

# Extracting Photon PDF and Proton PDFs at an EIC

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1. Possible realizations of an EIC
2. Photon structure studied at eRHIC
  - Motivation and Introduction
  - (Un)polarized photon structure
  - Calculation of the underlying events effect
3. Extracting proton PDFs from EIC by a global analysis
4. Summary and outlook

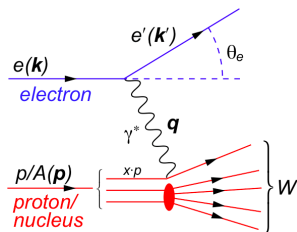
# Questions an EIC aims to answer

The core questions described in the EIC white paper

- How are the **sea quarks and gluons, and their spins**, distributed in space and momentum inside the nucleon? - **Polarization**
- How do color-charged **quarks and gluons distributed** with a nuclear medium? - **A range of center of mass energies & High Luminosity**
- What happens to the **gluon density** in nuclei? Where does the **saturation** of gluon densities set in? - **Ion beams**

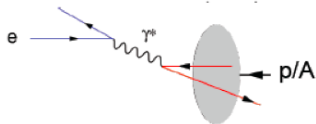
These questions call for facilities with capabilities that far exceed any current or past colliding beams accelerator facility: **Electron Ion Collider (EIC)**

# Deep Inelastic Scattering

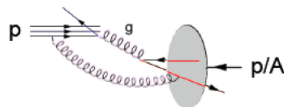


$$Q^2 = sxy$$

- $s$ : center-of-mass energy squared
- $Q^2$ : Resolution power
- $x$ : The fraction of the nucleon's momentum carried by the struck quark
- $y$ : Inelasticity



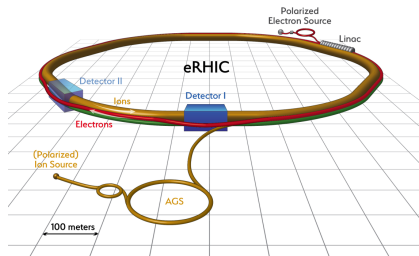
- Electron beams provide point-like probe - resolution
- Direct, model independent determination of partonic kinematics of physics processes
- High precision & access to partonic kinematics through scattered lepton



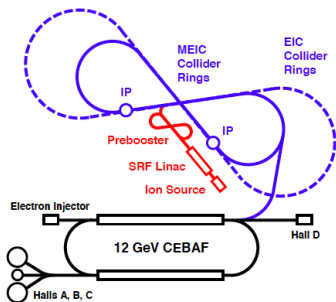
- Probe has complex structure
- No simple access to partonic kinematics

# Physics cases of EIC in US

eRHIC @ BNL



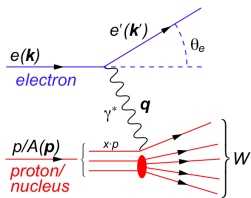
JLEIC @ JLAB



## eRHIC:

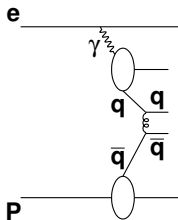
- Center-of-mass energy ( $E_{cm}$ ) of (29-140) GeV
- A luminosity of up to  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- High polarization of electron and ion beams with frequent changes to the spin direction with polarizations well above 70%
- Collisions of electrons with a large range of light to heavy ions (protons to Gold ions)

# Photon structure studied at EIC: Motivation

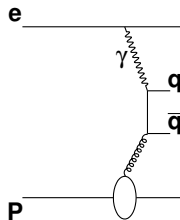


- Behavior of the exchanged photon: direct photon state, **resolved photon state**
- The “internal structure” of photons is a manifestation of **quantum fluctuations**: photon splits into parton content
- **Photoproduction**: low  $Q^2$
- **Parton Distribution Functions(PDFs)** of Photon:  $q(x, Q^2), g(x, Q^2)$

Resolved state

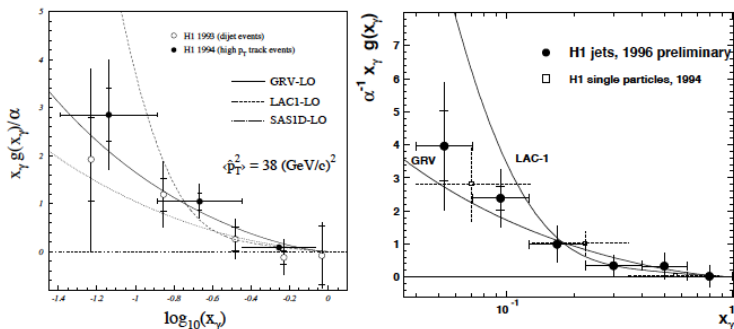


Direct state



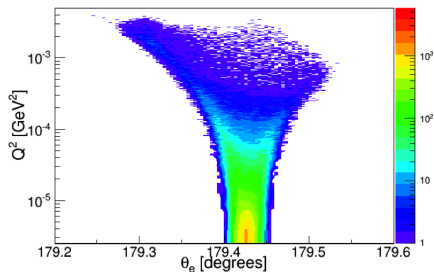
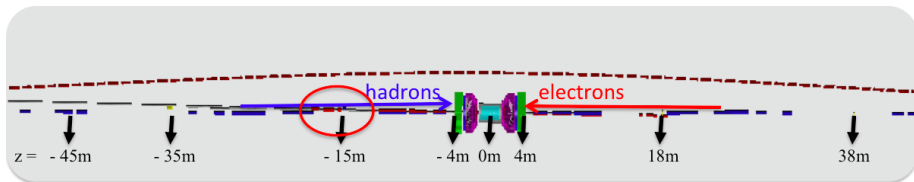
# Motivation: Existing experiment results

[arXiv:9504004, arXiv:9710018, Eur. Phys. J. C 10, 363-372 (1999), DESY 97-164]



- Lack of statistic, especially in the small  $x_\gamma$  region which is important for the constrain of photon PDFs.
- Results from jet and charged particle measurements show that the best fit are GRV and SAS
- The nature of  $e^+e^-$  collisions is two photon physics, the photon structure is very important for ILC  $\gamma\gamma$  option.
- Polarized photon PDFs are never measured before.

# Low $Q^2$ tagger

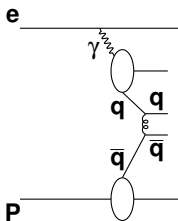


- Outgoing electrons are reconstructed in the tagger
- Acceptance for electrons is down to  $10^{-5}$   $\text{GeV}^2$

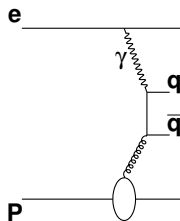


# Di-jet measurement

Resolved process



Direct process



- How to separate: **Resolved:  $x_\gamma < 1$ ; direct:  $x_\gamma = 1$ .**

$$x_\gamma^{\text{rec}} = \frac{1}{2E_e y} (p_{T1} e^{-\eta_1} + p_{T2} e^{\eta_2}), \quad y = \frac{E_\gamma}{E_e}.$$

- Parton densities can be extracted by **measuring di-jet cross section:**

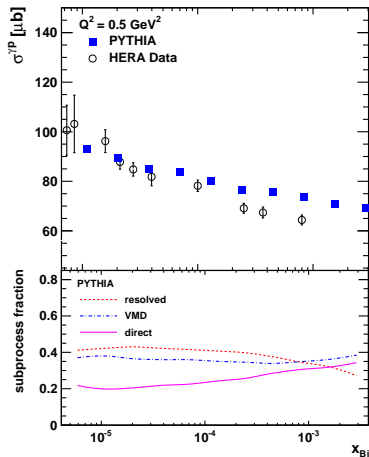
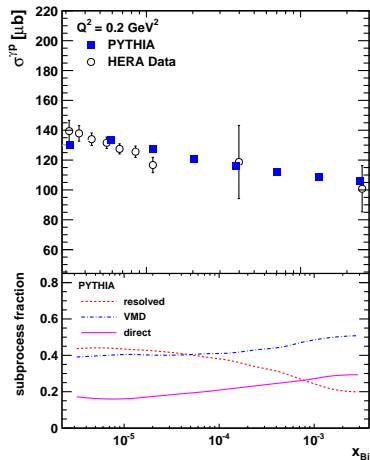
$$\frac{d^2\sigma}{dx_\gamma dQ^2} = \gamma_{\text{flux}} \otimes f_\gamma(x_\gamma, Q^2, \mu) \otimes f_p(x_p, \mu) \otimes \sigma_{ij},$$

$\gamma_{\text{flux}}$  is calculable in QED,  $f_p$  is the PDF of the proton,  $\sigma_{ij}$  is the cross section of the hard process, which is calculable in pQCD

# Reproduce HERA data

Reproduce the inclusive cross section, photon PDF set is SAS, proton PDF is CTEQ5m,

$$10^{-5} \text{GeV}^2 < Q^2 < 1 \text{GeV}^2, L = 1 \text{fb}^{-1}.$$

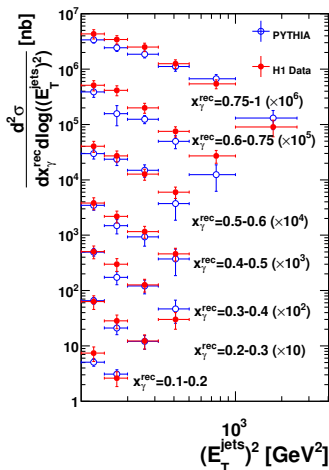


[HERA Data: Phys. Rev. D 96 014001(2017)]

# Reproduce HERA data

Reproduce the di-jet cross section, photon PDF set is SAS, proton PDF is CTEQ5m,

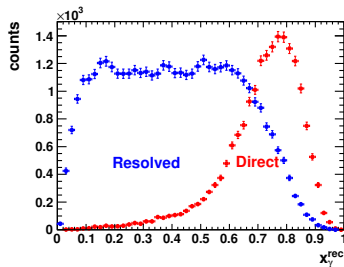
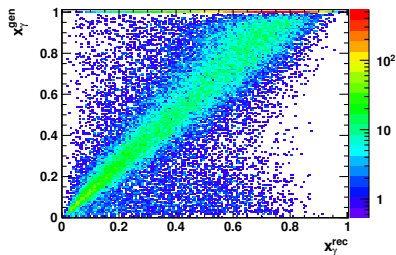
$$10^{-5}\text{GeV}^2 < Q^2 < 1\text{GeV}^2.$$



- Kinematics cuts from HERA:  
 $27.5\text{GeV} \times 820\text{GeV}$ ,  
 $0.2 < y < 0.83$ ,  $|\Delta\eta^{\text{jets}}| < 1$ ,  
 $0 < \eta^{\text{jet1}} + \eta^{\text{jet2}} < 4$ ,  
 $E_T^{\text{jet1}}, E_T^{\text{jet2}} > 7.5\text{GeV}$ ,  
 $E_T^{\text{jet1}} + E_T^{\text{jet2}} > 20\text{GeV}$ ,  
 $|E_T^{\text{jet1}} - E_T^{\text{jet2}}| / (E_T^{\text{jet1}} + E_T^{\text{jet2}}) < 0.25$
- Our simulation can match the existing data

# Unpolarized photon structure at EIC

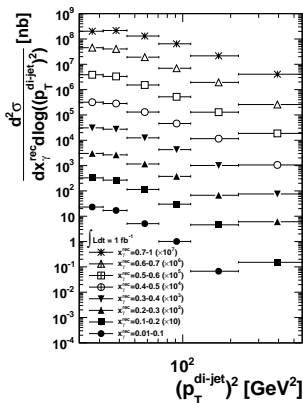
20 GeV  $\times$  250 GeV,  $0.01 < y < 0.95$ , two highest  $p_T$  jets,  $p_T^{\text{jet1}} > 5 \text{ GeV}$ ,  $p_T^{\text{jet1}} > p_T^{\text{jet2}} > 4.5 \text{ GeV}$ ,  $|\eta^{\text{jets}}| < 4.5$ , stable particle  $p_T > 250 \text{ MeV}$ .



Di-jet method provides a good way to reconstruct  $x_\gamma$ , we can separate resolved/direct process ( $x_\gamma^{\text{rec}} < 0.6$ ).

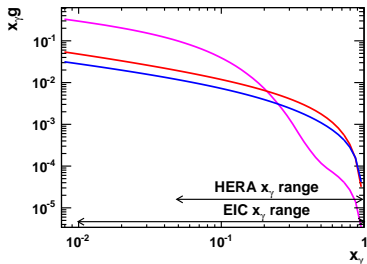
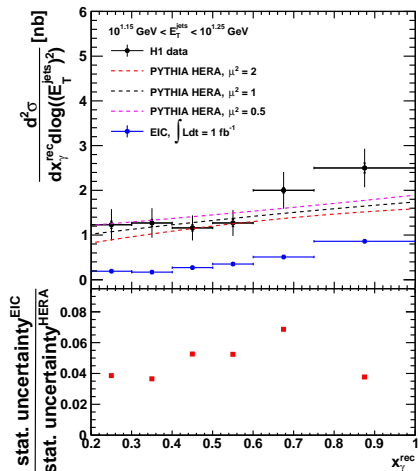
# Unpolarized photon structure at EIC

20 GeV  $\times$  250 GeV,  $0.01 < y < 0.95$ , two highest  $p_T$  jets,  $p_T^{\text{jet1}} > 5 \text{ GeV}$ ,  $p_T^{\text{jet1}} > p_T^{\text{jet2}} > 4.5 \text{ GeV}$ ,  $|\eta^{\text{jets}}| < 4.5$ , stable particle  $p_T > 250 \text{ MeV}$ .



The simulation shows the capability to measure the cross section for di-jet production at  $\int L = 1 \text{ fb}^{-1}$ , with high accuracy in a wide kinematic range at EIC and extract the unpolarized photon PDFs from a global fit.

# EIC advantages compared to HERA



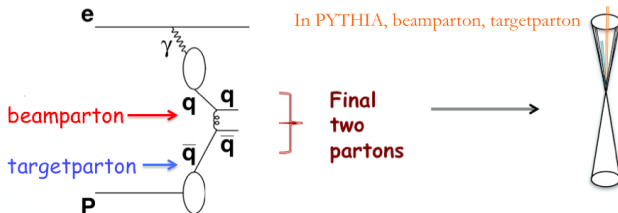
- High luminosity to define the uncertainty band
- Feasibility to probe small  $x_\gamma$  region

# Method of flavor tagging

The photon is in the hadronic state, can we expect to know the information of the parton content inside the photon?

- $\frac{d^2\sigma}{dx_\gamma dQ^2} = \gamma_{flux} \otimes f_\gamma(x_\gamma, Q^2, \mu) \otimes f_p(x_p, \mu) \otimes \sigma_{ij}$
- From measuring the di-jet cross section, we can extract the total PDFs of the photon.
- We search the possibility of q/g discrimination. (will be discussed later)
- We do flavor tagging to achieve the goal of separating the contribution from different flavor partons.

# Method of flavor tagging

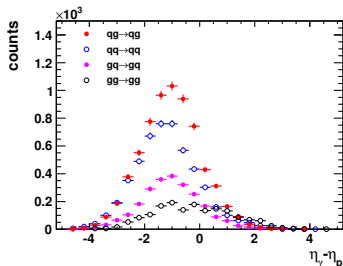
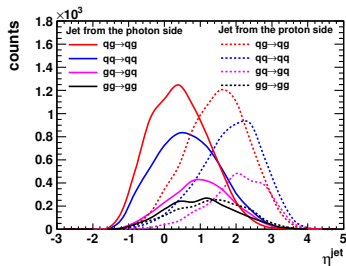


We will separate  $q/g$  jet first and select the jet from the parton which has the same flavor as the beamparton, which is marked with "jet from the photon side".



# How to choose the jet from the photon side

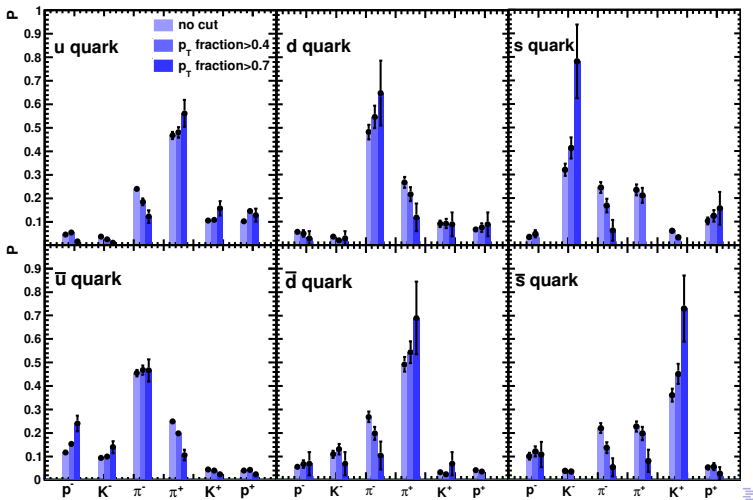
$$\overbrace{\hspace{10em}}^{\text{hadrons, } \eta_{\text{Lab}} > 0} \quad \overleftarrow{\hspace{10em}}^{\text{electrons, } \eta_{\text{Lab}} < 0}$$



- **Conclusion:** Influenced by the moving direction of the incoming electrons, the jets from the photon which is radiated from the electron, the pseudo-rapidity of jet from the photon is smaller than that of proton side jet
- **What we can do in the experiment:** take the jet with smaller  $\eta$  as the photon side jet

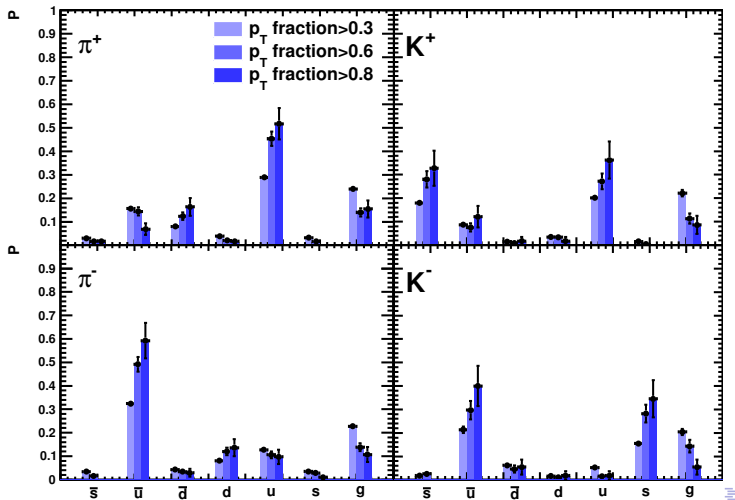
# Flavor tagging

The correlation between the beampton flavor and the type of the leading hadron inside photon side jet.



# Flavor tagging

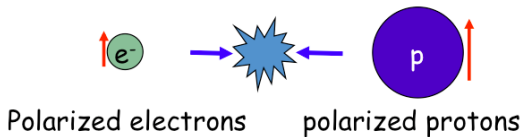
The correlation between the beampton flavor and the type of the leading hadron inside photon side jet.



What is the behavior  
of the photon if we  
add spin on it?



# Polarized photon PDFs



# Input for polarized ep collision

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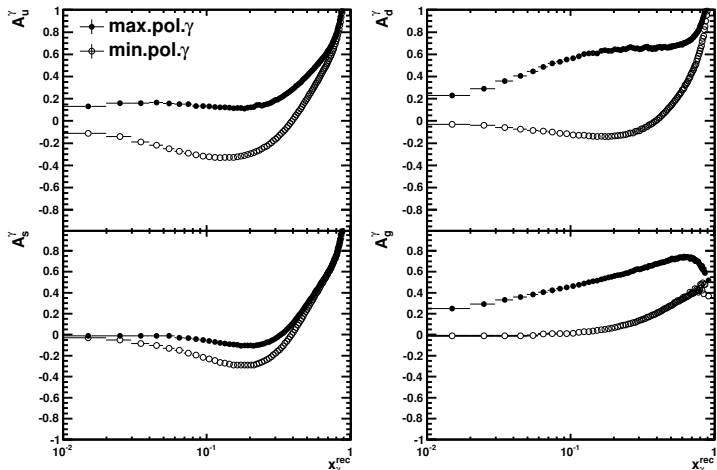
pol. photon PDFs    min:  $\Delta f^\gamma = 0$ ; max:  $\Delta f^\gamma = f^\gamma$

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pol. proton PDF    DSSV

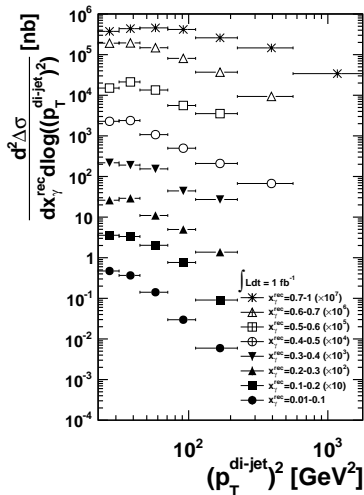
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$$A^\gamma = \Delta f^\gamma / f^\gamma$$



# Polarized photon structure

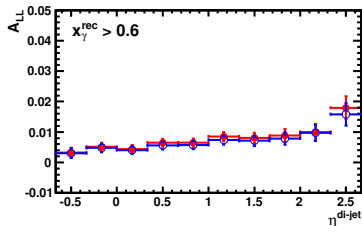
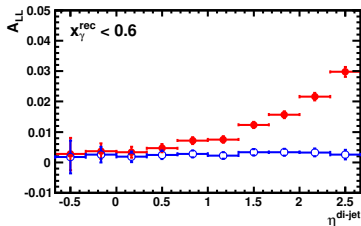
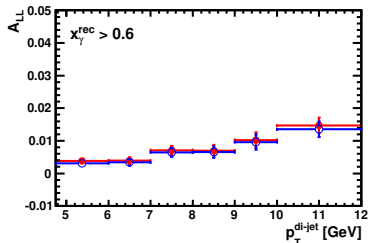
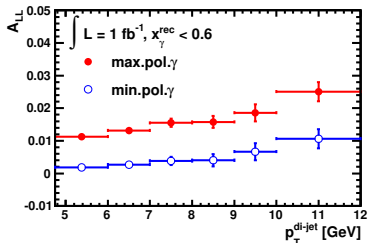
$$\frac{d^2 \Delta \sigma}{dx_\gamma dQ^2} = \Delta \gamma_{flux} \otimes \Delta f_\gamma(x_\gamma, Q^2, \mu) \otimes \Delta f_p(x_p, \mu) \otimes \sigma_{ij}$$



$$\Delta \sigma = \frac{1}{2} (\sigma^{++} - \sigma^{+-})$$

- The simulation shows the capability to measure the polarized cross section for di-jet production, with high accuracy in a wide kinematic range at EIC.
- First measurement of polarized photon PDFs with high precision.
- Flavor tagging can also be applied in polarized case.

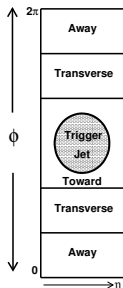
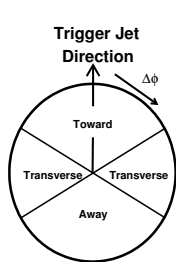
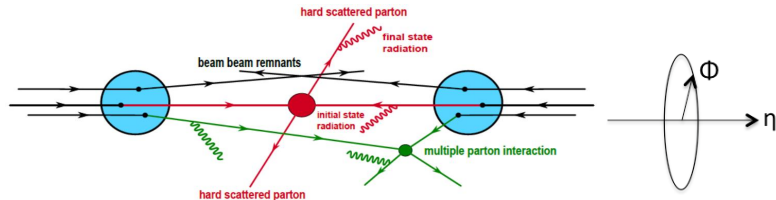
$$A_{LL} = \Delta\sigma/\sigma$$



The difference between max.pol. photon and min.pol. photon can be measured in experiment, the pol.photon PDFs can be constrained at EIC.

# Underlying events: region method

Underlying events: everything except the particles fragmented from the hard scattered partons.



Three regions: ( $\Delta\Phi = \Phi_{\text{part}} - \Phi_{\text{Jet1}}$ )

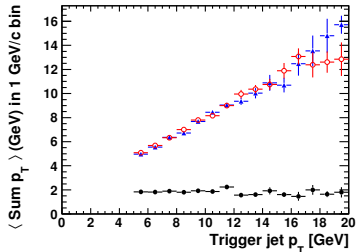
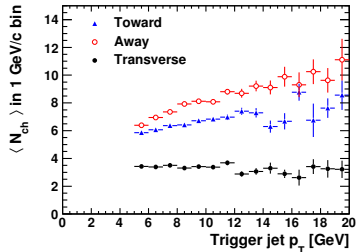
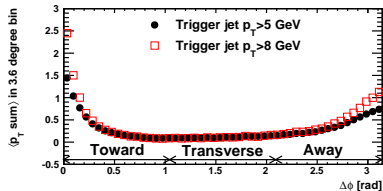
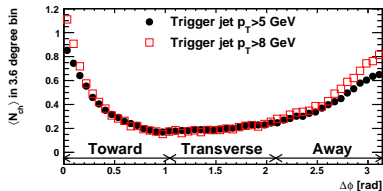
- Toward:  $|\Delta\Phi| < 60^\circ$
- Transverse:  $60^\circ < |\Delta\Phi| < 120^\circ$
- Away:  $|\Delta\Phi| > 120^\circ$

Measurements:

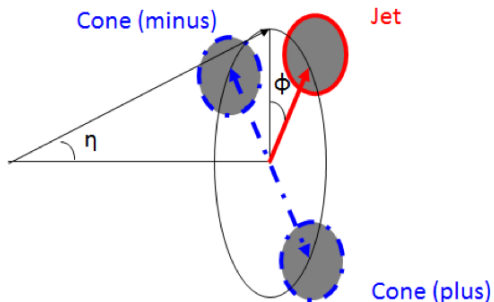
- Charged multiplicity density, sum pt density Versus  $\Delta\Phi$
- Charged multiplicity density, sum pt density Versus  $p_T^{\text{Jet1}}$



# Results from region method

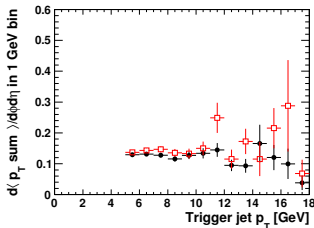
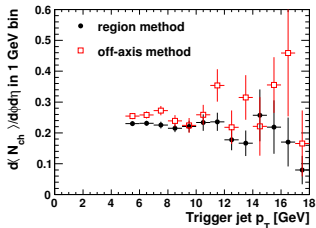


# Off-axis method



- Look at jets with high momentum, jet by jet
- Two off-axis cones are centered at the same  $\eta$  as the jet but  $\pm\pi$  away in  $\Phi$  from the jet
- Take the particles inside the cones as from underlying events. By using this method, the dependence on  $\eta$  is considered.

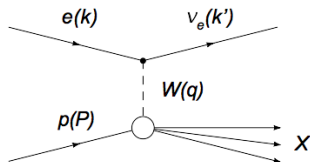
# Comparison of the two methods



- Results from two different methods are consistent, the dependence on  $\eta$  is minor
- The underlying event effect from EIC is comparable with the results from  $\sqrt{s} = 250$  GeV  $pp$  collisions at STAR

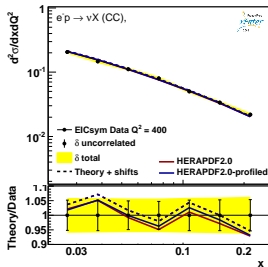
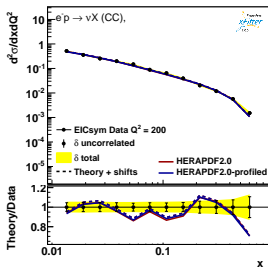
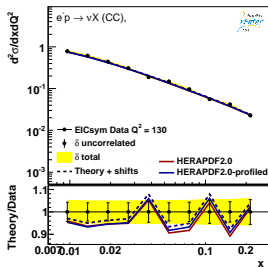
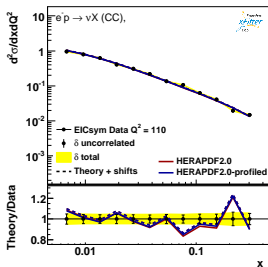
# Proton PDFs extracted from inclusive CC $ep$ scattering

High  $x$  and high  $Q^2$  events

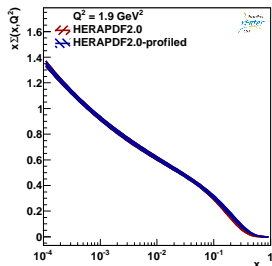
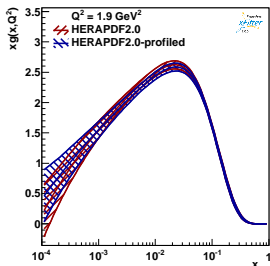
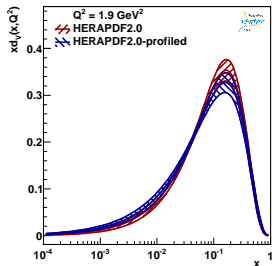
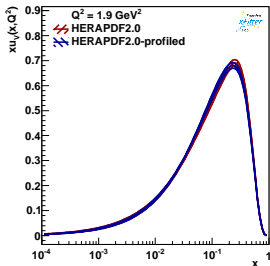


- The reduced cross section for inclusive Charged Current  $ep$  scattering are defined as  $\sigma_{r,CC} = \frac{2\pi x_{Bj}}{G_F^2} \left[ \frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d^2\sigma_{CC}}{dx_{Bj}dQ^2}$ , in HERAFitter, the value of  $G_F = 1.16 \times 10^{-5} \text{ GeV}^2$  and  $M_W = 80.385 \text{ GeV}$ .
- CC structure function are defined as  $\sigma_{r,CC}^- \approx (xU + (1-y)^2 x\bar{D})$ ,  $U = xu + xc$ ,  $\bar{D} = x\bar{d} + x\bar{s}$

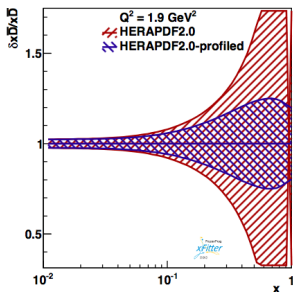
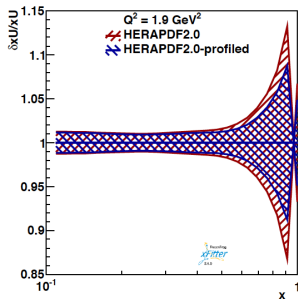
# Inclusive cross section



# Extracting PDFs by a global fitting



# How well can EIC constrain PDFs?



$$xU = xu + xc, x\bar{D} = x\bar{d} + x\bar{s}$$

$U$  and  $\bar{D}$  are better constrained compared with HERA

# Summary and outlook

The EIC will profoundly impact our understanding of QCD and its dynamics with high luminosity & high energy, nuclei & beam polarization

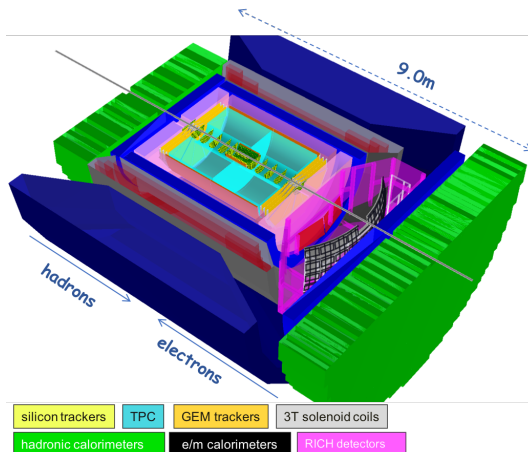
- The structure of nucleons and nuclei
- Spin of the proton
- Will enable images of yet unexplored nonlinear regions



Thank you!

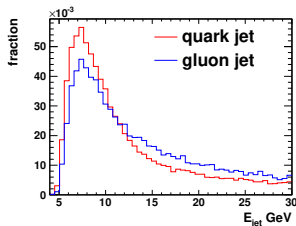
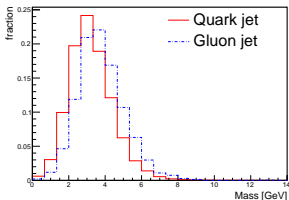
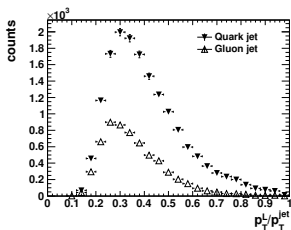
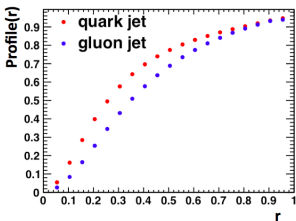


# back up: The tracking system used in the model detector for eRHIC



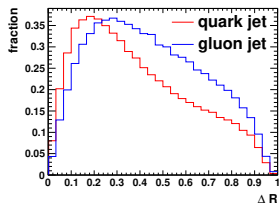
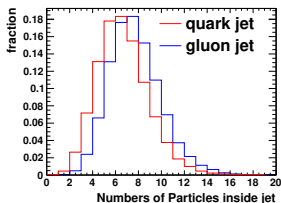
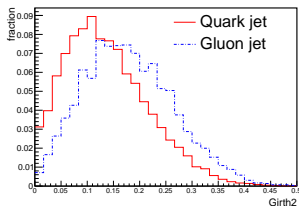
- Time projection chamber (TPC)  
 $|\eta| < 2$
- Silicon trackers  
 $2 < |\eta| < 4$
- Electromagnetic Calorimeter (ECal)  
 $-4 < \eta < 4$
- Hadron Calorimeter (HCal):  
 $1 < |\eta| < 4$

# Multivariable-distribution of q/g jet



Gluon jets have a more uniform energy fragmentation, while quark jets are more likely to produce narrow jets with hard constituents that carry a significant fraction of the energy.

# q/g jet discrimination

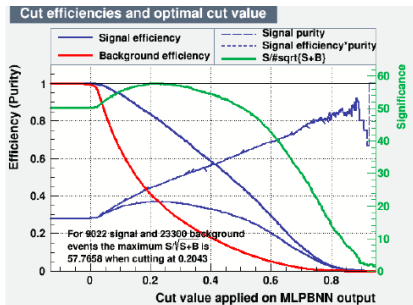
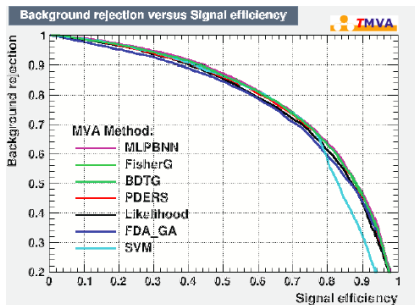


- **Some definitions:**  $p_T^L$  represents the highest  $p_T$  of the hadrons inside the jet;

$$\text{Girth2} = \sum_{i \in \text{cone}} \frac{p_T^i}{p_T^{\text{jet}}} |R_i|^2; \Delta R \text{ is the distance between particle and jet axis}$$

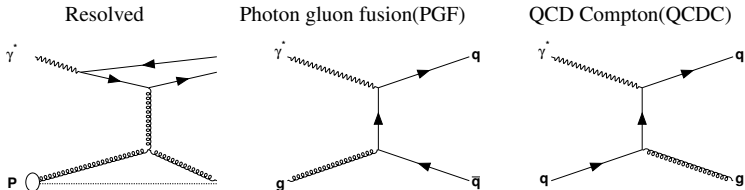
- **Conclusion:** Gluon jets are wider, with higher multiplicities, having a more uniform energy fragmentation, while quark jets are more likely to produce narrow jets with hard constituents that carry a significant fraction of the energy

# TMVA method

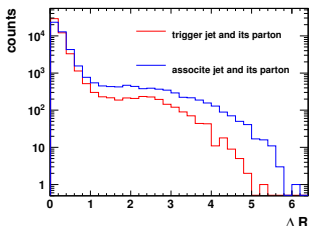


Toolkit for Multivariate Data Analysis with ROOT (TMVA): for current study, we place cut where signal purity = signal efficiency

# Di-jets at EIC from PYTHIA



- The resolved, direct (PGF, QCDC) processes can produce di-jets.
- For each di-jet pair, we do geometry match in the simulation, then will know the jet is a quark/gluon jet.



- two output partons  $\rightarrow$  di-jet match in each event,  $\Delta R < 1.0$

# Jet algorithm

- Clustering Algorithms

- $k_T$ :  $d_i = p_{T,i}^2$ ,

$$d_{ij} = \min(p_{T,i}^2, p_{T,j}^2) \times \frac{\Delta R_{ij}^2}{R^2} = \min(p_{T,i}^2, p_{T,j}^2) \times \frac{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}{R^2}, \text{ if}$$

$d_{\min} = \min(d_i, d_{ij})$  is  $d_{ij}$ ; else, remove  $j$  from the list as a jet.

- anti- $k_T$ :  $d_i = \frac{1}{p_{T,i}^2}$ ,  $d_{ij} = \min\left(\frac{1}{p_{T,i}^2}, \frac{1}{p_{T,j}^2}\right) \times \frac{\Delta R_{ij}^2}{R^2}$ .

Given  $p_{T,j}$  is very small, also  $\frac{\Delta R_{ij}^2}{R^2} > 1$ :

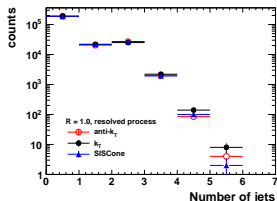
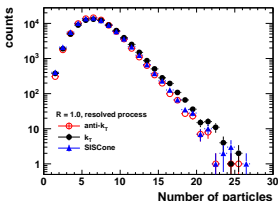
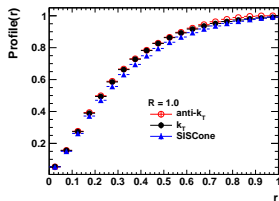
$$\text{anti-}k_T: d_{ij} = \frac{1}{p_{T,i}^2} \times \frac{\Delta R_{ij}^2}{R^2} > \frac{1}{p_{T,i}^2}.$$

It's more likely that  $j$  will be a candidate particle for jets by applying  $k_T$  algorithm than of anti- $k_T$ . The back reaction sensitivity is highly suppressed by using anti- $k_T$  algorithm in comparison with  $k_T$  algorithm.

- Cone-Type Algorithms

- SIScone: All circles defined by pairs of edge points are all stable cones.

# Jet algorithm

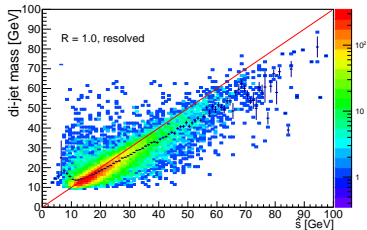
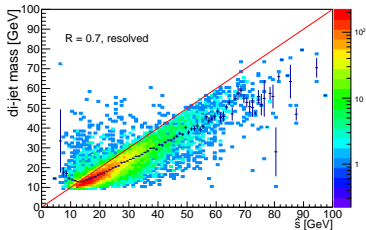
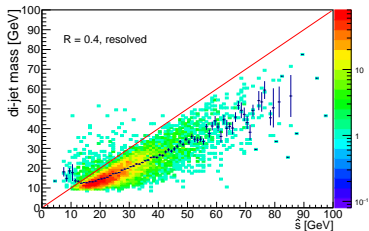
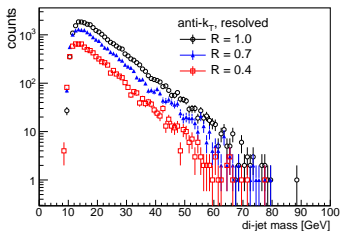


- Some definitions:  $Profile(r) = \frac{\sum_{r_i < r} p_T^i}{p_T^{\text{jet}}}$ , with drawing a inner cone ( $r$  is the radius of this cone,  $r = \sqrt{\Delta\eta^2 + \Delta\phi^2}$ ) inside the jet
- Result: While there are differences in the general behavior of different algorithms, they are relatively minor
- Conclusion: The choice of algorithm will have little impact, anti- $k_T$  algorithm produces the most collimated jets with regular boundaries

# Jet definition: jet radius

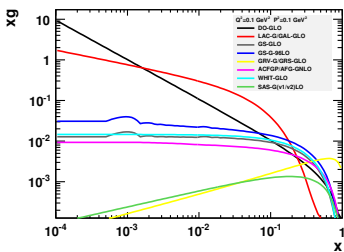
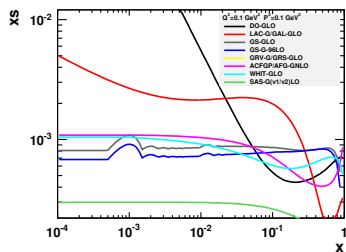
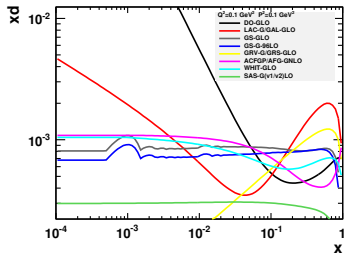
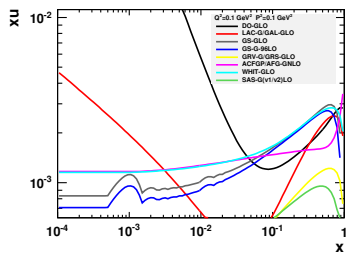
$R=0.4, 0.7, 1.0$ .  $\hat{s}$  is the input squared invariant mass of the two partons. di-jet mass is reconstructed:

$$M = \sqrt{2p_{T1}p_{T2}(\cosh(\Delta\eta) - \cos(\Delta\Phi))}.$$





# Motivation: Existing photon PDFs



$x$  is the momentum fraction of the parton from the photon, in the following section, it is marked with  $x_\gamma$