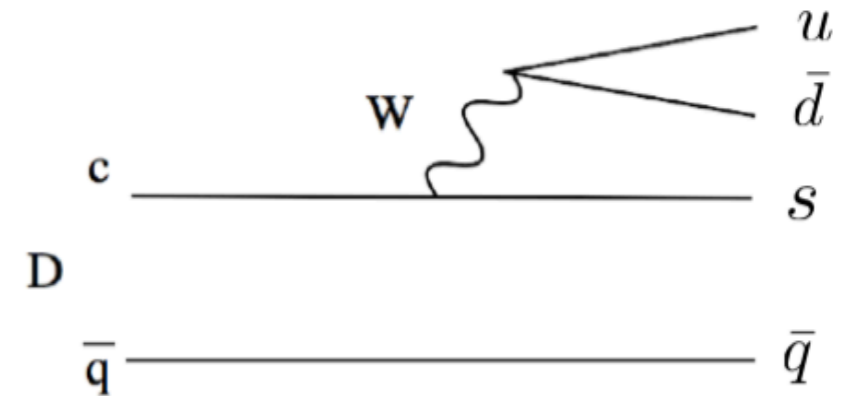
★ Can be classified by SM CKM suppression

★ Cabibbo-favored (CF) decay

- originates from  $c \rightarrow s u \bar{d}$
- examples:  $D^0 \rightarrow K^- \pi^+$

$$V_{cs} V_{ud}^*$$

$$\sim 1$$

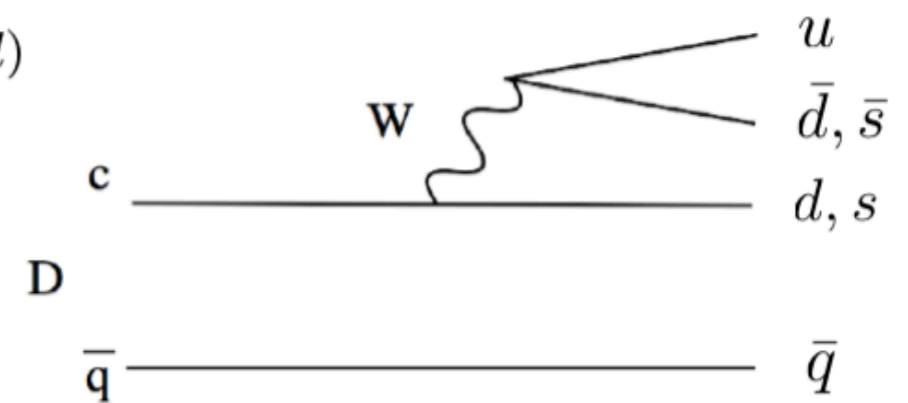


★ Singly Cabibbo-suppressed (SCS) decay

- originates from  $c \rightarrow q u \bar{q}$
- examples:  $D^0 \rightarrow \pi \pi$  and  $D^0 \rightarrow KK$

$$V_{cs(d)} V_{us(d)}^*$$

$$\sim \lambda$$

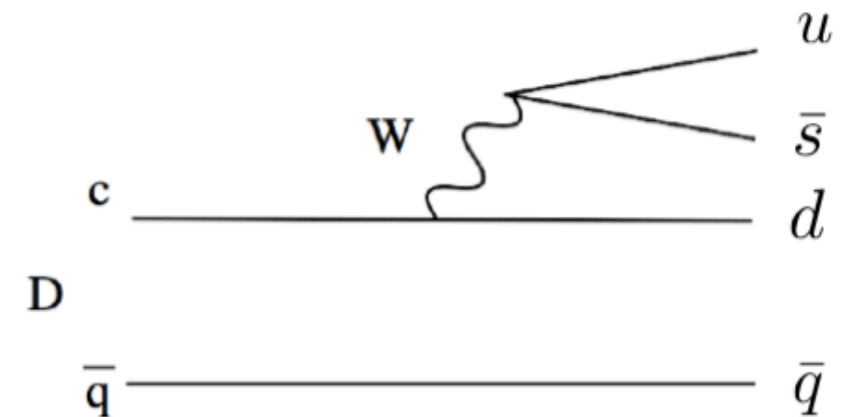


★ Doubly Cabibbo-suppressed (DCS) decay

- originates from  $c \rightarrow d u \bar{s}$
- examples:  $D^0 \rightarrow K^+ \pi^-$

$$V_{cd} V_{us}^*$$

$$\sim \lambda^2$$



$$\lambda = 0.225$$

# Outline

## 1. CPV in Cabibbo-suppressed processes

- $\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+K^-) - A_{CP}(D^0 \rightarrow \pi^+\pi^-)$

## 2. CPV in Cabibbo-favored D to neutral Kaons

# **1. CPV in Singly Cabibbo-Suppressed (SCS) modes**

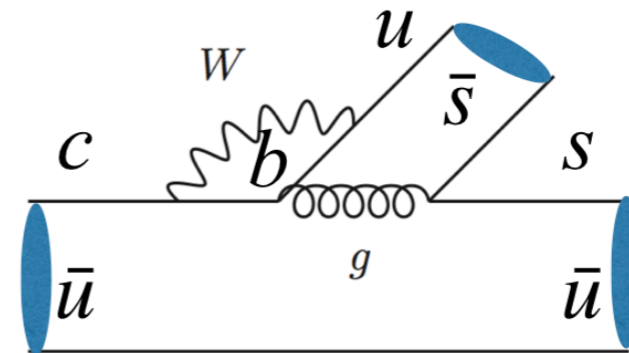
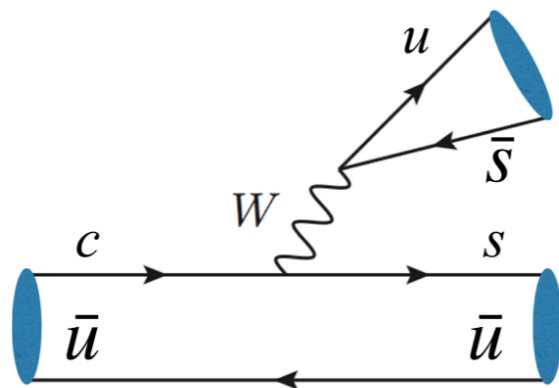
# Direct CPV in charm

## Scenario 1 : SCS

tree

v.s.

penguin



$$V_{cd}V_{ud}/V_{cs}V_{us}$$

$$V_{cb}V_{ub}$$

$$\lambda$$

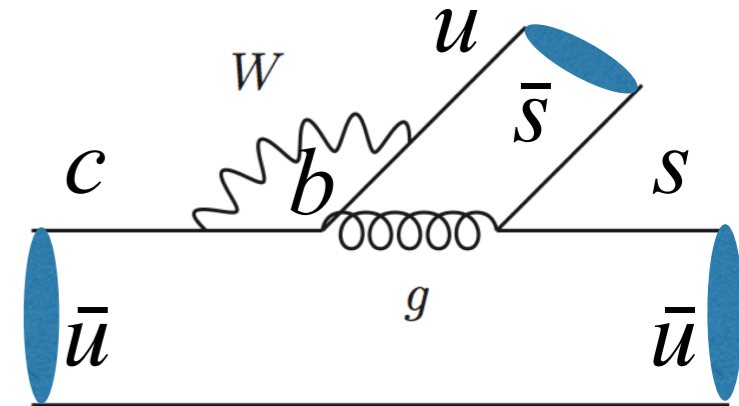
$$\lambda^5 + i\lambda^5$$

$$\Delta A_{CP} \equiv A_{CP}(K^- K^+) - A_{CP}(\pi^- \pi^+)$$

# CPV in SCS decays: tree *v.s.* penguin

## \* Ambiguity in penguins

- heavy quark expansion  $1/m_c$ ,  
 $m_c = 1.3\text{GeV}$ , converges slowly  
in exclusive decays



## ★ $\Delta A_{CP}(K^+K^-, \pi^+\pi^-)$ predicted from $10^{-4}$ to $10^{-2}$

Grossman, Kagan, Nir, '07; Bigi, Paul, '11; Isidori, Kamenik, Ligeti, Perez, '11;  
Brod, Grossmann, Kagan, Zupan, '11, '12; Feldmann, Nandi, Soni, '12;  
Bhattacharya, Gronau, Rosner, '12; Cheng, Chiang, '12; Li, Lu, **FSY**, '12;  
Franco, Mishima, Silvestrini, '12; Hiller, Jung, Schacht, '12.  
Khodjamirian, Petrov, 17.

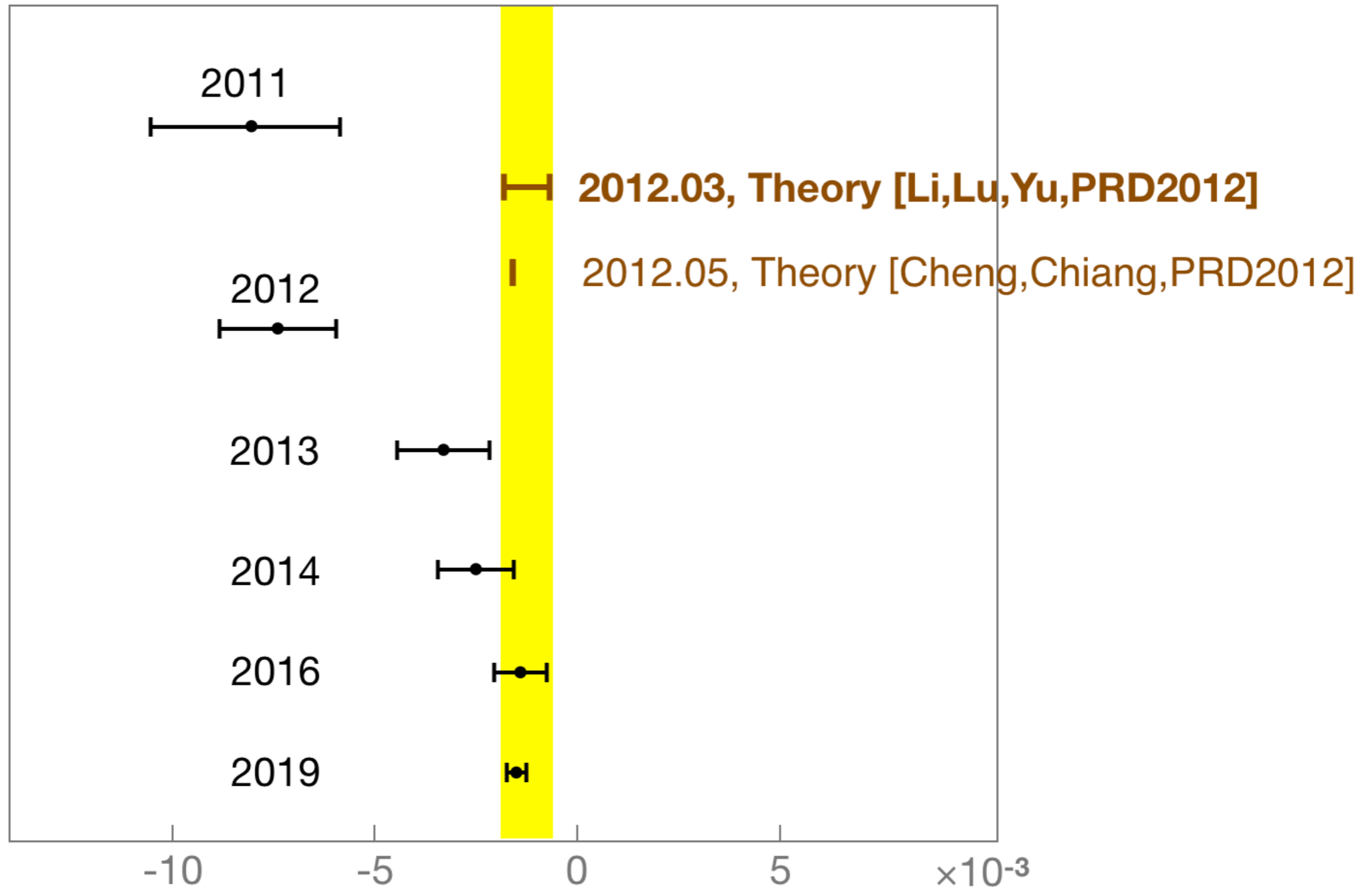
$$\text{Cheng, Chiang, '12 : } (-1.51 \pm 0.04) \times 10^{-3}$$

$$\text{Li, Lu, FSY, '12 : } (-0.6 \sim -1.9) \times 10^{-3}$$

# Measurements of $\Delta A_{CP}$

Measurements	$\Delta A_{CP}$	Publication	World Average
2011 LHCb ( $D^*$ )	$(-0.82 \pm 0.24)\%$	PRL108,111602	$(-0.74 \pm 0.15)\%$
2012 CDF	$(-0.62 \pm 0.23)\%$	PRL109,111801	
2012 Belle	$(-0.87 \pm 0.41)\%$	1212.1975	
2013 LHCb ( $D^*$ )	$(-0.34 \pm 0.18)\%$	LHCb- CONF-2013-03	$(-0.33 \pm 0.12)\%$
2013 LHCb (B)	$(+0.49 \pm 0.33)\%$	PLB723(2013)33	
2014 LHCb (B)	$(+0.14 \pm 0.18)\%$	JHEP07(2014)041	$(-0.25 \pm 0.10)\%$
2016 LHCb ( $D^*$ )	$(-0.10 \pm 0.09)\%$	PRL116,191601	$(-0.14 \pm 0.07)\%$
2019 LHCb(all)	$(-0.15 \pm 0.03)\%$	1903.08726	$(-0.16 \pm 0.03)\%$

# Exp Averages of $\Delta A_{CP}$





# Understanding charm CPV

$$\mathcal{A}(D^0 \rightarrow K^+ K^-) = \lambda_s \mathcal{T}^{KK} + \lambda_b \mathcal{P}^{KK},$$

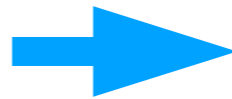
$$\mathcal{A}(D^0 \rightarrow \pi^+ \pi^-) = \lambda_d \mathcal{T}^{\pi\pi} + \lambda_b \mathcal{P}^{\pi\pi},$$

$$\Delta A_{CP} = -2r \sin \gamma \left( \frac{|\mathcal{P}^{KK}|}{|\mathcal{T}^{KK}|} \sin \delta^{KK} + \frac{|\mathcal{P}^{\pi\pi}|}{|\mathcal{T}^{\pi\pi}|} \sin \delta^{\pi\pi} \right) \quad r = |\lambda_b / \lambda_{d,s}|$$

$$2r \sin \gamma = 1.5 \times 10^{-3}$$
$$\Delta A_{CP} = (-1.54 \pm 0.29) \times 10^{-3} \quad \longrightarrow \quad \left( \frac{|\mathcal{P}^{KK}|}{|\mathcal{T}^{KK}|} \sin \delta^{KK} + \frac{|\mathcal{P}^{\pi\pi}|}{|\mathcal{T}^{\pi\pi}|} \sin \delta^{\pi\pi} \right) \approx 1$$

Li, Lu, **FSY**, PRD86,036012(2012); 1903.10638

$$\left( \frac{|\mathcal{P}^{KK}|}{|\mathcal{T}^{KK}|} \sin \delta^{KK} + \frac{|\mathcal{P}^{\pi\pi}|}{|\mathcal{T}^{\pi\pi}|} \sin \delta^{\pi\pi} \right) \approx 1$$



$$\frac{|\mathcal{P}|}{|\mathcal{T}|} \sin \delta \sim 1/2$$

## topological approach

Li, Lu, **FSY**, '12; Cheng, Chiang, '12

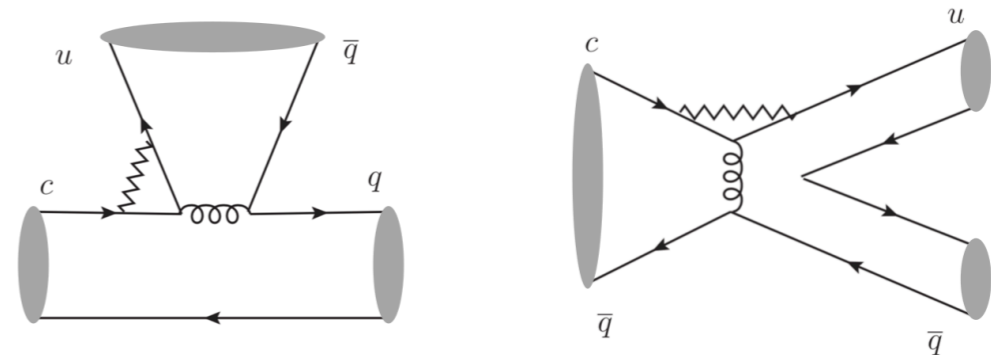
$$\frac{\mathcal{P}^{\pi\pi}}{\mathcal{T}^{\pi\pi}} = 0.66e^{i134^\circ}, \quad \text{and} \quad \frac{\mathcal{P}^{KK}}{\mathcal{T}^{KK}} = 0.45e^{i131^\circ}$$

$\Delta U = 0$  over  $\Delta U = 1$

Grossman, Schacht, '19

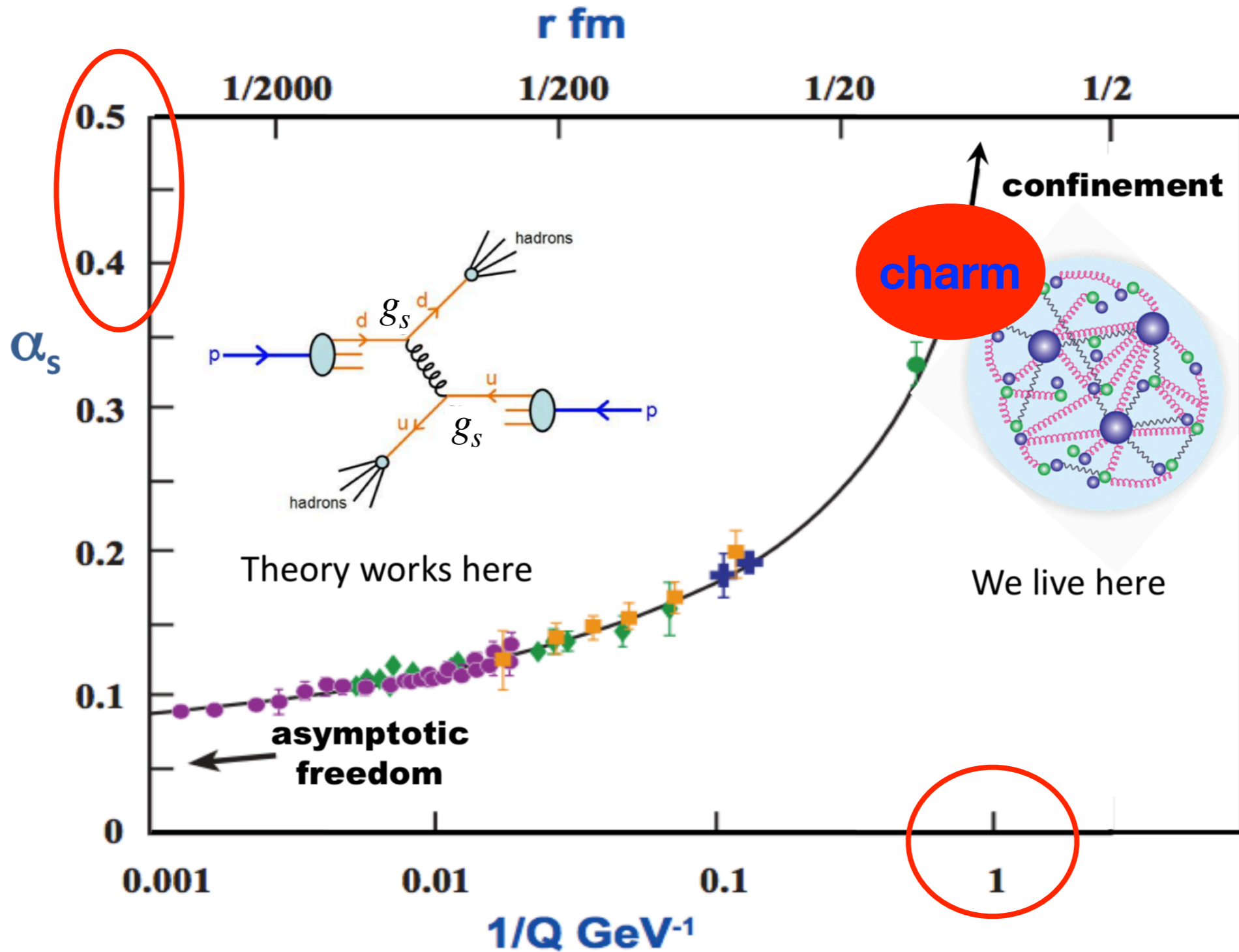
$$|\tilde{p}_0| \sin(\delta_{\text{strong}}) = 0.65 \pm 0.11$$

**Key:** Long-distance  
non-perturbative



**Understand:** tree  $\rightarrow$  penguin; **Branching ratio**  $\rightarrow$  **CPV**

# The QCD “dilemma”



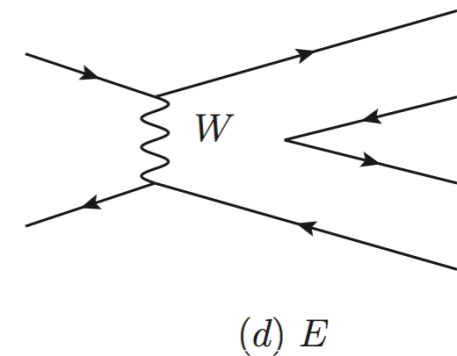
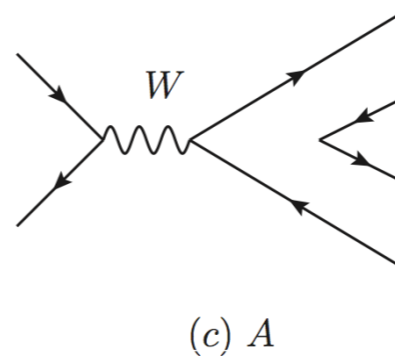
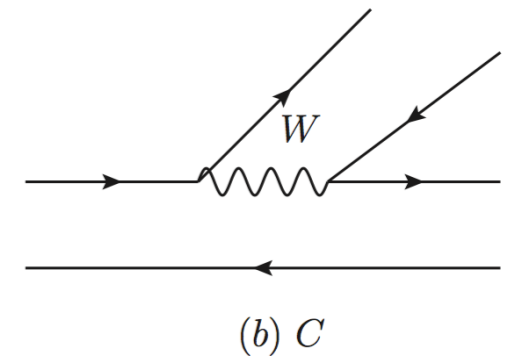
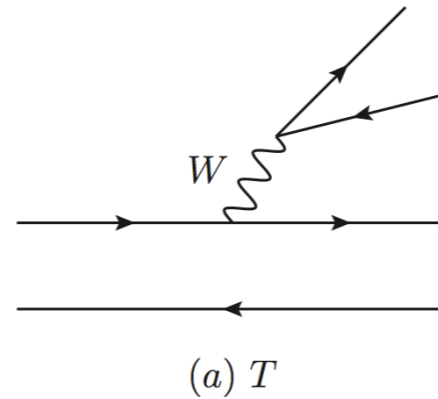
[S.Olsen's talk @ HIEPA2018]

# Topological Amplitudes

- According to the **weak flavour flows**

- **Including all strong interaction effects**

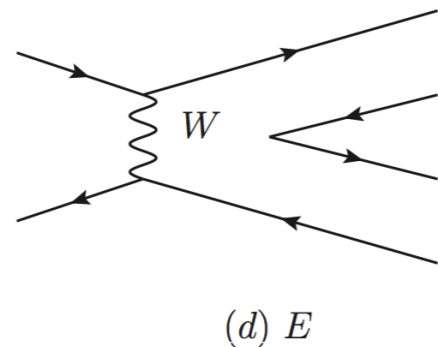
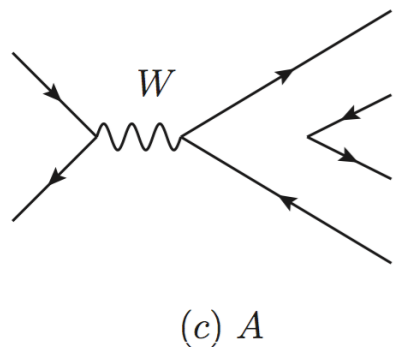
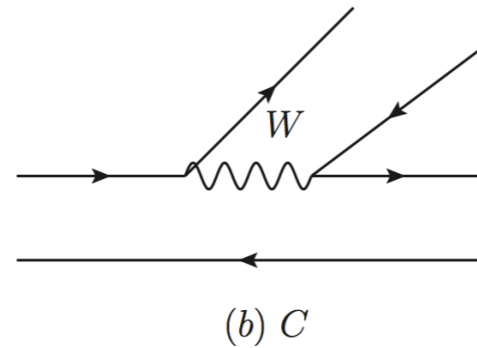
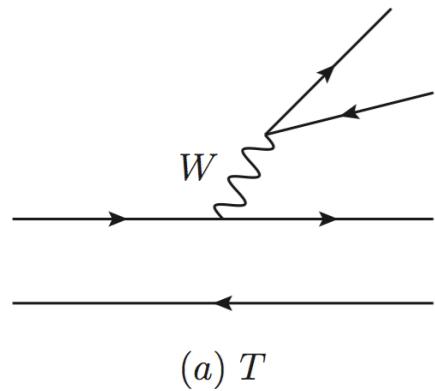
- **Amplitudes extracted from data**



Chau,86'; Chau,Cheng,87'; Bhattacharya, Rosner, 08'; Cheng, Chiang,10'

- Always in the flavour **SU(3) symmetry** limit, but **losing predictive power**

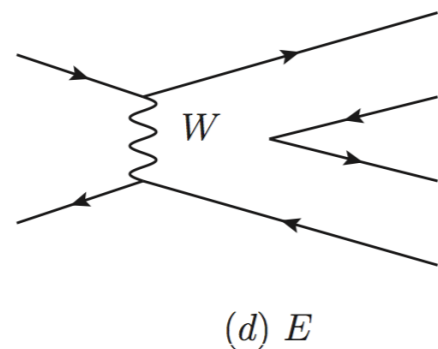
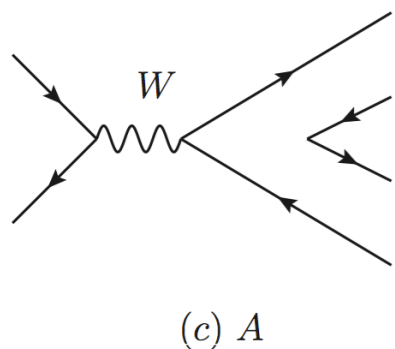
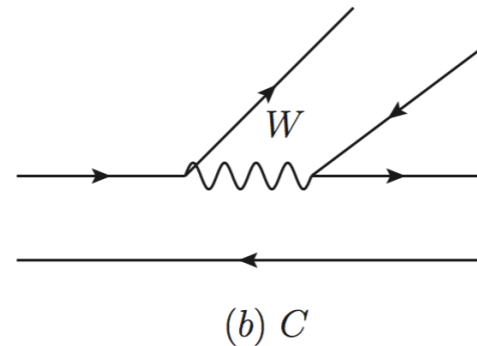
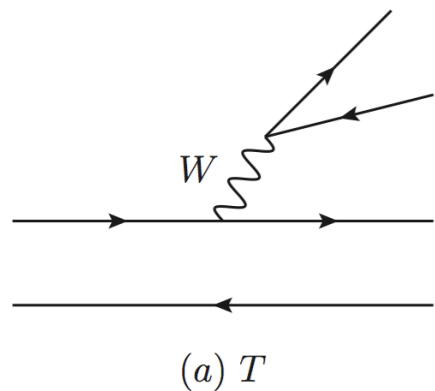
# Factorization-Assisted Topological-Amplitude Approach (FAT)



- Dynamics In factorization:
  - ▶ **Short-distance:**  
Wilson coefficients
  - ▶ **Long-distance:**  
hadronic matrix elements

Li, Lu, FSY, '12

# Factorization-Assisted Topological-Amplitude Approach (FAT)



- **Dynamics In factorization:**

- ▶ **Short-distance:**  
Wilson coefficients

- ▶ **Long-distance:**  
hadronic matrix elements

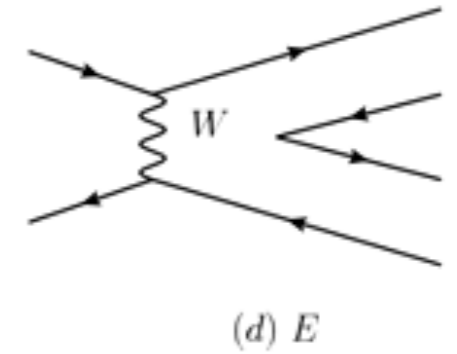
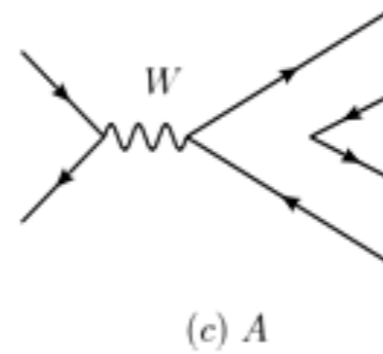
---

↓  
**Non-perturbative** quantities

↓  
Extracted from data

Li, Lu, **FSY**, '12

# W-annihilation (A) W-exchange (E)



$$\langle P_1 P_2 | \mathcal{H}_{\text{eff}} | D \rangle_{E,A} = \frac{G_F}{\sqrt{2}} V_{\text{CKM}} b_{q,s}^{E,A}(\mu) f_D m_D^2 \left( \frac{f_{P_1} f_{P_2}}{f_\pi^2} \right)$$

Li, Lu, FSY, '12

$$\begin{aligned} \mathbf{A}: b_{q,s}^A(\mu) &= C_1(\mu) \chi_{q,s}^A e^{i\phi_{q,s}^A} \\ \mathbf{E}: b_{q,s}^E(\mu) &= C_2(\mu) \chi_{q,s}^E e^{i\phi_{q,s}^E} \end{aligned}$$

**SU(3) breaking effects**

nonperturbative  
contributions

Modes	Br(exp)	Br(this work)	$A_{CP}^{SM} \times 10^{-3}$
$D^0 \rightarrow \pi^+ \pi^-$	$1.45 \pm 0.05$	1.43	0.58
$D^0 \rightarrow K^+ K^-$	$4.07 \pm 0.10$	4.19	-0.42
$D^0 \rightarrow K^0 \bar{K}^0$	$0.320 \pm 0.038$	0.36	1.38
$D^0 \rightarrow \pi^0 \pi^0$	$0.81 \pm 0.05$	0.57	0.05
$D^0 \rightarrow \pi^0 \eta$	$0.68 \pm 0.07$	0.94	-0.29
$D^0 \rightarrow \pi^0 \eta'$	$0.91 \pm 0.13$	0.65	1.53
$D^0 \rightarrow \eta \eta$	$1.67 \pm 0.18$	1.48	0.18
$D^0 \rightarrow \eta \eta'$	$1.05 \pm 0.26$	1.54	-0.94
$D^+ \rightarrow \pi^+ \pi^0$	$1.18 \pm 0.07$	0.89	0
$D^+ \rightarrow K^+ \bar{K}^0$	$6.12 \pm 0.22$	5.95	-0.93
$D^+ \rightarrow \pi^+ \eta$	$3.54 \pm 0.21$	3.39	-0.26
$D^+ \rightarrow \pi^+ \eta'$	$4.68 \pm 0.29$	4.58	1.18
$D_S^+ \rightarrow \pi^0 K^+$	$0.62 \pm 0.23$	0.67	0.39
$D_S^+ \rightarrow \pi^+ K^0$	$2.52 \pm 0.27$	2.21	0.84
$D_S^+ \rightarrow K^+ \eta$	$1.76 \pm 0.36$	1.00	0.70
$D_S^+ \rightarrow K^+ \eta'$	$1.8 \pm 0.5$	1.92	-1.60

**2. then  
predict  
charm CPV**

**1. Understand QCD dynamics @ 1GeV  
by Branching Ratios**

Li, Lu, FSU, '12

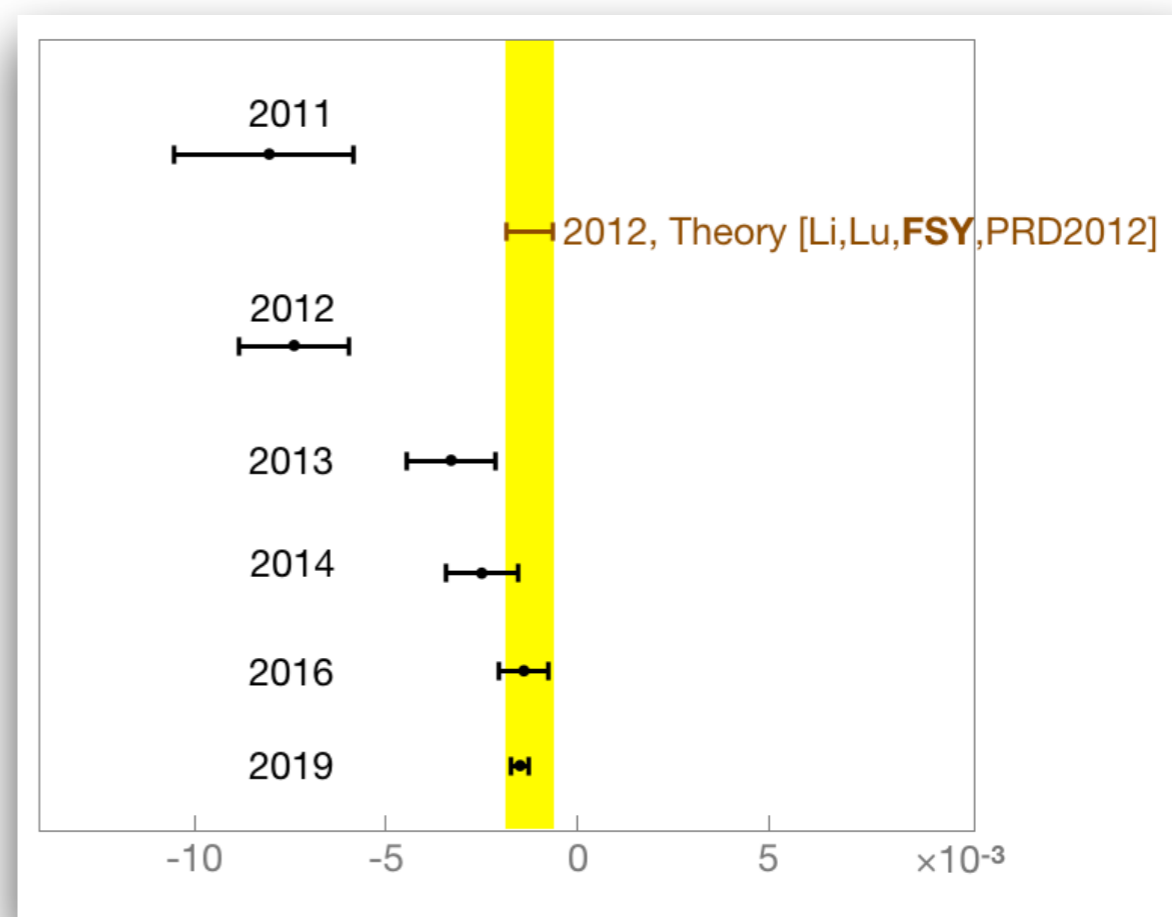


Modes	Br(exp)	Br(this work)	$A_{CP}^{SM} \times 10^{-3}$
$D^0 \rightarrow \pi^+ \pi^-$	$1.45 \pm 0.05$	1.43	0.58
$D^0 \rightarrow K^+ K^-$	$4.07 \pm 0.10$	4.19	-0.42

$\Delta A_{CP}^{SM} = -1 \times 10^{-3}$

**1. Understand QCD dynamics @ 1GeV by Branching Ratios**

**2. Then predict charm CPV**



**Factorization-Assisted Topological approach**

Modes	Br(exp)	Br(this work)	$A_{CP}^{SM} \times 10^{-3}$
$D^0 \rightarrow \pi^+ \pi^-$	$1.45 \pm 0.05$	1.43	0.58
$D^0 \rightarrow K^+ K^-$	$4.07 \pm 0.10$	4.19	-0.42
$D^0 \rightarrow K^0 \bar{K}^0$	$0.320 \pm 0.038$	0.36	1.38
$D^0 \rightarrow \pi^0 \pi^0$	$0.81 \pm 0.05$	0.57	0.05
$D^0 \rightarrow \pi^0 \eta$	$0.68 \pm 0.07$	0.94	-0.29
$D^0 \rightarrow \pi^0 \eta'$	$0.91 \pm 0.13$	0.65	1.53
$D^0 \rightarrow \eta \eta$	$1.67 \pm 0.18$	1.48	0.18
$D^0 \rightarrow \eta \eta'$	$1.05 \pm 0.26$	1.54	-0.94
$D^+ \rightarrow \pi^+ \pi^0$	$1.18 \pm 0.07$	0.89	0
$D^+ \rightarrow K^+ \bar{K}^0$	$6.12 \pm 0.22$	5.95	-0.93
$D^+ \rightarrow \pi^+ \eta$	$3.54 \pm 0.21$	3.39	-0.26
$D^+ \rightarrow \pi^+ \eta'$	$4.68 \pm 0.29$	4.58	1.18
$D_S^+ \rightarrow \pi^0 K^+$	$0.62 \pm 0.23$	0.67	0.39
$D_S^+ \rightarrow \pi^+ K^0$	$2.52 \pm 0.27$	2.21	0.84
$D_S^+ \rightarrow K^+ \eta$	$1.76 \pm 0.36$	1.00	0.70
$D_S^+ \rightarrow K^+ \eta'$	$1.8 \pm 0.5$	1.92	-1.60

**Factorization-Assisted Topological approach**

# Implications of LHCb2019

1903.08726

$$\begin{aligned}\Delta A_{CP} &= A_{CP}(D^0 \rightarrow K^+K^-) - A_{CP}(D^0 \rightarrow \pi^+\pi^-) \\ &= (-1.54 \pm 0.29) \times 10^{-3}\end{aligned}$$



**1. Charm CPV**  
of order  **$10^{-3}$**

**2. Precision**  
of order  **$10^{-4}$**

# Implication: What next potential to observe charm CPV?

1. Charm CPV of order  $10^{-3}$

2. Precision of order  $10^{-4}$



1) Large branching fractions

2) Fully charged final particles

@LHCb

3) Large production

$$Br(D^+ \rightarrow K^+ K^- \pi^+) = 9.5 \times 10^{-3}$$

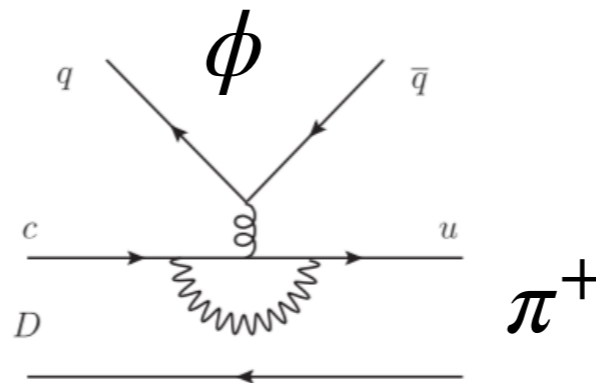
Compared to  $Br(D^0 \rightarrow \pi^+ \pi^-) = 1.4 \times 10^{-3}$

which dominates error of

# What is the next potential mode to observe charm CPV?

$$Br(D^+ \rightarrow K^+ K^- \pi^+) = 9.5 \times 10^{-3}$$

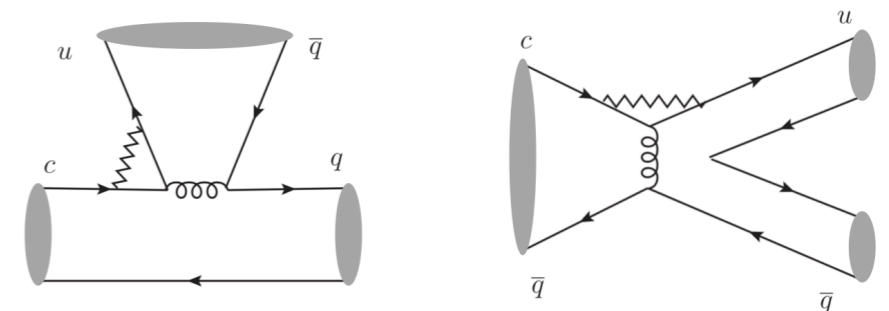
$$A_{CP}(D^+ \rightarrow \pi^+ \phi) = 10^{-7}$$



Qin, Li, Lu, **FSY**, '14

$$A_{CP}(D^+ \rightarrow K^+ \bar{K}^{*0}) = 0.2 \times 10^{-3}$$

$$A_{CP}(D^+ \rightarrow K^+ \bar{K}_0^{*0}(1430)) = -0.88 \times 10^{-3}$$

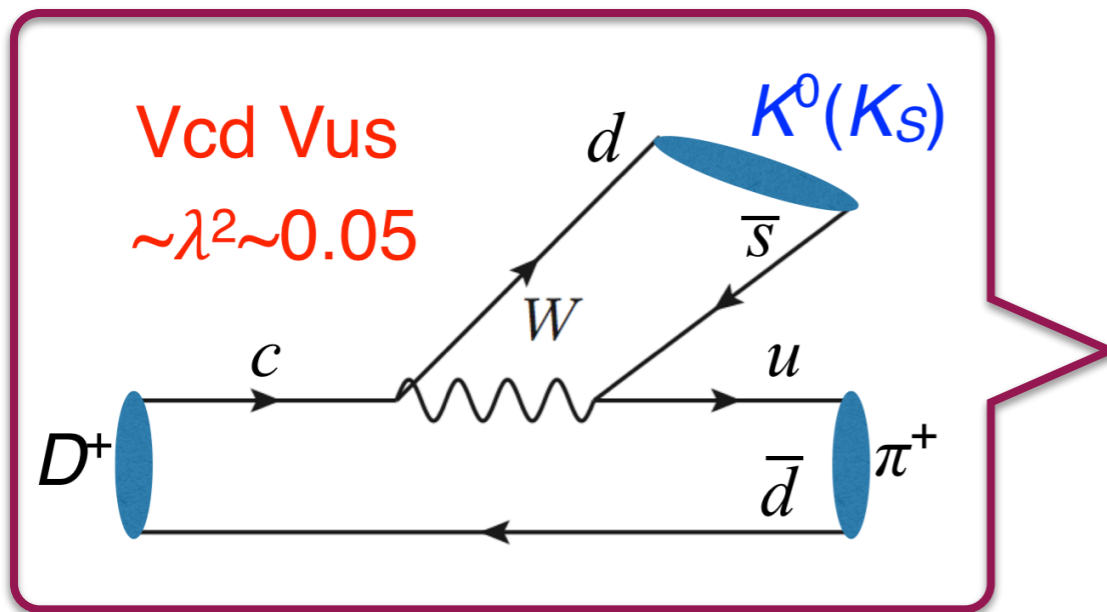
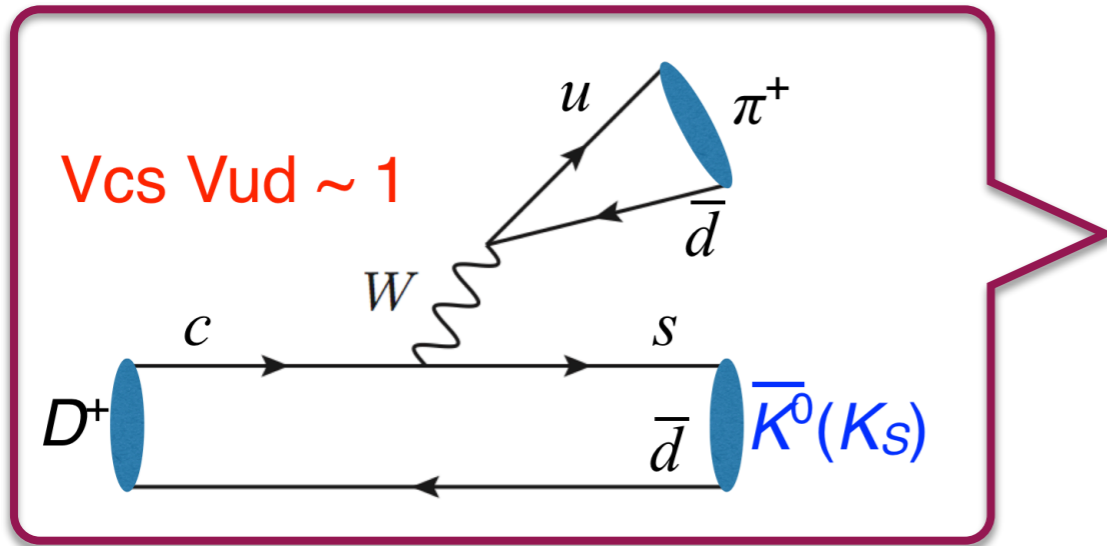


Li, Lu, **FSY**, 1903.10638

**2. CPV in  
Cabibbo-Favored (CF)  
and  
Doubly Cabibbo-Suppressed (DCS)  
modes**

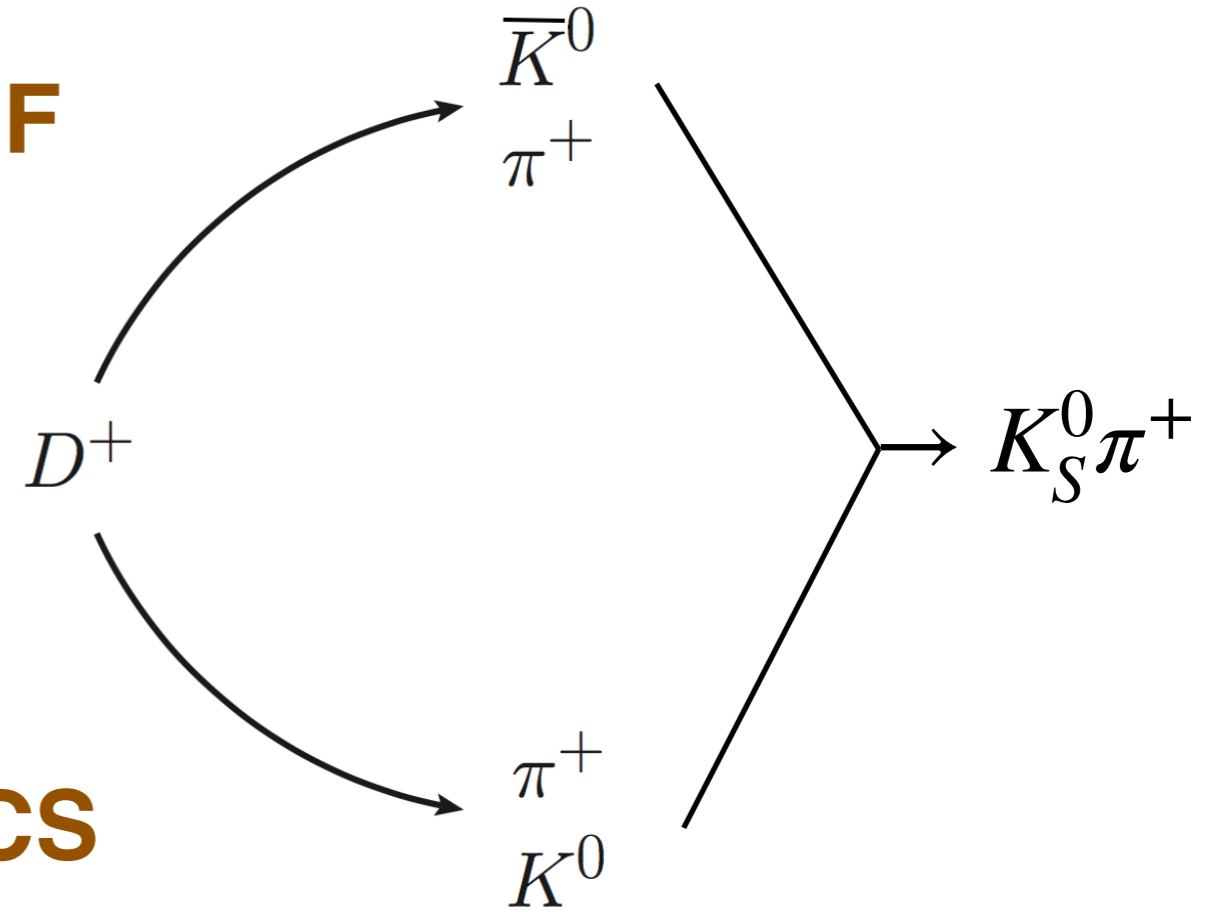
**Precision  $\rightarrow 10^{-4}$  ?**

## 2. CPV in $D \rightarrow f K_S$



**CF**

**DCS**



$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 - \lambda^4/8 & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) + A\lambda^5(\bar{\rho} - i\bar{\eta})/2 \\ -\lambda + A^2\lambda^5[1 - 2(\bar{\rho} + i\bar{\eta})]/2 & 1 - \lambda^2/2 - \lambda^4(1 + 4A^2)/8 & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 + A\lambda^4[1 - 2(\bar{\rho} + i\bar{\eta})]/2 & 1 - A^2\lambda^4/2 \end{pmatrix}$$

# New Physics in $D \rightarrow f K_S^0$

$$A_{CP}^{dir} \sim 2r_f \sin \phi \sin \delta_f$$

SM:  $\phi = \mathcal{O}(10^{-4})$

NP:  $\phi = \mathcal{O}(1)$

**Search for new physics at tree-level**



**Postulated in literature:**  
**deducting kaon mixing,**  
**data reveal direct CPV in charm**

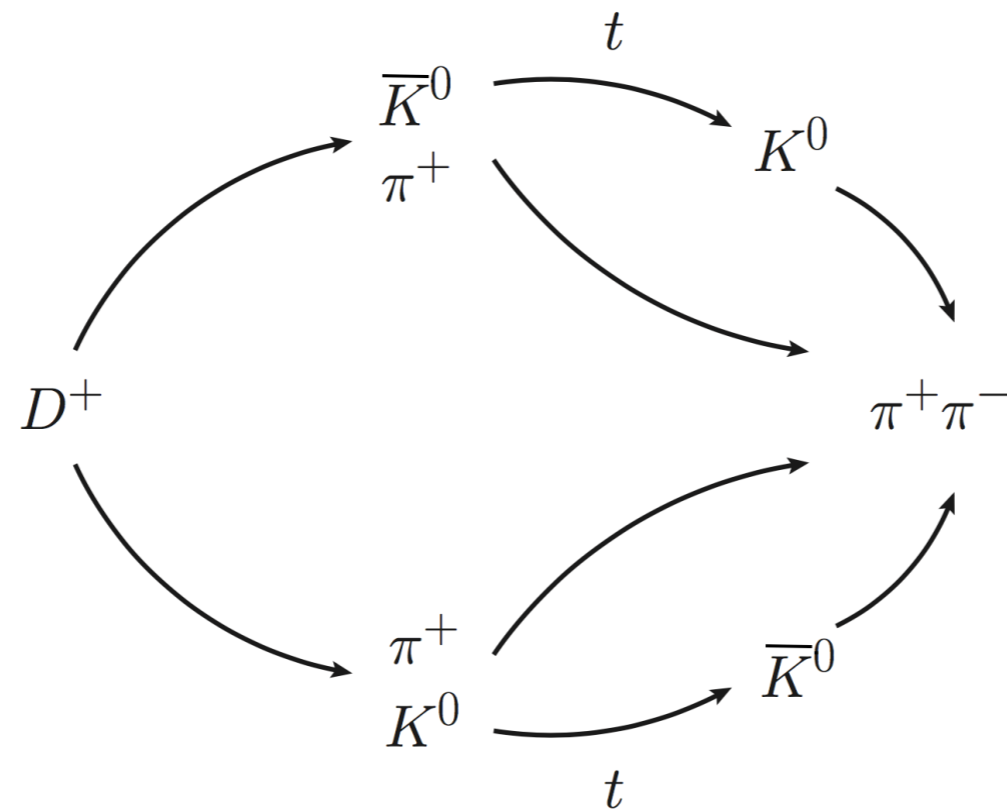
$$\begin{aligned} A_{CP}^{D^+ \rightarrow K_S^0 \pi^+} &\equiv \frac{\Gamma(D^+ \rightarrow K_S^0 \pi^+) - \Gamma(D^- \rightarrow K_S^0 \pi^-)}{\Gamma(D^+ \rightarrow K_S^0 \pi^+) + \Gamma(D^- \rightarrow K_S^0 \pi^-)} \\ &= A_{CP}^{\Delta C} + A_{CP}^{\bar{K}^0} \end{aligned}$$

Lipkin, Xing, '95; D'Ambrosio, Gao, '01; Bianco, Fabbri,  
Benson, Bigi, '03; Grossman, Nir, '12; Belle, '12

However...

# Full decay chain

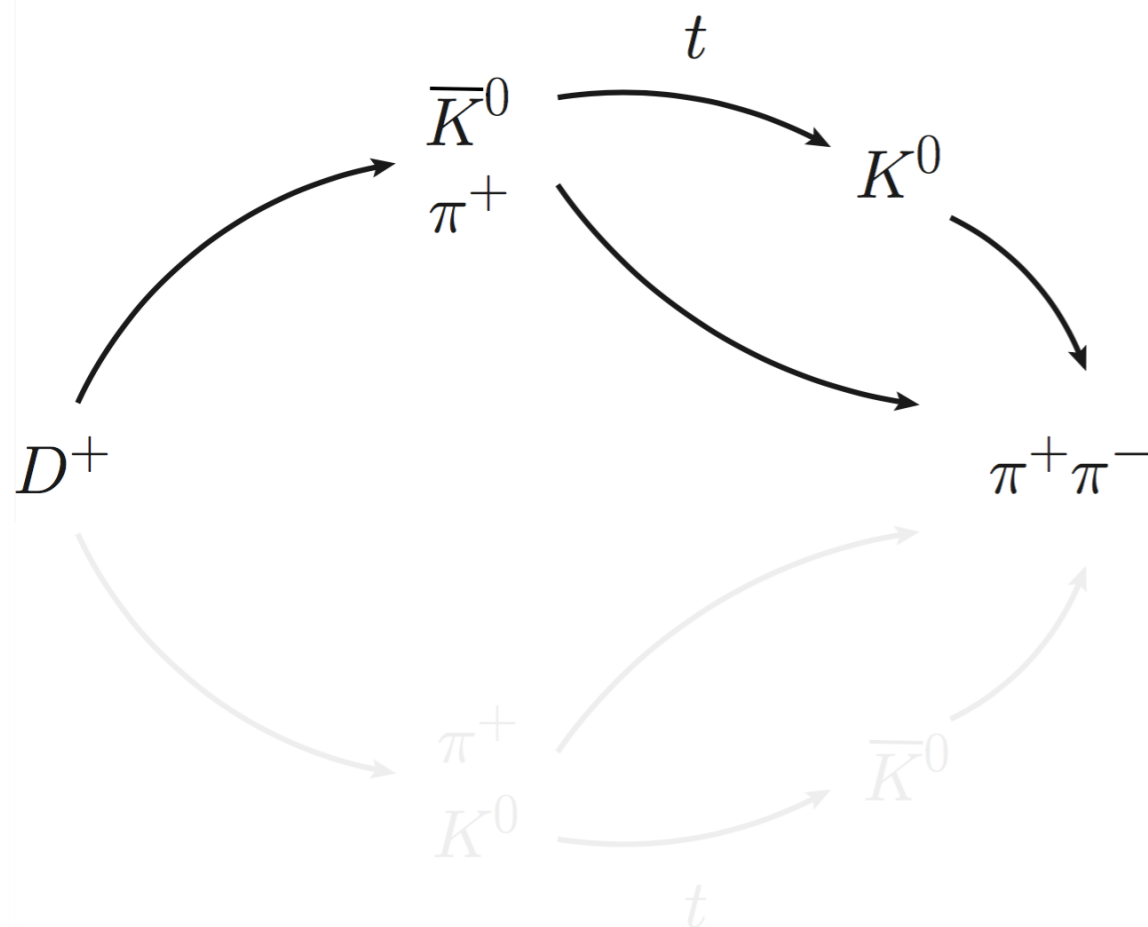
$$D^+ \rightarrow \pi^+ K(t) (\rightarrow \pi^+ \pi^-)$$



$$A_{CP}(t) = A_{CP}^{\bar{K}^0}(t) + A_{CP}^{\text{dir}}(t)$$

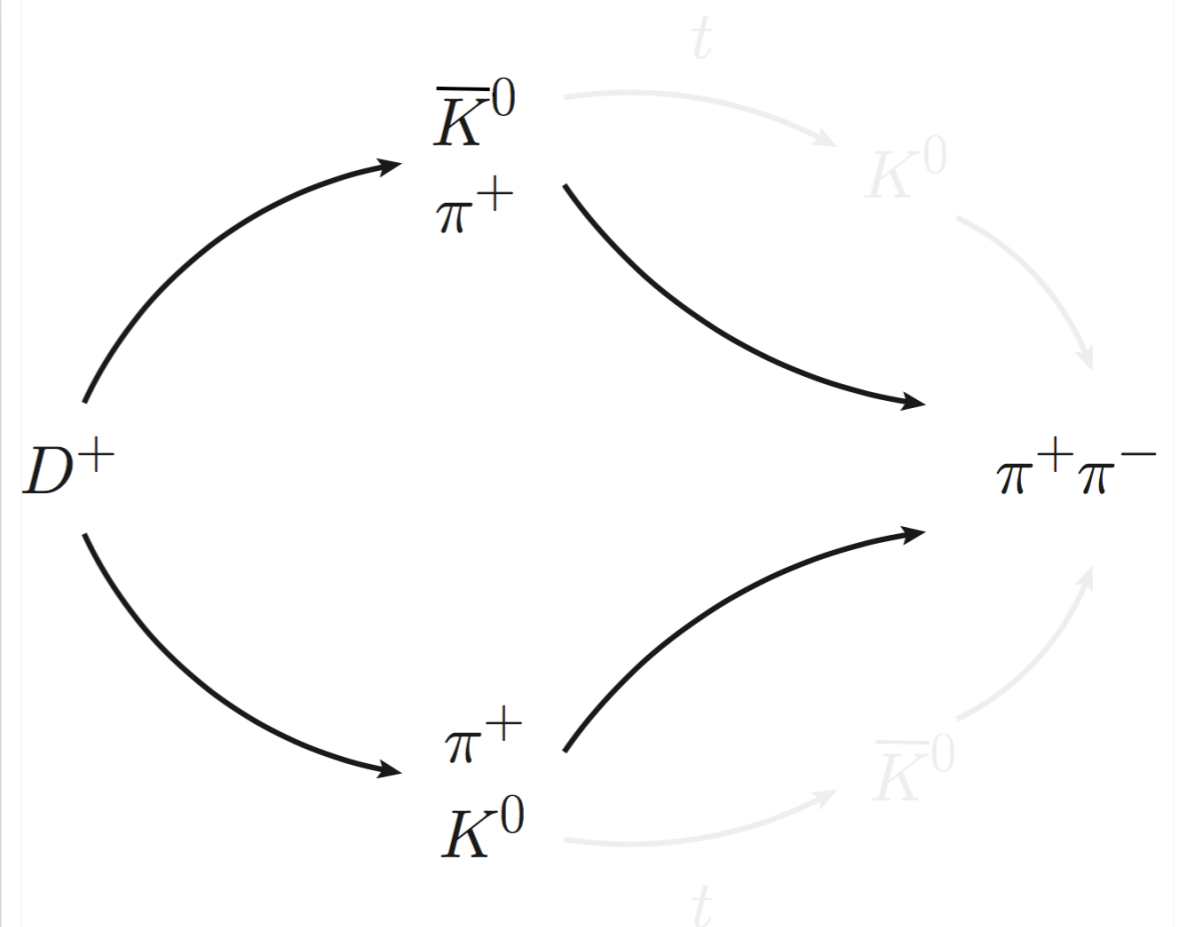
## Indirect CPV in kaon mixing

$$\text{Re}(\epsilon) = 10^{-3}$$



## Direct CPV in charm decays

$$\text{Im}(V_{cd}V_{us}/V_{cs}V_{ud}) = \lambda^6 = 10^{-5}$$

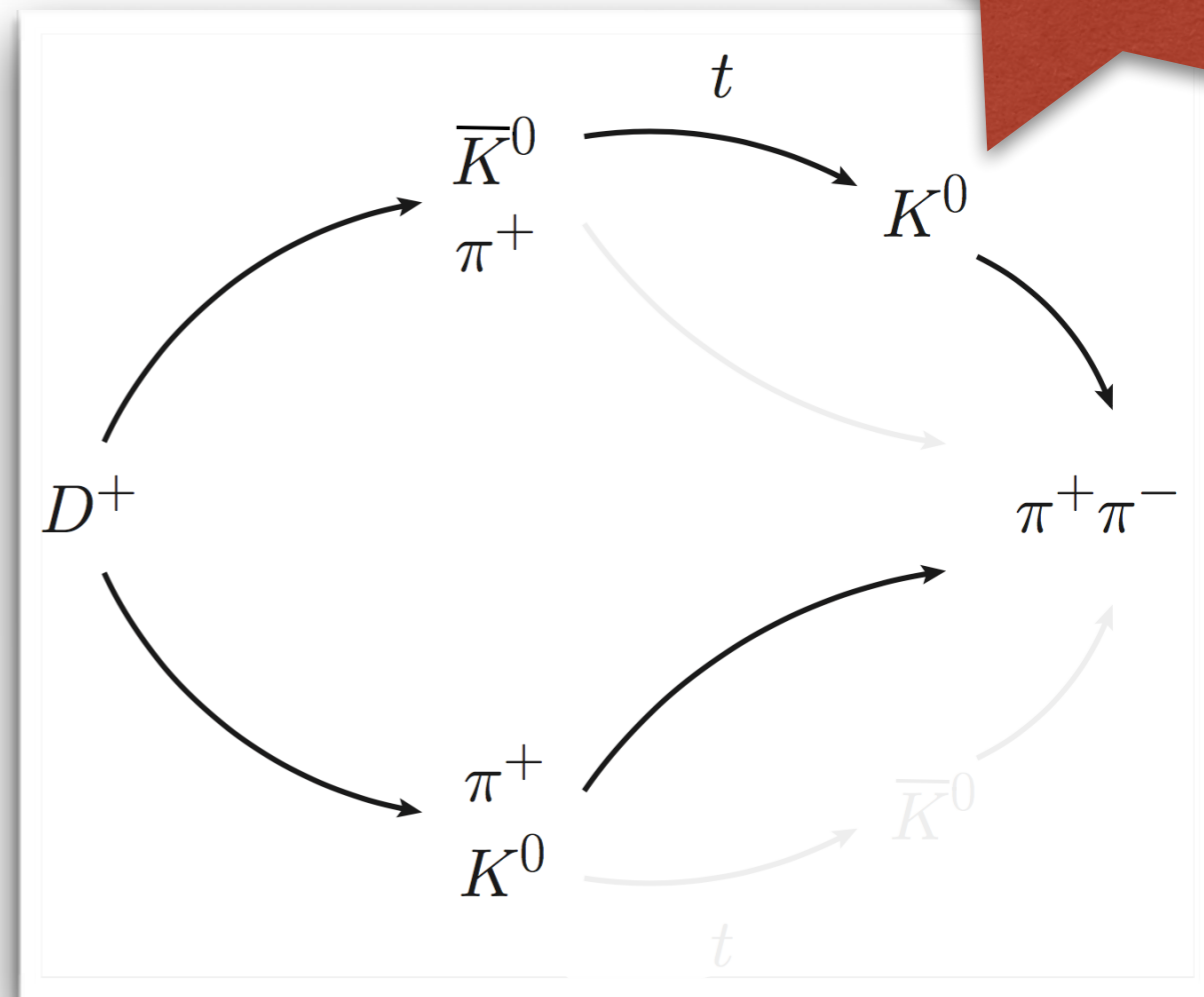
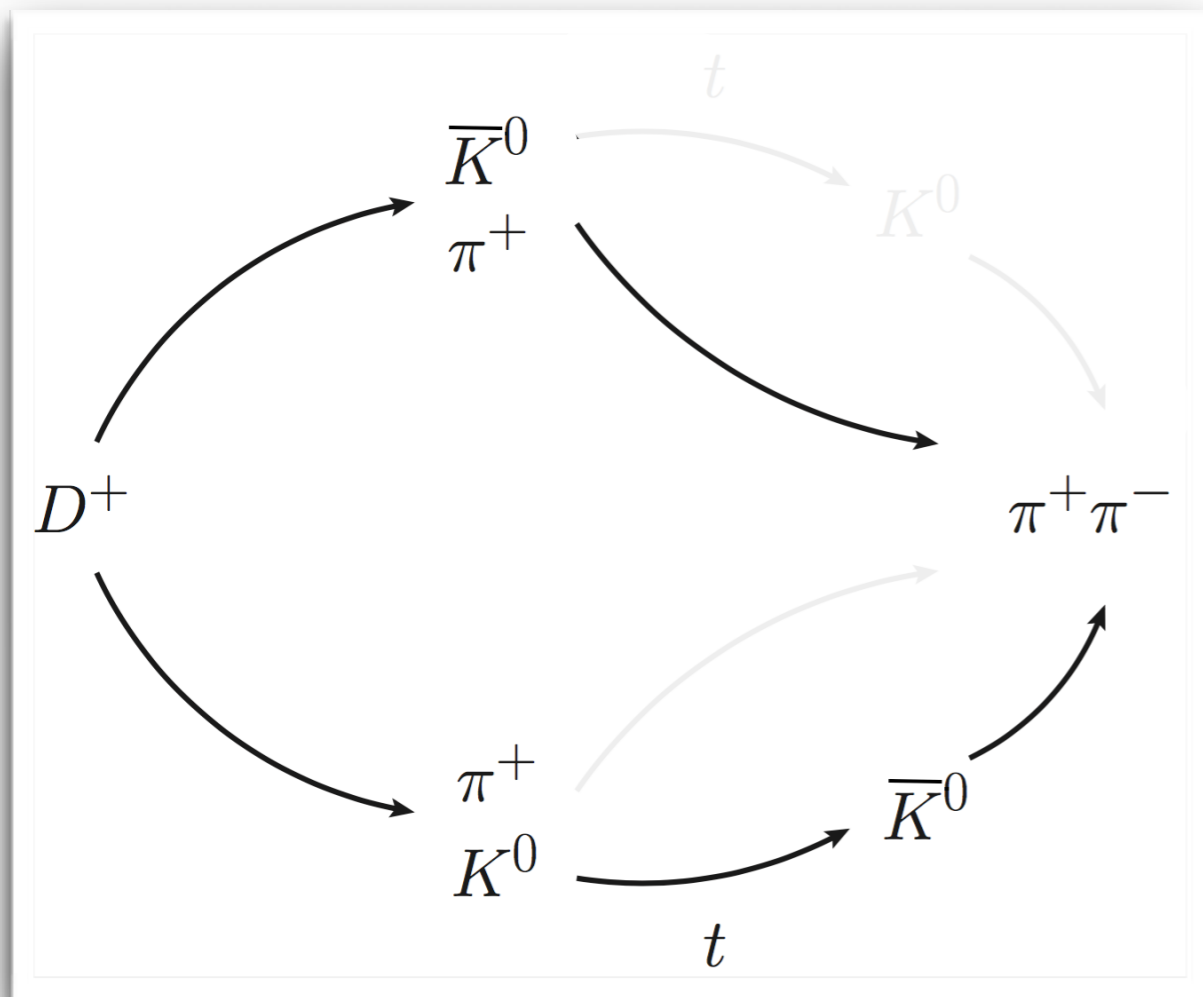


$$A_{CP}(t) = A_{CP}^{\bar{K}^0}(t) + A_{CP}^{\text{dir}}(t) + A_{CP}^{\text{int}}(t)$$

## CPV induced by mother decay and daughter mixing

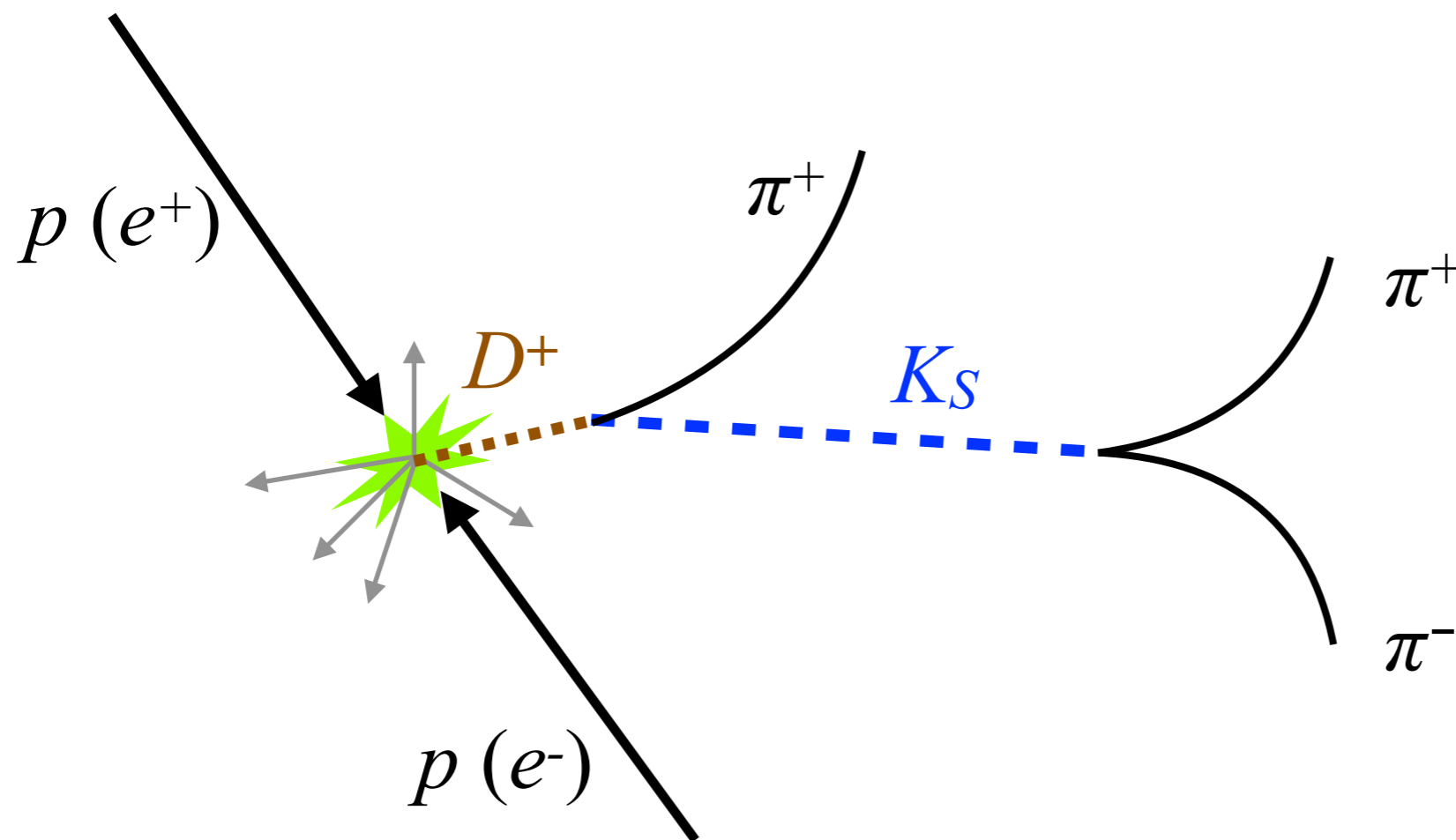
$$\text{Im}(\epsilon) \text{Re}(V_{cd}^* V_{us} / V_{cs}^* V_{ud}) = 10^{-4} \sim -3$$

NEW

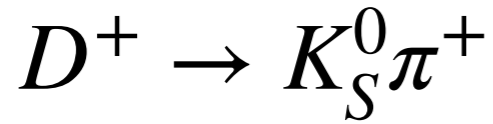


# Time-dependent & Time integrated CPV

time of  $K_S$  flying

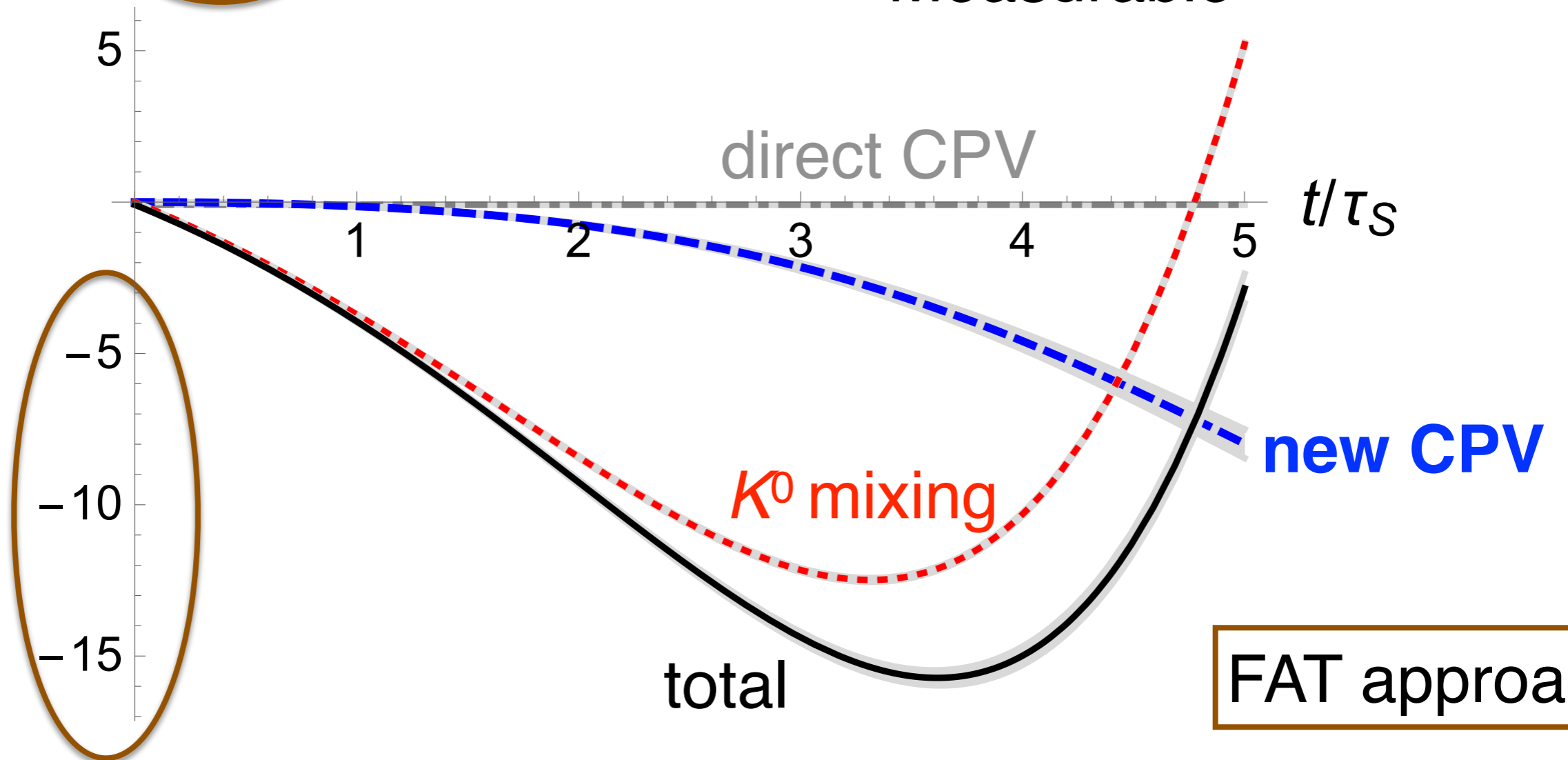


$$A_{CP}^{\bar{K}^0}(t) > A_{CP}^{\text{int}}(t) > A_{CP}^{\text{dir}}(t)$$



$A_{CP}(t) [\times 10^{-3}]$

Non-negligible  
Measurable

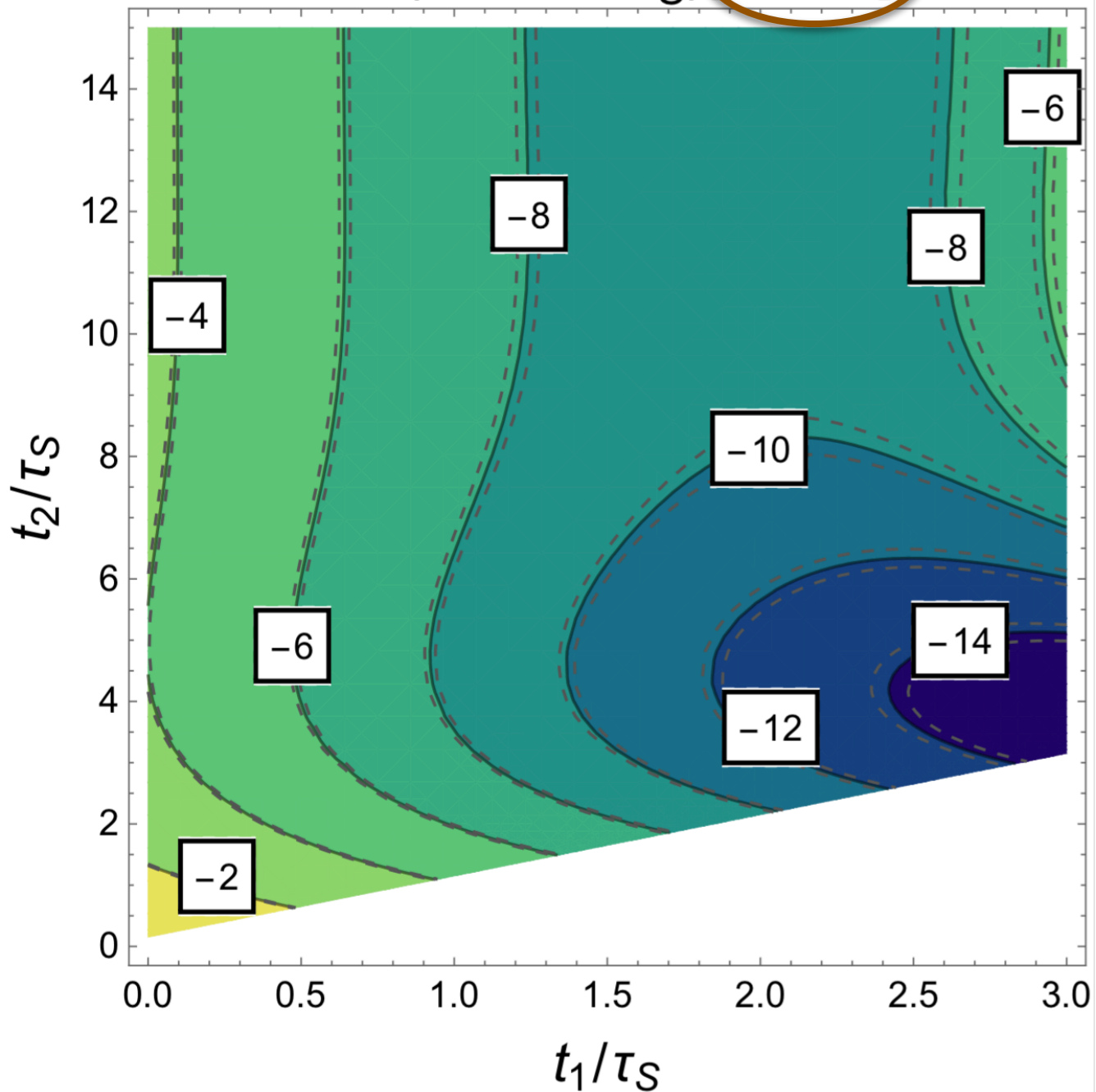


$A_{CP}^{\text{tot}}$ 
  $A_{CP}^{\bar{K}^0}$ 
  $A_{CP}^{\text{dir}}$ 
  $A_{CP}^{\text{new}}$

# Time-Integrated CPV

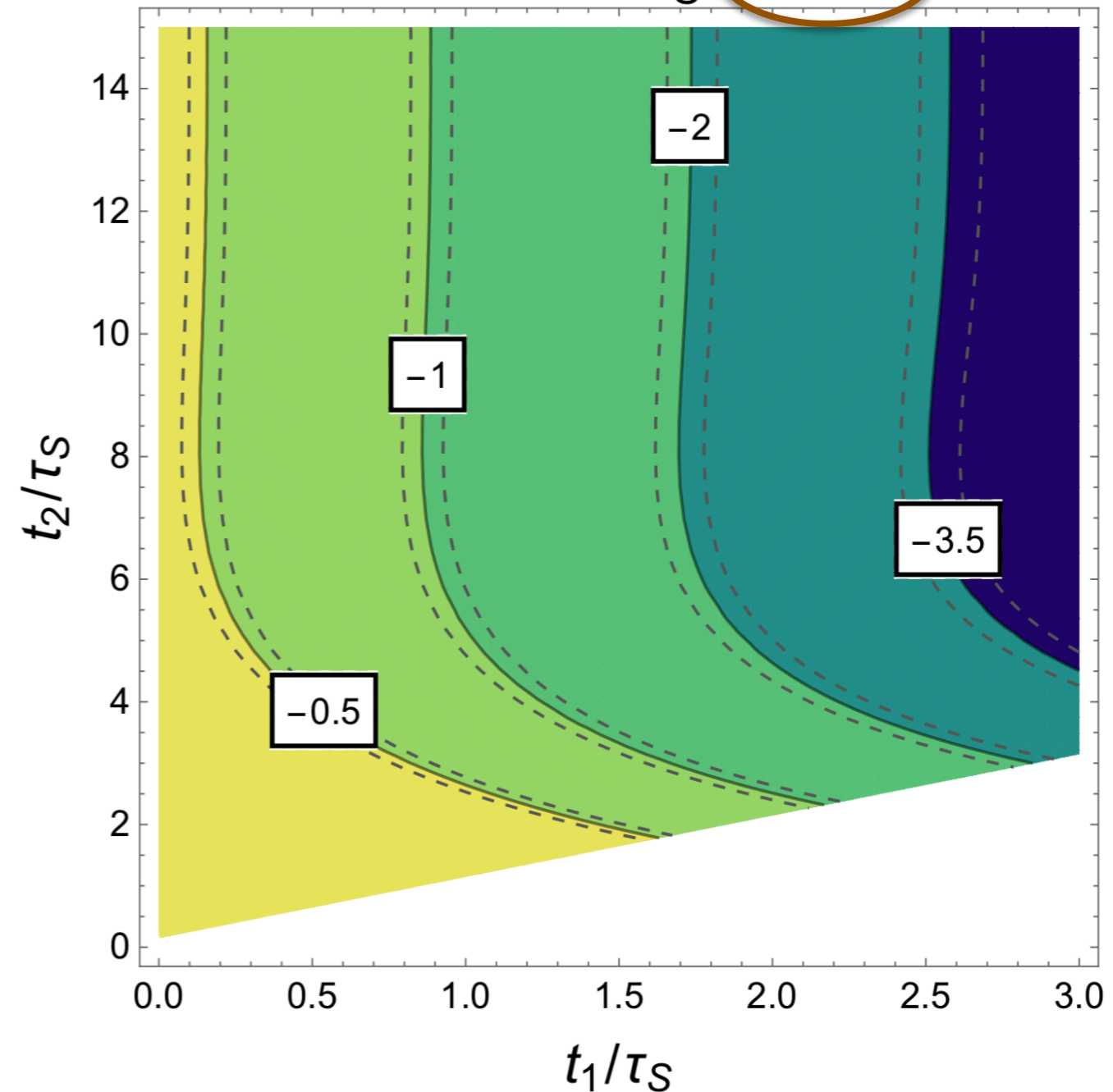
total

$$A_{CP}(D^+ \rightarrow \pi^+ K_S^0) [\times 10^{-3}]$$



Interference

$$A_{CP}^{\text{int}}(D^+ \rightarrow \pi^+ K_S^0) [\times 10^{-3}]$$



# Belle: Evidence for CP Violation in the Decay $D^+ \rightarrow K_S^0 \pi^+$

PRL109,021601(2012) [arXiv:1203.6409]

$$\begin{aligned} A_{CP}^{D^+ \rightarrow K_S^0 \pi^+} &\equiv \frac{\Gamma(D^+ \rightarrow K_S^0 \pi^+) - \Gamma(D^- \rightarrow K_S^0 \pi^-)}{\Gamma(D^+ \rightarrow K_S^0 \pi^+) + \Gamma(D^- \rightarrow K_S^0 \pi^-)} \\ &= A_{CP}^{\Delta C} + A_{CP}^{\bar{K}^0}, \end{aligned} \quad (1)$$

$$A_{CP}^{D^+ \rightarrow K_S^0 \pi^+} = (-0.363 \pm 0.094 \pm 0.067)\% \quad \text{Belle}$$

$$A_{CP}^{\bar{K}^0} = (-0.339 \pm 0.007)\%$$

$$A_{CP}^{\Delta C} = (-0.024 \pm 0.115)\%$$

Belle



# Belle: Evidence for CP Violation in the Decay $D^+ \rightarrow K_S^0 \pi^+$

PRL109,021601(2012) [arXiv:1203.6409]

$$A_{CP}^{D^+ \rightarrow K_S^0 \pi^+} \equiv \frac{\Gamma(D^+ \rightarrow K_S^0 \pi^+) - \Gamma(D^- \rightarrow K_S^0 \pi^-)}{\Gamma(D^+ \rightarrow K_S^0 \pi^+) + \Gamma(D^- \rightarrow K_S^0 \pi^-)}$$
$$= A_{CP}^{\Delta C} + A_{CP}^{\bar{K}^0} + A_{CP}^{int}$$

$$A_{CP}^{D^+ \rightarrow K_S^0 \pi^+} = (-0.363 \pm 0.094 \pm 0.067)\% \quad \text{Belle}$$

$$A_{CP}^{\bar{K}^0} = (-0.339 \pm 0.007)\%$$

$$A_{CP}^{\Delta C} = (-0.024 \pm 0.115)\%$$

Belle

$$A^{\Delta C} = (-0.006 \pm 0.115)\%$$

[Wang, FSY, Li, '17]

$$\Delta A_{CP} = A_{CP}(D^+ \rightarrow \pi^+ K_S^0) - A_{CP}(D_s^+ \rightarrow K^+ K_S^0)$$

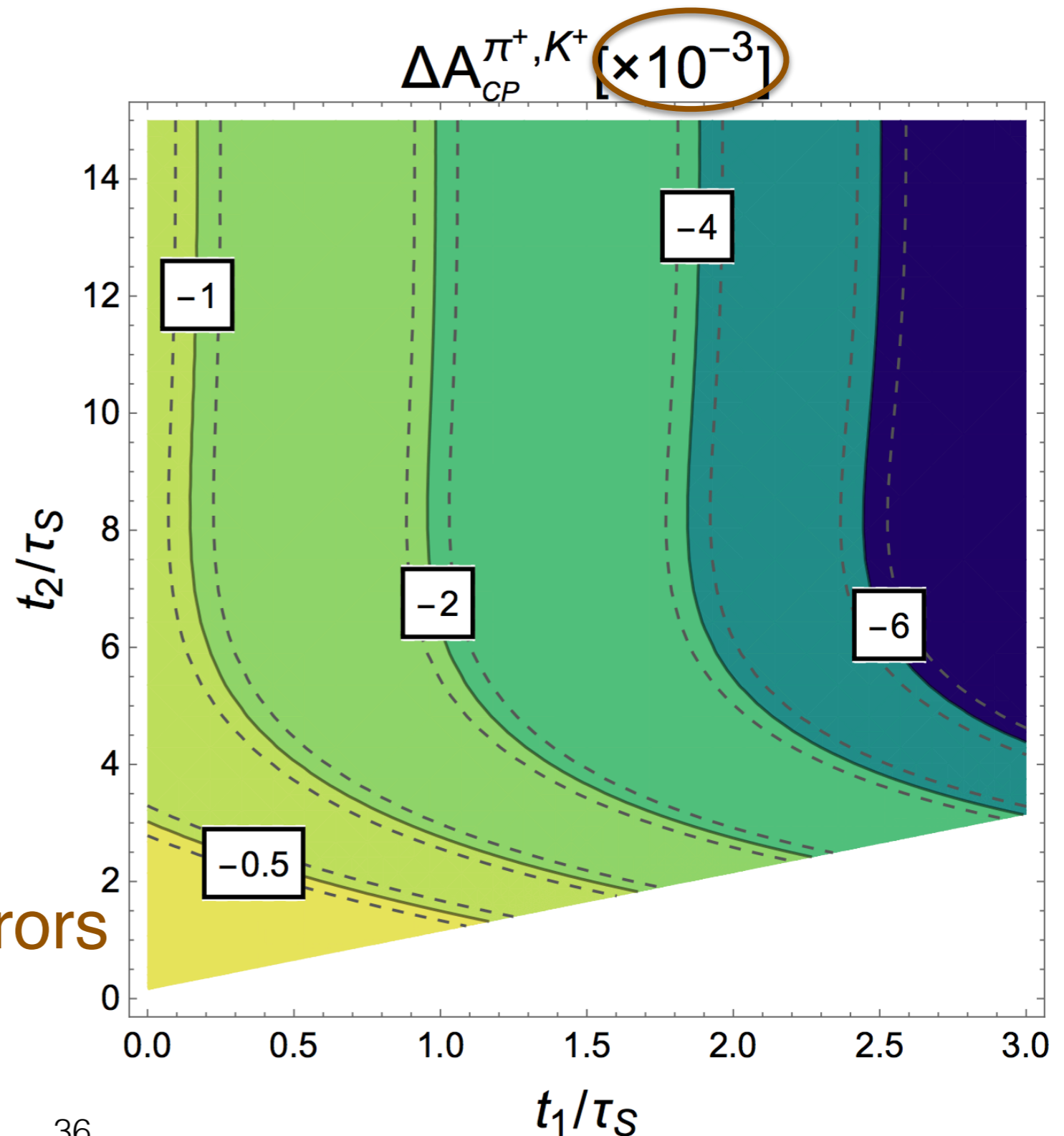
# New Observable

revealing  
new CPV effect

$$A_{CP}(t) \simeq \left[ \cancel{A_{CP}^{\bar{K}^0}(t)} + \cancel{A_{CP}^{dir}(t)} + A_{CP}^{int}(t) \right]$$

Cancel some systematic errors  
@ LHCb & Belle-II

[Wang, FSY, Li, '17]



# New CPV @ Ultimate Precision

**LHCb:**  $\Delta a_{CP} = (-15.4 \pm 2.9) \times 10^{-4}$  @ 9 fb<sup>-1</sup>

CF mode	Yield	SCS mode	Yield
$D^+ \rightarrow K_S \pi^+$	$4.8 \times 10^6$	$D^0 \rightarrow K^+ K^-$	$7.7 \times 10^6$
$D_s^+ \rightarrow K_S K^+$	$1.5 \times 10^6$	$D^0 \rightarrow \pi^+ \pi^-$	$2.5 \times 10^6$

[1406.2624]

LHCb @ 3 fb<sup>-1</sup>

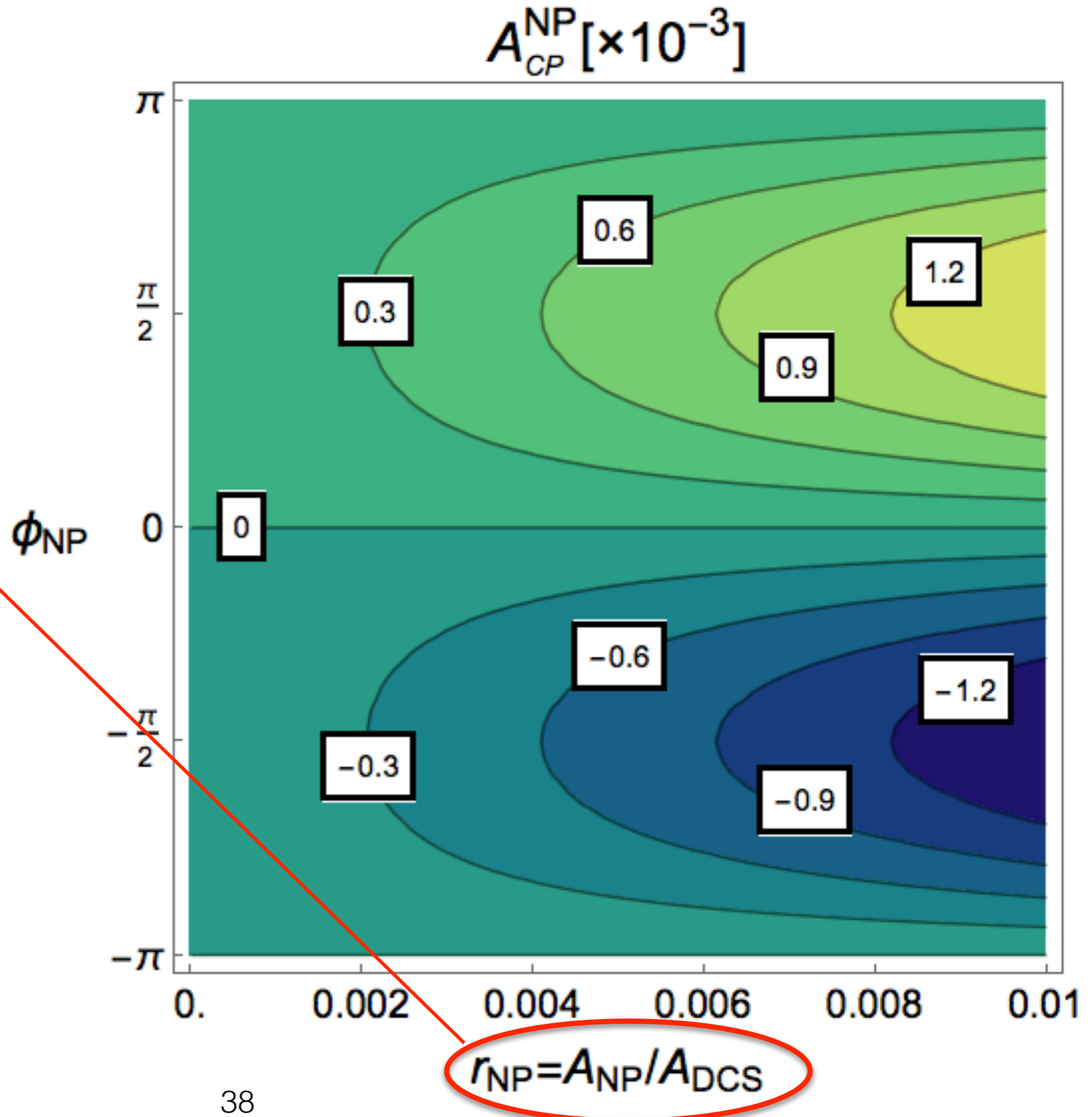
[1602.03160]

mode	$\mathcal{L}$ (fb <sup>-1</sup> )	$A_{CP}$ (%)	Belle II at 50 ab <sup>-1</sup>
$D^+ \rightarrow K_S^0 \pi^+$	977	$-0.36 \pm 0.09 \pm 0.07$	$\pm 0.03$

Belle II book, 1808.10567

$$\mathcal{A}(D \rightarrow f K_S^0) = \mathcal{A}_{CF}^{\text{SM}} + \mathcal{A}_{DCS}^{\text{SM}} (1 + r^{\text{NP}} e^{i\phi^{\text{NP}}} e^{i\delta^{\text{NP}}})$$

$$\frac{\mathcal{A}_{NP}}{\mathcal{A}_{SM}} = (0.1 \sim 1)\%$$



$$\mathcal{A}(D \rightarrow f K_S^0) = \mathcal{A}_{CF}^{\text{SM}} + \mathcal{A}_{DCS}^{\text{SM}}(1 + r^{\text{NP}} e^{i\phi^{\text{NP}}} e^{i\delta^{\text{NP}}})$$

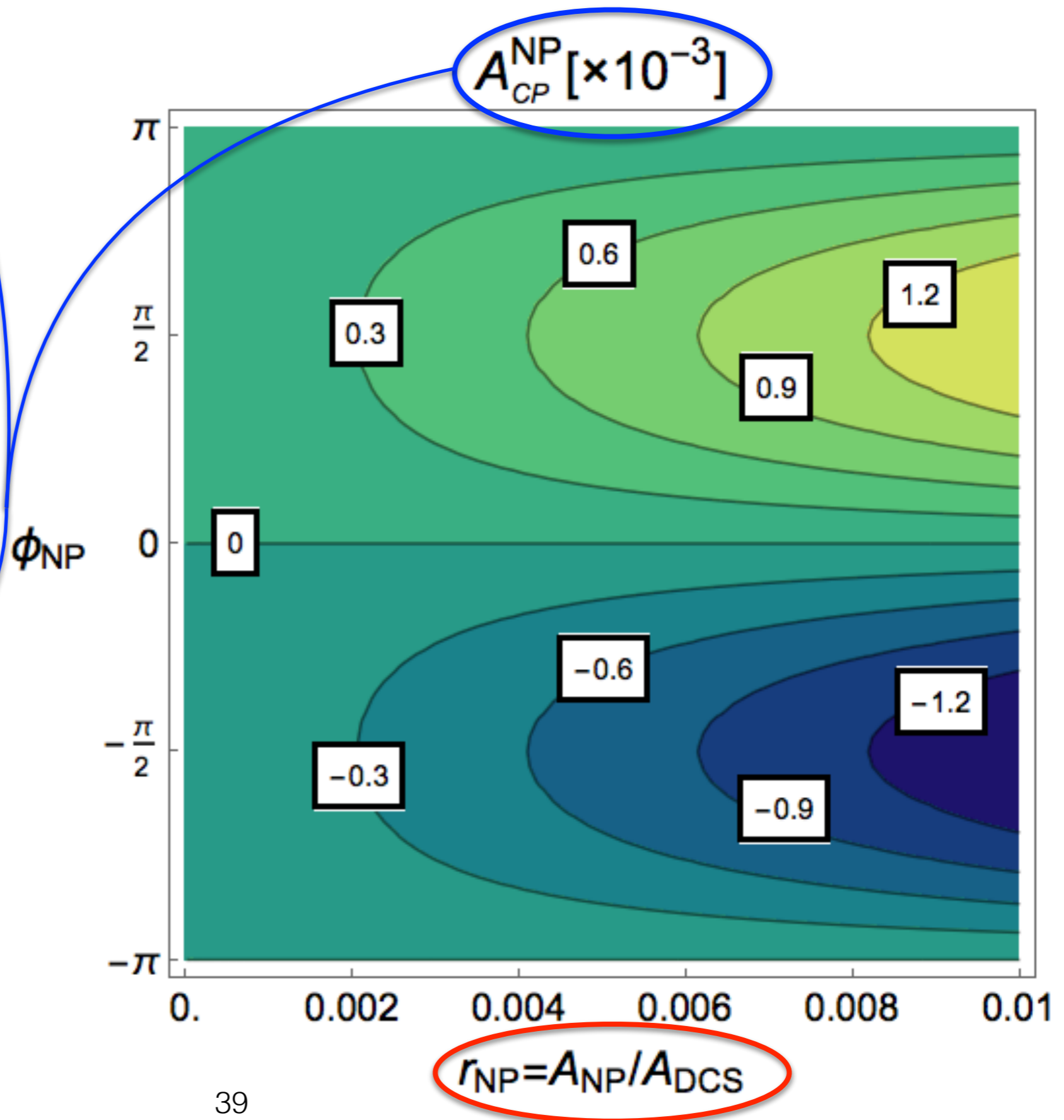
$$A_{\text{SM}}^{\text{dir}} = \mathcal{O}(10^{-5})$$

Even if

$$\frac{A_{\text{NP}}}{A_{\text{SM}}} = (0.1 \sim 1)\%$$

$$\frac{A_{\text{CP}}^{\text{NP}}}{A_{\text{CP}}^{\text{SM}}} = \mathcal{O}(10)$$

Promising for  
new physics!

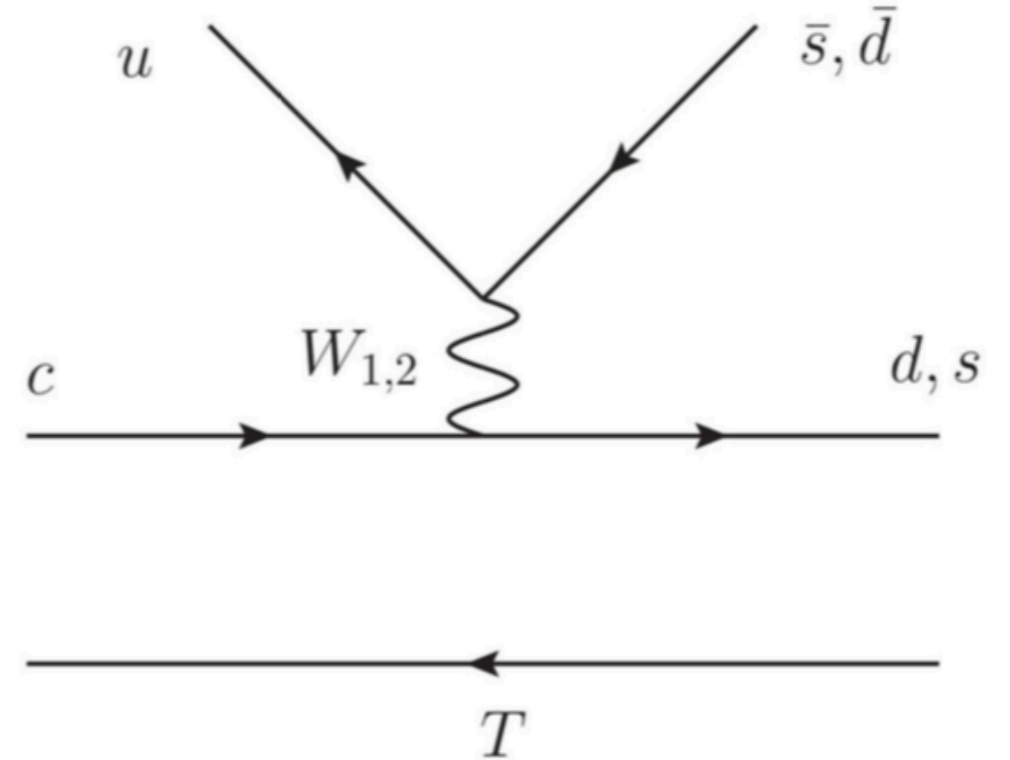


# Left-Right Symmetric Model

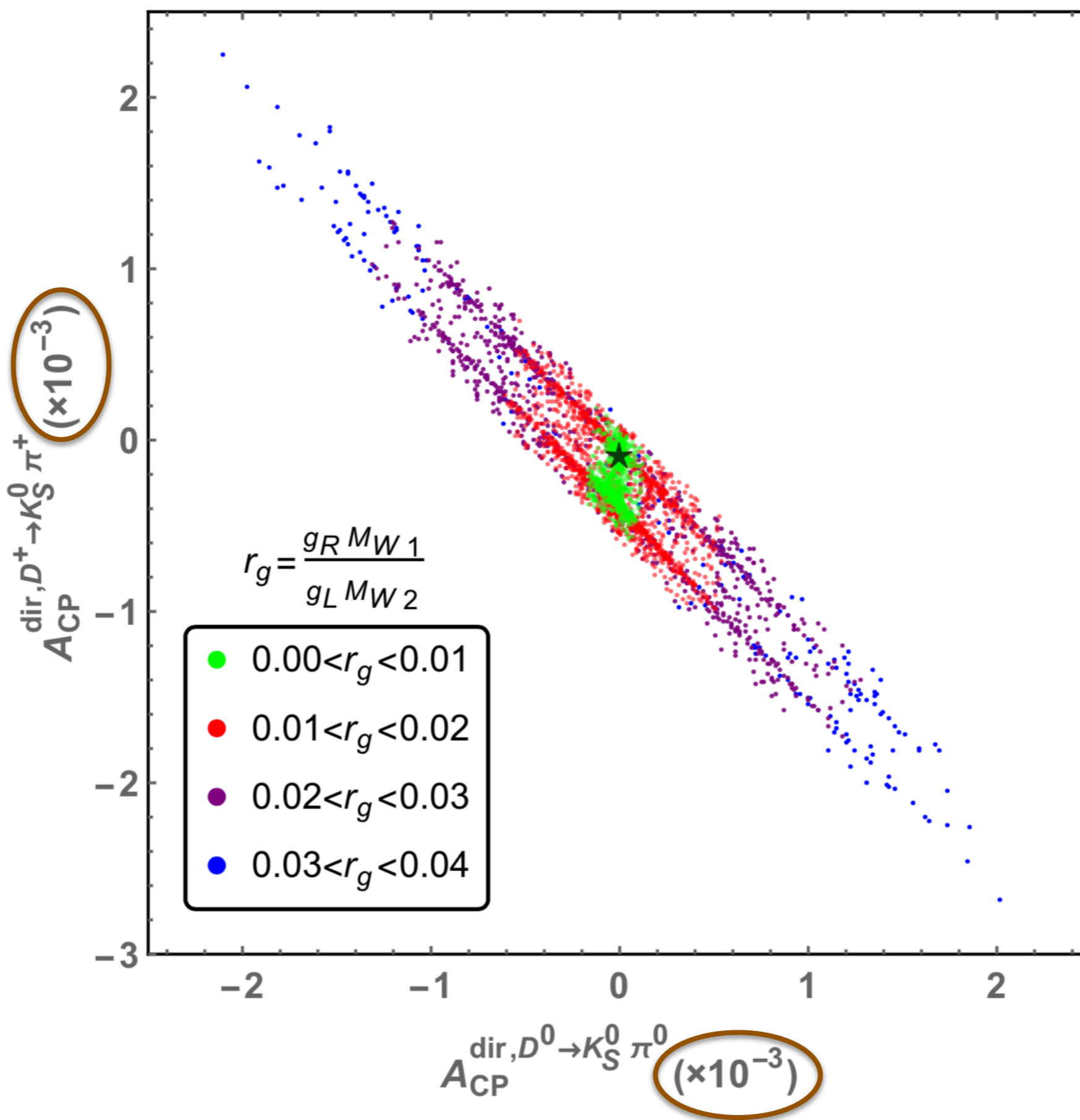
$$SU(2)_L \times SU(2)_R \times U(1)_{B-L} \rightarrow SU(2)_L \times U(1)_Y$$

$$\begin{pmatrix} W_L^- \\ W_R^- \end{pmatrix} = \begin{pmatrix} \cos \zeta & -\sin \zeta e^{i\omega} \\ \sin \zeta e^{-i\omega} & \cos \zeta \end{pmatrix} \begin{pmatrix} W_1^- \\ W_2^- \end{pmatrix}$$

$$V_{CKM}^R = \begin{pmatrix} 0 & e^{i\phi_0} & 0 \\ \cos \theta e^{i\phi_1} & 0 & -\sin \theta e^{i(\phi_1 - \phi_3)} \\ \sin \theta e^{i\phi_2} & 0 & \cos \theta e^{i(\phi_2 - \phi_3)} \end{pmatrix}$$







constrained by  $\Delta M_K$ ,  $\Delta M_{B_d}$ ,  $\Delta M_{B_s}$ ,  $|\epsilon|$ ,  $S_{J/\psi K_S^0}$  and  $\phi_{B_s}^{c\bar{c}s}$

# Advantages – $A_{CP}(D \rightarrow K_s f)$

- 1. Less ambiguities. Only tree diagrams,** easily established in theory, extracted from Br's.  
**Compared to SCS processes with penguins.**  
FAT approach works well.
- 2. More clear to signal NP.** NP may have large CP phase
- 3. Large branching fractions to measure.** CF processes.



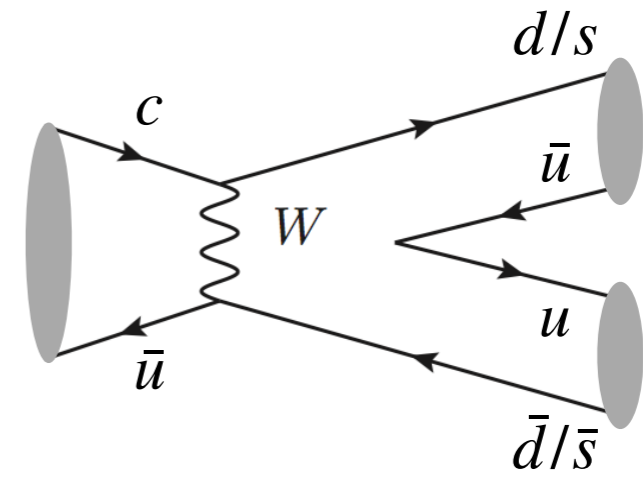
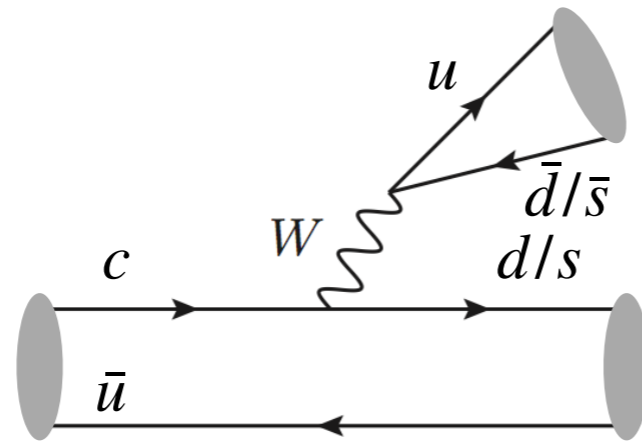
# Summary

- ❖ CPV in  $D^0 \rightarrow K^+ K^-$  and  $\pi^+ \pi^-$ 
  - Understandable in the Standard Model
  - Next potential is  $D^+ \rightarrow K^+ K^- \pi^+$
- ❖ **New CPV effect** is found in CF  $D \rightarrow K_s f$ 
  - mother decay and daughter mixing
  - To be subtracted to extract direct CPV
- ❖ Charm CPV is becoming more charming with precision at order of  $10^{-4}$

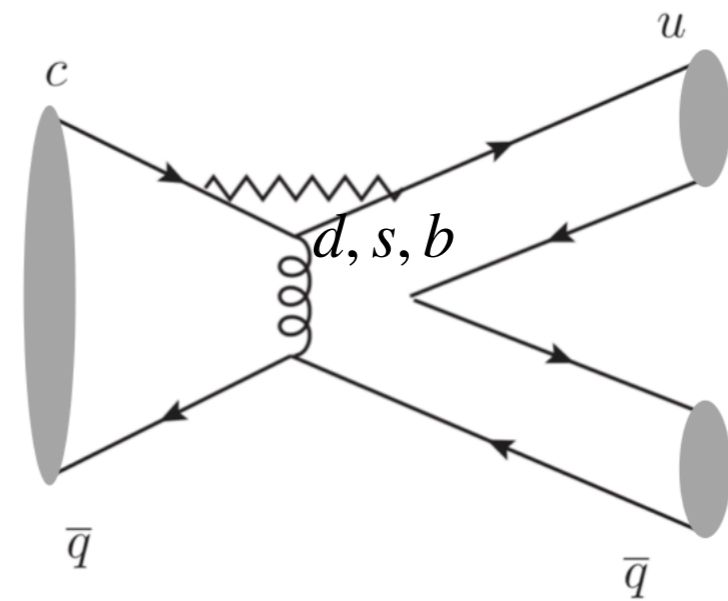
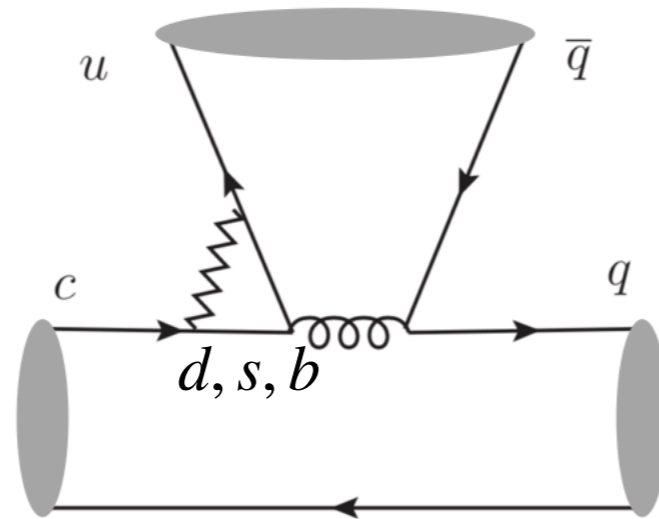
**Thank you for your attention!**

# Backups

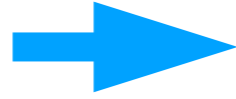
# Tree



# Penguin



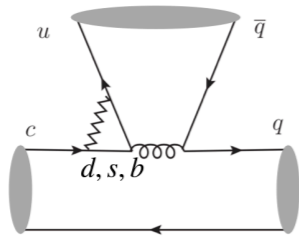
$$\left( \frac{|\mathcal{P}^{KK}|}{|\mathcal{T}^{KK}|} \sin \delta^{KK} + \frac{|\mathcal{P}^{\pi\pi}|}{|\mathcal{T}^{\pi\pi}|} \sin \delta^{\pi\pi} \right) \approx 1$$



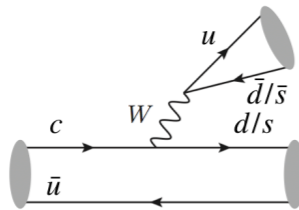
$$\frac{|\mathcal{P}|}{|\mathcal{T}|} \sin \delta \sim 1/2 \quad \text{or} \quad \text{Im}[\mathcal{P}/\mathcal{T}] \sim 1/2$$

**FAT2012**

$$\frac{\mathcal{P}^{\pi\pi}}{\mathcal{T}^{\pi\pi}} = 0.66e^{i134^\circ}, \quad \text{and} \quad \frac{\mathcal{P}^{KK}}{\mathcal{T}^{KK}} = 0.45e^{i131^\circ}$$



————— =



$$\frac{P}{T} = \frac{a_4 + a_6 r_\chi}{a_1} = 0.36e^{-i108^\circ}$$

$$r_\chi = 2m_0^2/m_c = 2.8, \quad \text{where} \quad m_0^\pi = m_\pi^2/(m_u + m_d)$$

$$a_4 = -0.036 - i0.098, \quad a_6 = -0.031 - i0.098$$

$$C_{3,5}(\mu) \rightarrow C_{3,5} - \frac{\alpha_s(\mu)}{8\pi N_c} \sum_{q=d,s} \frac{\lambda_q}{\lambda_b} C^q(\mu, \langle l^2 \rangle) + \frac{1}{N_c} \frac{\alpha_s(\mu)}{4\pi} \frac{m_c^2}{\langle l^2 \rangle} [C_{8g}(\mu) + C_5(\mu)],$$

$$C_{4,6}(\mu) \rightarrow C_{4,6} + \frac{\alpha_s(\mu)}{8\pi} \sum_{q=d,s} \frac{\lambda_q}{\lambda_b} C^q(\mu, \langle l^2 \rangle) - \frac{\alpha_s(\mu)}{4\pi} \frac{m_c^2}{\langle l^2 \rangle} [C_{8g}(\mu) + C_5(\mu)],$$

$$D \rightarrow f K_S^0 (\rightarrow \pi^+ \pi^-)$$

$$A_{CP}(t) \equiv \frac{\Gamma_{\pi\pi}(t) - \bar{\Gamma}_{\pi\pi}(t)}{\Gamma_{\pi\pi}(t) + \bar{\Gamma}_{\pi\pi}(t)}$$

Define:  $\frac{A_{DCS}}{A_{CF}} = \frac{\mathcal{A}(D \rightarrow K^0 f)}{\mathcal{A}(D \rightarrow \bar{K}^0 f)} = r e^{i(\phi+\delta)}$

$\downarrow$  strong phase  
 $\searrow$  weak phase  
 $\sim \lambda^2 \sim 0.05$

**Tree amplitudes !!!**

**Can be extracted from data of branching fractions**

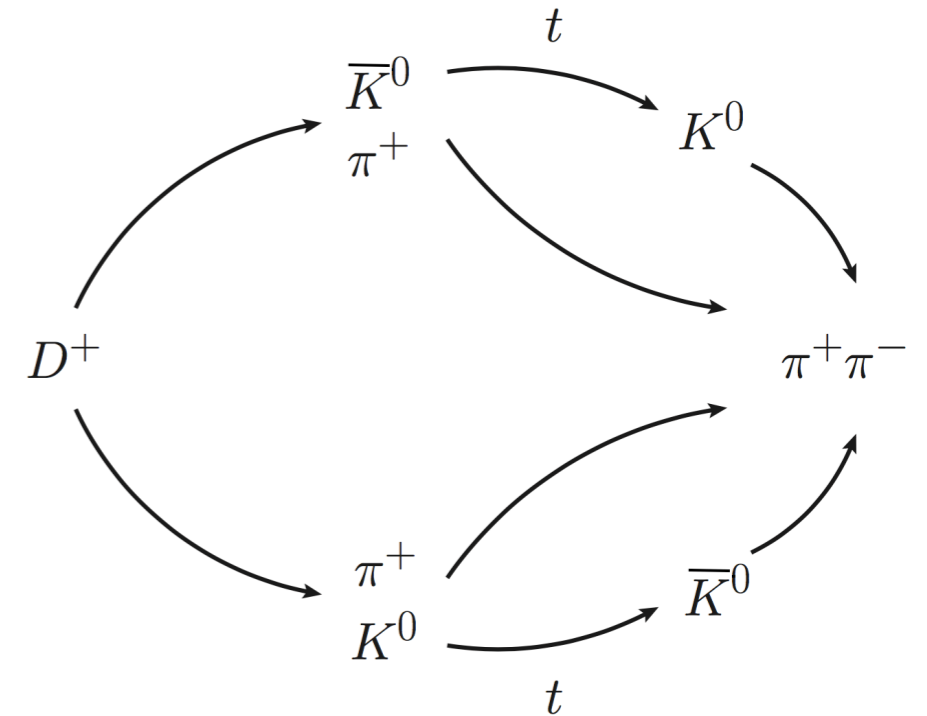
$$A_{CP}(t) = A_{CP}^{\bar{K}^0}(t) + A_{CP}^{\text{dir}}(t) + A_{CP}^{\text{int}}(t)$$

$$A_{CP}^{\bar{K}^0}(t) = 2e^{-\Gamma st} \mathcal{R}e(\epsilon) - 2e^{-\Gamma t} \left[ \mathcal{R}e(\epsilon) \cos(\Delta mt) + \mathcal{I}m(\epsilon) \sin(\Delta mt) \right],$$

$$A_{CP}^{\text{dir}}(t) = e^{-\Gamma st} 2r_f \sin \delta_f \sin \phi$$

$$\text{SM: } \phi \equiv \text{Arg}[-V_{cd}^* V_{us} / V_{cs}^* V_{ud}] = (-6.2 \pm 0.4) \times 10^{-4}$$

$$A_{CP}^{\text{int}}(t) = -4r_f \cos \phi \sin \delta_f \left[ e^{-\Gamma st} \mathcal{I}m(\epsilon) - e^{-\Gamma t} \left( \mathcal{I}m(\epsilon) \cos(\Delta mt) - \mathcal{R}e(\epsilon) \sin(\Delta mt) \right) \right]$$



**Mother decay,  
daughter mixing**

$$\phi \equiv \text{Arg} [-V_{cd}^* V_{us} / V_{cs}^* V_{ud}] = (-6.2 \pm 0.4) \times 10^{-4}$$

$$A_{CP}(t_1 \ll \tau_S \ll t_2 \ll \tau_L)$$

$$\simeq \frac{-2\text{Re}(\epsilon) + 2r_f \sin \phi \sin \delta_f - 4\text{Im}(\epsilon) r_f \cos \phi \sin \delta_f}{1 - 2r_f \cos \phi \cos \delta_f}$$

CPV in kaon mixing

**(10<sup>-3</sup>)**

direct CPV

**(10<sup>-5</sup>)**

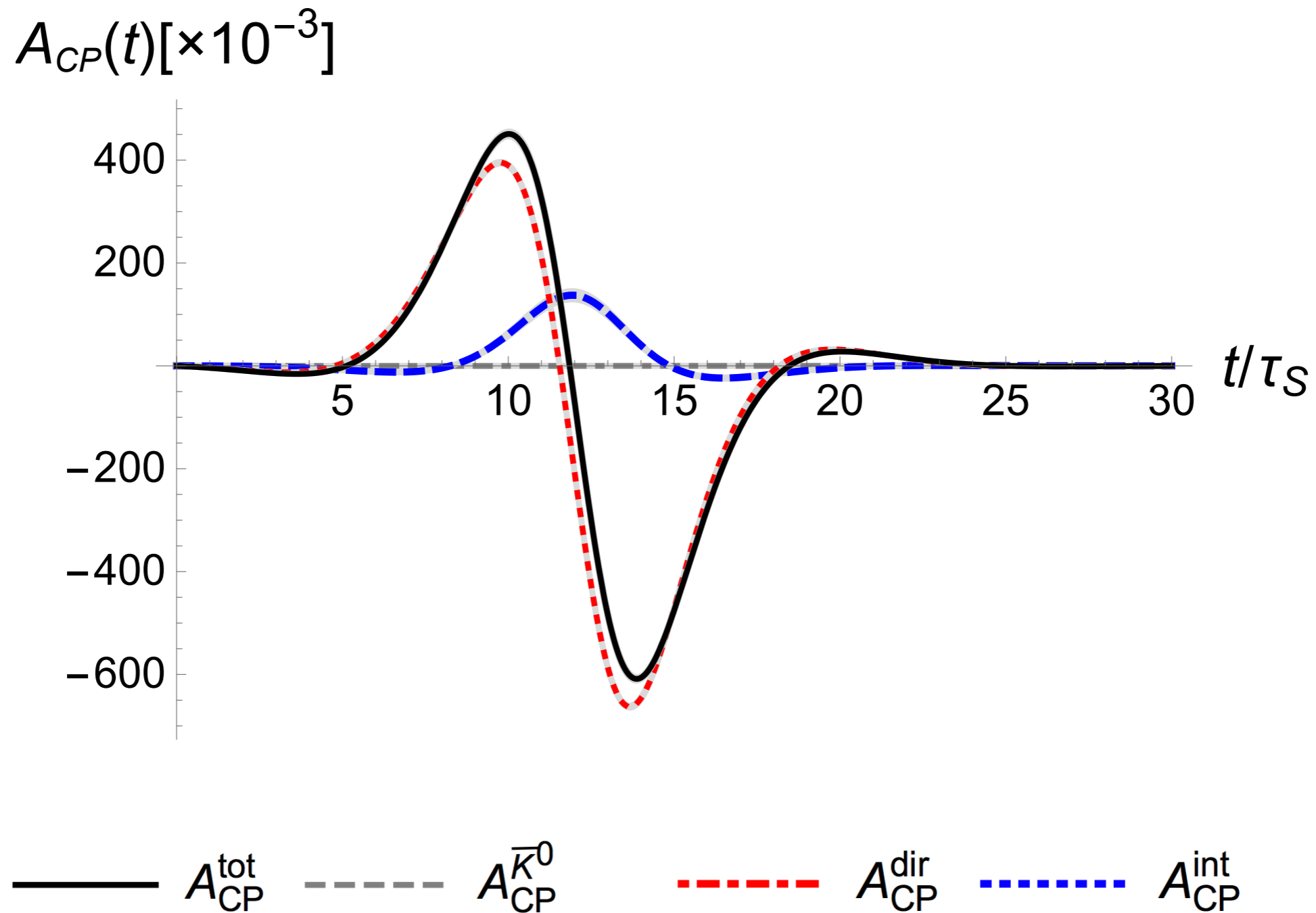
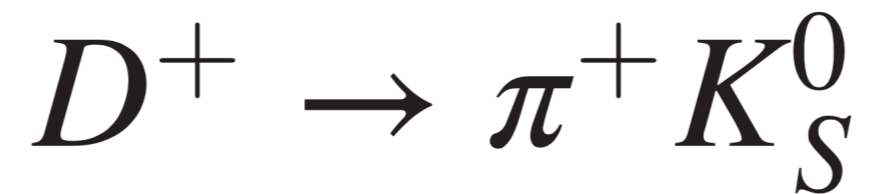
New CPV effect

**(10<sup>-4 ~ -3</sup>)**

Sensitive to New Physics CP phase

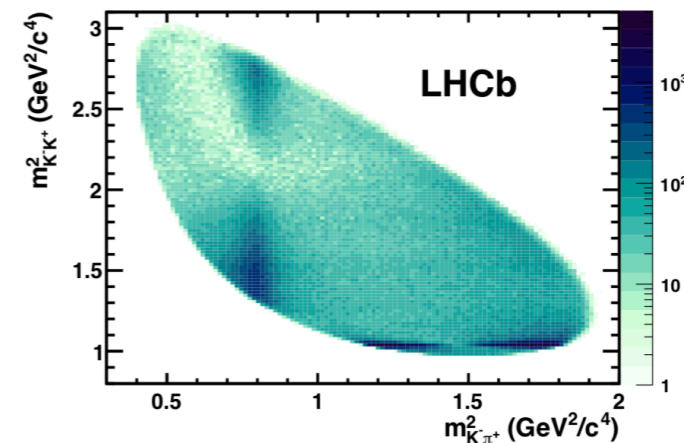


# Time-dependent CPV



# Searching Strategies

## 1. Binned $D^+ \rightarrow K^+ K^- \pi^+$



	Branching Fractions	CP Violation
$D^+ \rightarrow \pi^+ \phi$	$2.6 \times 10^{-3}$	$10^{-7}$ <span style="border: 1px solid brown; padding: 2px;">Benchmark</span>
$D^+ \rightarrow K^+ \bar{K}^{*0}$	$2.4 \times 10^{-3}$	$0.2 \times 10^{-3}$
$D^+ \rightarrow K^+ \bar{K}_0^{*0}(1430)$	$1.8 \times 10^{-3}$	$-0.9 \times 10^{-3}$

# Searching Strategies

## 2. Phase Space Integrated

Li, Lu, FSY, 1903.10638

$$(1) \quad A_{CP}(D^+ \rightarrow K^+ K^- \pi^+) - A_{CP}(D^+ \rightarrow \pi^+ \pi^- \pi^+) \\ = A_{CP}^{\text{raw}}(D^+ \rightarrow K^+ K^- \pi^+) - A_{CP}^{\text{raw}}(D^+ \rightarrow \pi^+ \pi^- \pi^+) \\ \text{Br}=0.95\% \qquad \qquad \qquad \text{Br}=0.3\%$$

$$(2) \quad A_{CP}(D^+ \rightarrow K^+ K^- \pi^+) - A_{CP}(D_s^+ \rightarrow K^+ \pi^+ \pi^-) \\ = \left[ A_{CP}^{\text{raw}}(D^+ \rightarrow K^+ K^- \pi^+) - A_{CP}^{\text{raw}}(D^+ \rightarrow K^- \pi^+ \pi^+) \right] \\ \text{Br}=0.95\% \qquad \qquad \qquad \text{Br}=9\% \\ - \left[ A_{CP}^{\text{raw}}(D_s^+ \rightarrow K^+ \pi^+ \pi^-) - A_{CP}^{\text{raw}}(D_s^+ \rightarrow K^+ K^- \pi^+) \right] \\ \text{Br}=0.66\% \qquad \qquad \qquad \text{Br}=5.5\%$$